

Exercises in Pressure Control During Drilling

Pål Skalle



PÅL SKALLE

EXERCISES IN DRILLING FLUID ENGINEERING

Exercises in Drilling Fluid Engineering

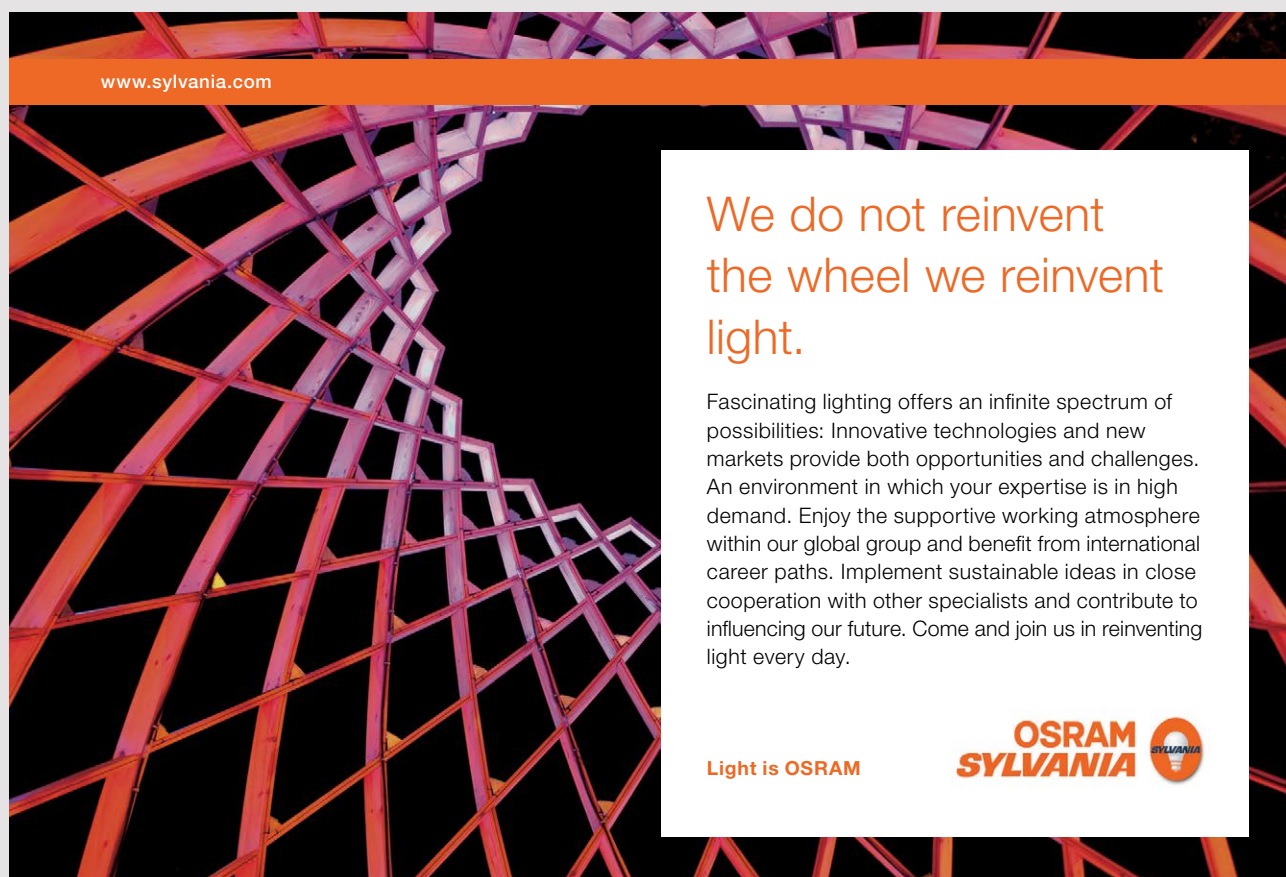
6th edition

© 2018 Pål Skalle & bookboon.com

ISBN 978-87-403-2634-5

CONTENTS

	Preface	8
1	Fluid Properties	9
1.1	Rheology control	9
1.2	Rheology control	9
1.3	Flocculation	10
1.4	Mud contamination	11
1.5	Flocculation	11
1.6	Fluid additives	12
1.7	Fluid additives	13
2	Rheological models	14
2.1	Bingham/ Power law.	14
2.2	Bingham/Power-law	15
2.3	Bingham / Power-law. Regression	17
2.4	Effective viscosity	17



www.sylvania.com

**We do not reinvent
the wheel we reinvent
light.**

Fascinating lighting offers an infinite spectrum of possibilities: Innovative technologies and new markets provide both opportunities and challenges. An environment in which your expertise is in high demand. Enjoy the supportive working atmosphere within our global group and benefit from international career paths. Implement sustainable ideas in close cooperation with other specialists and contribute to influencing our future. Come and join us in reinventing light every day.

Light is OSRAM

**OSRAM
SYLVANIA** 

2.5	All models	18
2.6	All models. Regression	19
2.7	All models	20
3	Drilling fluid dynamics	21
3.1	Velocity profile. Continuity equation	21
3.2	Velocity profile. Momentum flux	21
3.3	Velocity profile	22
3.4	Pressure loss vs. rheology I	22
3.5	Pressure loss vs. rheology II	23
3.6	Pressure loss. Power-law	24
3.7	Pressure loss. Turbulent. Energy equation	24
3.8	Pressure loss vs. flow rate	24
3.9	Pressure loss. Use field data to evaluate model	24
3.10	Pressure loss. Effect of rotation	25
3.11	Pressure loss. Nozzles. OFU	26
3.12	Swab pressure. Cling factor	27
3.13	Swab pressure	27
4	Hydraulic program	28
4.1	Mud pump issues	29
4.2	Optimal nozzles? Section wise	29
4.3	Liner selection. Section wise	30
4.4	Hydraulic program. Section wise (i.e. all liners are treated as if in range I)	30
4.5	Optimal parameters for BHHP. OFU. Section wise	31
4.7	Liner selection. Complete well	33
5	Well challenges	34
5.1	Filtration control	34
5.2	Filtration control	35
5.3	Cuttings concentration I	35
5.4	Cuttings concentration II	36
5.5	Density control	36
5.6	Density control	37
5.7	ECD. Barite	38
5.8	ECD. Fluid and flow	38
5.9	Water activity	39
5.10	Shale stability	40
5.11	Shale stability	42
5.12	Wellbore problem	42

6	Supportive Information	43
6.1	Pump (National 12-P-160) and hydraulic program data	43
6.2	Pressure loss equations	44
6.3	Conversion factors and formulas:	45
	Solutions to exercises in drilling fluid engineering	46
1	Fluid Properties - Solutions	47
1.1	Rheology control - Solution	47
1.2	Rheology control - Solution	48
1.3	Flocculation - Solution	49
1.4	Mud contamination - Solution	50
1.5	Flocculation - Solution	52
1.6	Fluid additives - Solution	53
1.7	Fluid additives - Solution	56
2	Rheological models - Solution	57
2.1	Bingham / Power-law - Solution	57
2.2	Bingham / Power-law - Solution	58
2.3	Bingham / Power-law. Regression - Solution	59
2.4	Effective viscosity - Solution	60
2.5	All models - Solution	62
2.6	All models. Regression - Solution	62
2.7	All models - Solution	65
3	Drilling fluid dynamics - Solution	67
3.1	Velocity profile. Continuity equation - Solution	67
3.2	Velocity profile. Momentum flux - Solution	68
3.3	Flow profile - Solution	69
3.4	Pressure loss vs. rheology I - Solution	71
3.5	Pressure loss vs. rheology II - Solution	74
3.6	Pressure loss. Power law - Solution	76
3.7	Pressure loss. Turbulent flow. Energy equation - Solution	77
3.8	Pressure loss vs. flow rate - Solution	78
3.9	Pressure loss. Field data - Solution	80
3.10	Pressure loss. Effects of rotation - Solution	81
3.11	Pressure loss. Bit nozzle. OFU - Solution	83
3.12	Swab pressure. Clinging factor - Solution	85
3.13	Swab pressure – Solution	86

4	Hydraulic program – Solution	87
4.1	Mud pump issues – Solution	87
4.2	Nozzle selection. Section wise – Solution	89
4.3	Liner selection. Section wise – Solution	90
4.4	Hydraulic program. Section wise – Solution	91
4.5	Optimal parameters with BHHP. OFU. Section wise – Solution	92
4.6	Liner selection. Complete well – Solution	94
4.7	Liner selection. Complete well – Solution	95
5	Wellbore challenges – Solutions	97
5.1	Fluid Properties - solutions	97
5.2	Filtration control – Solution	97
5.3	Cuttings concentration I – Solution	99
5.4	Cuttings concentration II – Solution	100
5.5	Density control – Solution	100
5.6	Density control – Solution	101
5.7	ECD. Barite – Solution	103
5.8	ECD. Flow rate & fluid consistency – Solution	104
5.9	Water activity – Solution	105
5.10	Shale stability – Solution	106
5.12	Wellbore problems – Solution	107
5.11	Shale stability - Solution	109

PREFACE

These exercises have been developed to fit the content of the textbook Drilling Fluid Engineering at www.bookboone.dk. The understanding of the physics and mathematics of the processes has been in focus of both the textbook and the exercises book. Many practical applications have also been created and entered into the collection of exercises. Most of the exercises have been solved and corrected by students in the corresponding course at the Department of Petroleum Engineering and Applied Geophysics at NTNU in Trondheim. If the readers have any comments that could improve the exercises, please contact me at pal.skalle@ntnu.no. Any such comments will be worked into the next year's issue of this book.

Pål Skalle
Trondheim, September 2018

1 FLUID PROPERTIES

We start the numbering at 1.5 after removing some older exercises.

1.1 RHEOLOGY CONTROL

- a) Will YP, PV and μ_{eff} be influenced by the addition of barite?
- b) Why is lye (NaOH) added to the drilling fluid?
- c) Define polymers and the purpose of adding them to the drilling fluid.
- d) Define pseudo plastic, thixotropic and rheopectic fluid behaviour.
- e) Why does viscosity of water increase when Bentonite is added?

1.2 RHEOLOGY CONTROL

- a) Explain how dispersed Bentonite is able to contain up to 18 times its own volume of distilled water. Why is it that the water-holding effect will be reduced when salt is added to the water?
- b) Explain the reason behind the non-Newtonian behavior of Bentonite suspensions.

Out on a drilling rig the questions asked are of practical nature: In the upper wellbore section seawater is often used as drilling fluid. If the viscosifying effect drilled-out clay does not produce the proper viscosity, the addition of Bentonite to the base water has to be considered. Use Figure 1-6 and assume that the quality of the drilled-out clay corresponds to Premium Drilling Clay. Assume that ROP is 35 m/hr while using a 26" bit. The pump rate is 3 000 l/min. The required mud viscosity must at least be 15 cP.

- c) Will the drilled-out formation provide the required viscosity?
- d) What is the yield (m^3 of mud/ton solids) of Wyoming Bentonite? ($\rho_{\text{Bentonite}} = 2.4 \text{ kg/l}$)
- e) What is the water density (originally 1.0 kg/l) after the addition of Bentonite, when an effective viscosity of 50 cP is reached?

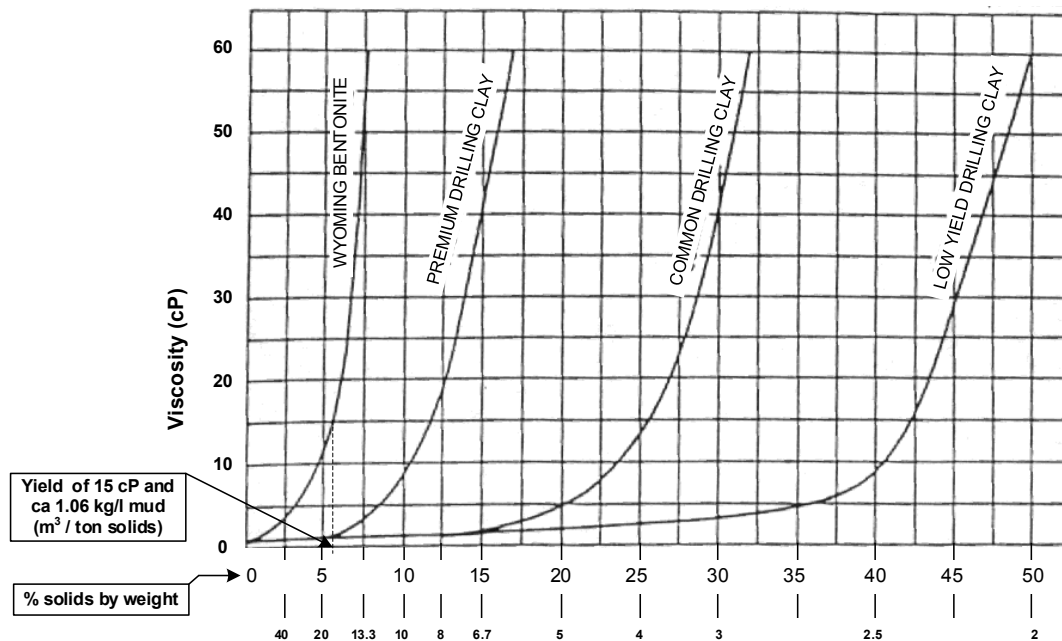


Figure 1-6: The ability of different solids to produce viscosity.

1.3 FLOCCULATION

Bentonite and polymers are the dominating viscosity agents. Bentonite is still widely used. We therefore have to understand its behavior properly. Bentonite behaves different from other additives; it swells and flocculates.

- Why does Bentonite flocculate (weak flocculation)?
- What will happen if untreated water based mud is used while drilling through the cement located in the casing shoe area? Explain what happens to the mud (exposed to strong flocculation) and the respective operational consequences. Sketch the flow curve of the mud before and after having drilled through the cement.
- Name 3 factors which enhance flocculation of Bentonite.
- Why does WBM behave shear-thinning?
- Why does WBM behave thixotropic?
- Explain the difference in flocculation tendency of pure edge-to-face and of cross-linking caused by external agents.

1.4 MUD CONTAMINATION

- a) What is a contaminated mud, and how are the drilling fluid parameters restored?
- b) The geologist expected that layers of silty anhydrite would be penetrated at a vertical depth of 1600 m. The mud engineer was therefore told to make measurements every 15 min. of the returning mud. The results are shown in the table below. After penetrating the anhydrite he observed that the viscosity of the mud, a dispersed WBM system, started to rise and became abnormally thick. Drilling continued and after a few hours of drilling/pumping, the viscosity fell back to a lower level than the original viscosity.

Parameter		Shear stress at RPM of			ρ	V _{filtrate}
		600	300	100		
Unit		(lb/100ft²)			kg/l	ml / 30 min
Time	0900	42	28	16	1.31	7
	0915	41	27	17	1.31	6
	0930	68	54	37	1.31	18
	1145	31	17	5	1.30	7

Together with the mud engineer you are responsible for the maintenance of the drilling fluid program. Explain changes in the recorded parameters observed at 0930 and at 1145. Suggest countermeasures against these changes.

- c) Assume two clay suspensions are flocculating for two different reasons during drilling operations; 1. Edge-to-face. 2. Calcium attack. How do the two clay suspensions behave rheologically? Make a sketch of the in-situ shear stress vs. time; during drilling into the Ca⁺⁺ containing layer. Assume you drill in the contaminated zone for 10 min. Then turn off the pump for 10 min. Continue drilling for 10 min till you are out of the contaminated zone.

1.5 FLOCCULATION

- a) Find necessary YP to keep a spherical particle suspended in a mud of $\rho_{\text{mud}} = 1.1 \text{ kg/l}$. The particle has these characteristics:
- $$d_p = 5 \text{ mm}$$
- $$\rho_p = 2.3 \text{ kg/l}$$
- Similarly, find out what is the maximum size the particles can be kept suspended at when YP = 15 Pa.

- b) At 12:00 the ROP became very low and it was decided to change the bit. A 15 min. stop in the operation was made before tripping-out from 2 100 mMD was initiated. When the first pipe was broken mud spilled out on the drill floor. Could this spill have been prevented? How high up can the string be hoisted before gravity pulls the mud down in the following situation:

$$\tau_{\text{gel } 15 \text{ min}} = 30 \text{ lb/100 ft}^2 \text{ (14.4 Pa)}$$

$$\text{Inner diameter of the drill pipe} = 4.127'' \text{ (104.85 mm)}$$

1.6 FLUID ADDITIVES

- a) Define the different concepts in the two columns below and explain their relevance for drilling fluids (e.g.; PAC = partially anionic cellulose - viscosifier).

Anhydrite	Lignosulphonate
Caustic soda	Lignite
CEC	MBT
Chalk	PAC
CMC	Pre hydrated
Colloid	PHPA
Dispersator	SAPP
Deflocculators	Sodium Sulphate
Gypsum	Starch
HEC	Xanthan
NaOH	

- b) How does the additive called “drag reducer” reduce turbulent pressure so dramatically?
 c) What significance does the K^+ concentration have for the shale?
 d) When drilling into swelling clay and swelling shale, problems like sloughing shale and stuck pipe may occur. Explain what happens to the mud. How and why do you convert Bentonite mud into gyp mud?

1.7 FLUID ADDITIVES

- a) How many moles/liter of hydroxyl (OH^-) concentration is required to change the pH of a drilling fluid from 7.5 to 11?
- b) How much caustic soda (weight per liter) will be required to increase the pH in question a)?
- c) Why is potassium hydroxide (KOH) often preferred to sodium hydroxide (NaOH) in controlling the pH of mud?

How does drilling fluids achieve the following functions:

- d) Lift cuttings from the bottom to the surface
- e) Releases cuttings at the surface
- f) Cool and lubricate the drill bit and the drill stem
- g) Prevent blowouts



Discover the truth at www.deloitte.ca/careers

Deloitte.

© Deloitte & Touche LLP and affiliated entities.



2 RHEOLOGICAL MODELS

To simplify the evaluation of drilling fluids out in the field, the simplified Bingham field method was developed. In this collection of exercises we distinguish between the simplified field method and the standard method of determining rheological model constants.

The simplified field method is applicable in conjunction with the Fann viscometer. For the standard method the Fann readings are converted to SI units and multiplied with the factor 1.067 (see SPE's Applied Drilling Engineering textbook Appendix A, eqn. A-6b).

Note also that conversion factors are presented in Chapter 6 in the corresponding textbook at BookBoon.

2.1 BINGHAM/ POWER LAW.

In the laboratory the data in Table 2-1 were obtained (θ is the dial reading in the viscometer):

Parameter	RPM	γ	θ	τ	τ
Unit		(s^{-1})	(-)	(lb/100ft ²)	(Pa)
Data	600	1022	106.4	112.8	54.0
	300	511	75.0	79.5	38.1
	100	170	42.4	44.9	21.5
	6	10	10.0	10.6	5.1
	3	5	6	6.3	3.0

Table 2-1: Rheological data.

The same data are presented as a flow curve in Figure 2-1.

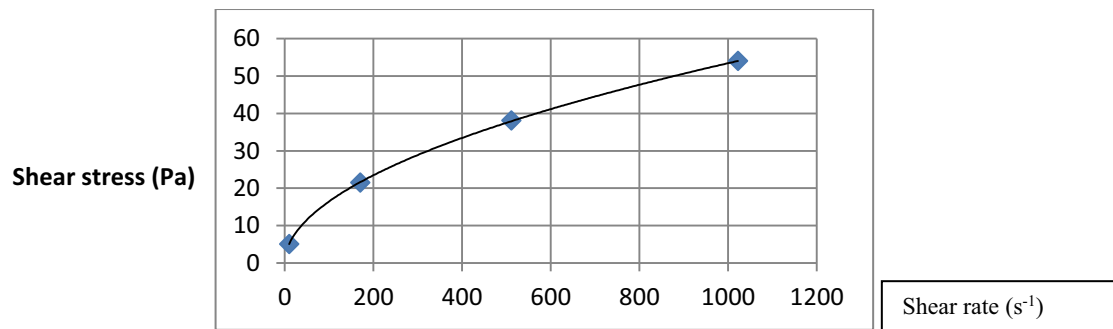


Figure 2-1: Flow curve of the rheological data from the Table 2-1.

- Find rheological constants for the two rheological models Bingham and Power-law. For Bingham model use both field and standard method.
- Which one of the two models in question a) fits the shear stress best at 100 RPM.
- Which one of the three models, Newtonian, Bingham or Power-law, would give the best answer on basis of the given rheology while pumping 1000 l/min through a pipe of 10 cm ID. Hint: Check theoretical vs. measured shear stress.

2.2 BINGHAM/POWER-LAW

Rheological data are tabulated and presented graphically in Figure 2-2. Note that shear stress, τ , has also been multiplied by 1.067 before converting readings, θ , to SI-units.

Parameter	RPM	$\dot{\gamma}$	θ	τ
Unit	-	s^{-1}	-	Pa
Data	600	1022	140	71.52
	300	511	98	50.06
	200	340		39.60
	100	170		27.39
	6			8.14
	3			6.14

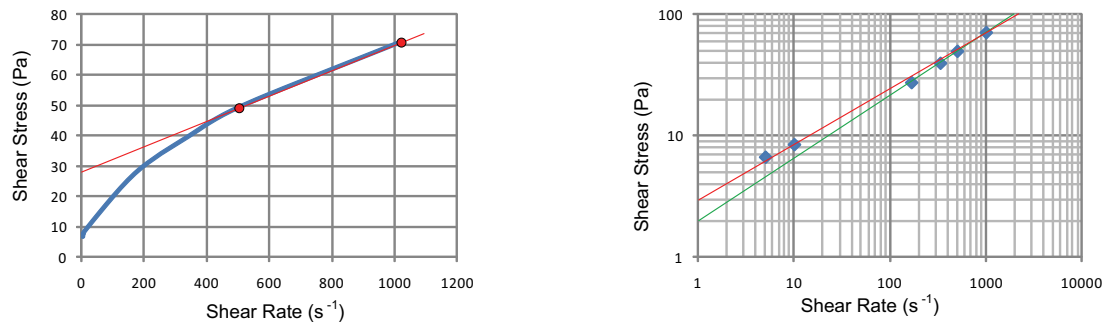


Figure 2-2: Graphical representation (flow curve) of rheological data.

- Select the best 2-data-point-rheology model, either Bingham or Power-law (at a viscometer speed of 100 RPM). Verify selection.
- Observe the log-log plot. It represents a typical clay-dispersed system. Why do the two data points of the lowest shear rate deviates from the straight line made on basis of the upper four data points?

Cynthia | AXA Graduate

**AXA Global
Graduate Program**

Find out more and apply

redefining / standards



2.3 BINGHAM / POWER-LAW. REGRESSION

After measuring the rheology of the fluid it is always useful to plot its flow curve. The following data are obtained:

Text	Speed		Reading	Shear stress	
Symbol	$\dot{\gamma}$		θ	τ	
Unit	(rpm)	(s ⁻¹)	(-)	(lbf/100 ft ²)	(Pa)
Data	600	1022	60.4	64	30.6
	300	511	39.6	42	20.2
	200	340	32.1	34	16.3
	100	170	24.5	26	12.5
	6	10	14.2	15	7.2
	3	5	9.4	10	4.8

- a) Plot τ vs. $\dot{\gamma}$ for three rheological models; Newtonian, Bingham and Power-law according to:

Field procedure (2 data points) (only for Bingham)

Standard procedure (2 data points) (for all models)

Regression (6 data points). Use Excel linear regression.

Find the constants of the three models. Determine which of the models are best fitted to the readings at high shear rates, i.e. for determining pressure loss in nozzles and inside the drill string (300 rpm and higher), and what model fits best to the lower shear rates, valid for annulus or flow (100 rpm and lower).

- b) An exercise without calculations: Will plug flow occur in this mud system?

2.4 EFFECTIVE VISCOSITY

- a) Rheology data:

Rotational speed	Dial Reading
600 rpm	43
300 rpm	30
200 rpm	23
100 rpm	16
6 rpm	8
3 rpm	7

A useful exercise is to plot the effective viscosity (apparent Newtonian viscosity) as a function of shear rate. The non-Newtonian and the shear thinning effect will then appear clearly.

- b) The mud is flowing in a 1000 m long pipe with inner diameter of 4 in, flow rate is 6 000 l/min (two pumps) and density is 1.1 kg/l. Use the Power-Law to estimate μ_{eff} at this flow rate.
- c) Determine the pressure loss in the pipe (Power-law).
- d) Why are drilling fluids often so well suited to the Bingham model?

2.5 ALL MODELS

The flow rate is 2 500 lpm in a 1000 m long pipe with an inner diameter of 10 cm. Rheological data points are given below. The mud density is 1.1 kg/l.

Shear rate (s^{-1})	Shear stress (Pa)
1022	55
511	40
340	35
5	19

- a) Find the rheological constant just for Bingham and Power-law (use only upper 2 data points).
- b) For Herschel-Bulkley model, discuss three different ways of obtaining the constants without calculation.
- c) Show that the effective viscosity for Bingham fluids is:

$$\mu_{\text{eff}} = \mu_{pl} + \frac{\tau_0 d}{6v}$$

- d) Explain why the Bingham field model is so useful for evaluating mud behavior.

2.6 ALL MODELS. REGRESSION

Symbol	$\dot{\gamma}$	RPM	θ	τ	τ
Unit	Hz	rpm	-	lb/100 ft ²	Pa
Data	1022	600	50	53	25.4
	511	300	34	36	17.2
	340	200	26	27.6	13.2
	170	100	17	18	8.6
	102	60	13	13.8	6.6
	51	30	9	9.5	4.5
	10	6	4	4.2	2.0
	5	3	3	3.2	1.5

- Use the Fann-viscometer data above to determine model-constants for the first 2 models listed in point b) below through standard (2 data points) procedure.
- Perform linear regression procedure (use Excel spread sheet). Make a plot of the results from the two first models in the list for 2, 4, 6 and 8 data points. Linear regression in Excel is in fact possible only for those two models. The lower three models are presented just to give an overview of available rheological models.

I joined MITAS because
I wanted **real responsibility**

The Graduate Programme
for Engineers and Geoscientists
www.discovermitas.com



Month 16

I was a construction supervisor in the North Sea advising and helping foremen solve problems

Real work
International opportunities
Three work placements



MAERSK

Bingham	$\tau = \tau_y + \mu_{pl} \cdot \dot{\gamma}$
Power law	$\tau = K \cdot \dot{\gamma}^n$
Herschel Bulkley (H-B)	$\tau = \tau_y + K \dot{\gamma}^n$
Collin-Graves (C-G)	$\tau = (\tau_o + K \dot{\gamma}^n) (1 - e^{-B\dot{\gamma}})$
Robertson-Stiff (R-S)	$\tau = K(\gamma_o + \dot{\gamma})^n$
Casson	$\tau = [\sqrt{\tau_o} + \sqrt{\mu \cdot \dot{\gamma}}]$

c) To solve H-B, use two methods:

- c1) Elimination and iteration.
- c2) Non-linear regression.

The latter procedure is presented in Chapter 10.6 in the Drilling Fluid Engineering Textbook.

2.7 ALL MODELS

Parameter	Speed	Shear Stress	
Unit	RPM	lb / 100 fl ²	Pa
Data	1022	52.2	25
	511	35.5	17
	340	25.1	12
	170	13.6	6.5
	10	6.3	3.0
	5	4.2	2.0

Which of the following three models, Power-law, Bingham and Herschel-Bulkley would give the most trustworthy answer for estimating τ at $\dot{\gamma} = 10$ Hz. Apply the two and three upper data points. Use Field and standard procedure for the Bingham 2-data point model. For the Herschel-Bulkley model, use the τ_5 reading as τ_o . K and n are found from Power-law. This you find out by comparing the resulting model graph with the measured data.

$$\tau = \tau_o + \mu \cdot \dot{\gamma}$$

$$\tau = K \cdot \dot{\gamma}^n$$

$$\tau = \tau_o + K \cdot \dot{\gamma}^n$$

3 DRILLING FLUID DYNAMICS

3.1 VELOCITY PROFILE. CONTINUITY EQUATION

The incompressible steady state flow between two parallel plates with breadth b in Figure 3.1 is initially uniform at the entrance; $v = \bar{v} = 8 \text{ cm/s}$. Downstream the flow develops into the parabolic laminar profile $v(z) = az(z_0 - z)$, where a is constant and z_0 the plate distance. If $z_0 = 4 \text{ cm}$, what is the value of $v_{\max}$?

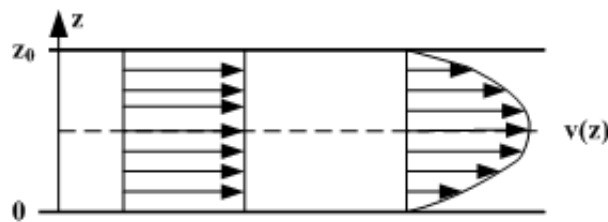


Figure 3-1: Flow data.

3.2 VELOCITY PROFILE. MOMENTUM FLUX

- The fully developed laminar pipe-flow velocity profile is expressed as: $v_z(r) = v_{\max} (1 - r^2 / R^2)$, $v_\theta = 0$, $v_r = 0$. z indicates here the axial direction: This is an exact solution to the cylindrical Navier-Stoke equation. Neglect gravity and compute the pressure distribution in the pipe; $p(r,z)$, and the shear-stress distribution; $\tau(r,z)$, using R , $v_{\max}$ and μ as parameters. Why does the maximum shear occur at the wall?
- For flow between parallel plates, compute b1) wall shear stress and b2) the average velocity. From the Text book, Chapter 4, we find that $v_z(y) = -dp/dz \cdot h^2/2 \mu (1 - y^2/h^2)$. The most general definition of shear stress is given by: $\tau = \tau_z = \mu \left(\frac{\partial v_z}{\partial y} + \frac{\partial v_y}{\partial z} \right)$

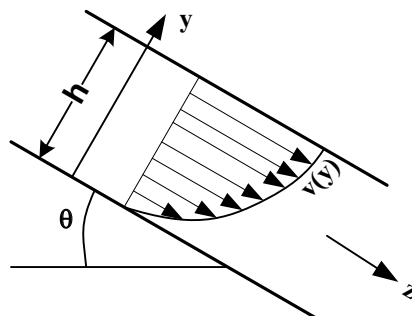


Figure 3-2: The geometry of pipe flow in the z -direction. $\theta = 0$ in this exercise.

3.3 VELOCITY PROFILE

- a) Discuss the meaning of this expression, its assumptions etc.

$$\frac{dp}{dx} = -\frac{1}{r} \frac{\partial}{\partial r} \left(r \mu \frac{\partial v_x}{\partial r} \right)$$

- b) For stationary non rotational and laminar flow of Newtonian fluids in circular horizontal pipes ($z = x$), show that $v(r) = \frac{dp/dx}{4\mu} (R^2 - r^2)$
- c) Determine first the average velocity. The absolute velocity is largest in the center of the pipe. Max velocity compared to the average velocity is forming an expression of the axial dispersion when one fluid is displaced by another. Find this expression.
- d) Find wall shear stress and average pipe velocity when the pressure loss is recorded to be 0.9 bar along a 1 000 m long pipe. Pipe radius is 5 cm and fluid viscosity 53.8 cP

3.4 PRESSURE LOSS VS. RHEOLOGY I

Water, assumed incompressible, flows steadily through a pipe of constant diameter $2R$. The entrance velocity is constant, $u = u_0$, and downstream the flow becomes turbulent, $u = u_{\max} (1 - r/R)^{1/4}$. Fluid viscosity is μ .

ie business school

93%
OF MIM STUDENTS ARE
WORKING IN THEIR SECTOR 3 MONTHS
FOLLOWING GRADUATION

MASTER IN MANAGEMENT

- STUDY IN THE CENTER OF MADRID AND TAKE ADVANTAGE OF THE UNIQUE OPPORTUNITIES THAT THE CAPITAL OF SPAIN OFFERS
- PROPEL YOUR EDUCATION BY EARNING A DOUBLE DEGREE THAT BEST SUITS YOUR PROFESSIONAL GOALS
- STUDY A SEMESTER ABROAD AND BECOME A GLOBAL CITIZEN WITH THE BEYOND BORDERS EXPERIENCE

Length: 10 MONTHS
Av. Experience: 1 YEAR
Language: ENGLISH / SPANISH
Format: FULL-TIME
Intakes: SEPT / FEB

5 SPECIALIZATIONS
PERSONALIZE YOUR PROGRAM

#10 WORLDWIDE
MASTER IN MANAGEMENT
FINANCIAL TIMES

55 NATIONALITIES
IN CLASS

www.ie.edu/master-management | mim.admissions@ie.edu | [f](#) [t](#) [i](#) Follow us on IE MIM Experience

- Determine the average velocity at turbulent flow. Use the viscometer readings from exercise 2.6.
- Determine the pressure loss pr. 1000 m in a 10 cm ID pipe at a flow rate of 1000 l/min. and a fluid density of 1000 kg/m³. Use three rheological models. The observed pressure loss at these circumstances were 4.5 bar.
- Calculate shear rates in the pipe for Bingham, Power-law and Newtonian model. Read shear stress from the flow curve, and determine pressure drop through the universal pressure loss model.

$$\Delta p = \tau_w \cdot \frac{L}{d} \cdot 4$$

- Show that wall shear stress can be expressed as $\tau_w = \frac{1}{2} R \cdot \frac{\Delta p}{\Delta L}$

for laminar, annular pipe flow, and $\mu_{eff} = \mu_{pl} + \frac{\tau \cdot d_{hydr}}{8 \bar{v}}$

- What effect has entrance length of a uniform pipe on estimated pressure loss?

3.5 PRESSURE LOSS VS. RHEOLOGY II

Mud is pumped at a rate of 800 l/min with these rheological data:

RPM	θ	τ (lb/100 ft ²)
600	66.0	70
300	47.2	50
100	25.5	27
6	9.4	10

- Find Δp_{pipe} in a 1000 m long pipe of $d = 0.109$ m for a field-Bingham fluid. Fluid density is 1100 kg/m³.
- Which rheological model, Newtonian or field-Bingham, is better suited for pressure loss estimation when the actual Δp_{pipe} was recorded to be 0.7 MPa. Apply the universal pressure loss model; $\Delta p = 4 \tau L / d$.

3.6 PRESSURE LOSS. POWER-LAW

a) Derive the laminar pressure loss expression in pipes for Power-Law fluids from the force balance.

b) Show that:

$$\frac{\rho v d}{\mu_{eff}} = N_{Re_{generalized}}$$

when μ_{eff} for a Power-law fluid is applied.

c) Show that the Reynolds number for a Power-law fluid increases as the inner pipe diameter of the annulus decreases, while for a Newtonian it decreases. Strange! Apply annular diameter in terms of $d_{hydr} = d_o - d_i$, and let flow rate be constant.

3.7 PRESSURE LOSS. TURBULENT. ENERGY EQUATION

Oil of density $\rho = 900 \text{ kg/m}^3$ and a kinematic viscosity $\nu = 0.00001 \text{ m}^2/\text{s}$, flows at a rate of $0.2 \text{ m}^3/\text{s}$ through a 500 m new cast-iron pipe of a diameter of 200 mm and a roughness of 0.26 mm. Determine the head loss.

3.8 PRESSURE LOSS VS. FLOW RATE

Make a graph of pressure loss vs. flow rate in a 1000 m long pipe of an inner diameter of 10 cm. Rheological data-points are given in Exercise 2.6 above, and the mud density is 1.1 kg/l. Select the Power law model for this purpose.

3.9 PRESSURE LOSS. USE FIELD DATA TO EVALUATE MODEL

Prior to a pre flush/cementing operation the driller performed several pressure tests to verify theoretical pressure estimations. Previous comparisons between the actual pressure readings during drilling with theoretically estimated pressure loss resulted in large deviations. He was convinced that the deviations could be back-tracked to the pressure drop across the mud motor and the bit. These two losses can only be estimated by means of empirical models and are thus highly uncertain. Now he had the chance to record pressure loss without these two disturbing pieces of equipment installed. After lowering the 5" * 4.127" DP (without the bit) down to the casing shoe he circulated for 45 min. to neutralize temperature effects. The casing, a 13 3/8", 68 lb/ft, (ID=12.40") had its casing shoe at 4 500 mMD. The pump was a relatively new (volumetric efficiency = 0.96) Garden-Denver PZ-11-1600 HP triplex mud pump, 6" liner. One complete pump stroke delivered 15.29 l. At the following pump speeds, with no drill string rotation, he read the average stand pipe pressures (SPP) which was the average of 3 tests:

- 5 spm - 13 (+/-2) bars
- 20 spm - 70 (+/-3) bars
- 50 spm - 100 (+/-5) bars
- 100 spm - 200 (+/-10) bars

Rheology of drilling fluid at this temperature is identical with the one in Task 2-1 above. Apply the Power -Law model. Mud density was 1.21 kg/l. The recorded pressure losses are presented in Figure 3-10 below. Estimate pressure losses and compare them with the recorded ones.

3.10 PRESSURE LOSS. EFFECT OF ROTATION

In this task you need to use your imagination. The driller made an additional test: At the lowest and the highest pump speeds [5 and 100 SPM from Task 3.9 above] he rotated the drill string at 100 RPM for a short time and saw that the average reading changed to 8 and 248 bars respectively at the two selected pump speeds. Determine the effect of rotation on the mud's rheology for the given flow rate (the changed rheology is obviously dictating the changed annular pressure loss). Assume that the rotational movement is additive to the axial flow with respect to shearing effect on the fluid. When determining the shear effect, simply



"I studied English for 16 years but...
...I finally learned to speak it in just six lessons"

Jane, Chinese architect

ENGLISH OUT THERE

Click to hear me talking before and after my unique course download

use the average rotational velocity across the annular gap. Assume also that the drilling fluid is the same as in task 3.9, a Power-law model with $n = 0.5$, $K = 1.63$. The author admit that this task contains many simplifying assumptions. But is only a model, which must be tested to verify the assumptions.

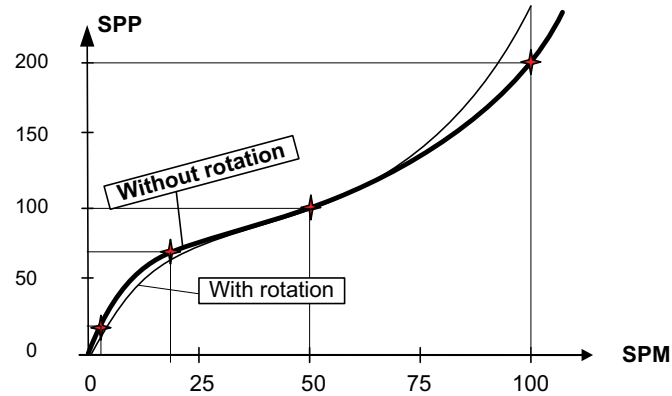


Figure 3-10: Recorded SPP (thick line), with rotation (thin line).

3.11 PRESSURE LOSS. NOZZLES. OFU

After having drilled a 17.5" hole the 13 3/8" casing was set and cemented at 2 300 mMD. Finally a 12 1/4" hole was drilled down to the reservoir at 2 500 mMD.

The drill string consisted of a drill pipe (54.276") and 100 m of drill collars (6.25 · 3.1"). The circulating rate was 800 GPM during drilling and the mud density was 12.9 PPG. A Fann-VG viscometer gave the following readings:

$$\begin{aligned}\theta_{300} &= 50 \\ \theta_{600} &= 85\end{aligned}$$

Assume the mud rheology is best described through the Bingham model. OFU-equations are copied from Applied Drilling Engineering SPE-text book Table 4.6:

$$N_{Re} = 928 \rho \bar{v} d_h / \mu_{eff} \quad \bar{v} = q / (2.448 d_h^2)$$

$$\Delta p_{lam} / \Delta l = \frac{\mu_{pl} \bar{v}}{1500 d^2} + \frac{\tau_y}{225 d}$$

$$\Delta p_{turb} / \Delta l = \frac{\rho^{0.75} \mu_{pl}^{0.25} \bar{v}^{1.75}}{1800 d^{1.25}}$$

$$\Delta p_{bi} = \frac{8.311 \cdot 10^{-5} \cdot \rho \cdot q^2}{C_d^2 \cdot A_t^2} [\text{psi}]$$

The OFU units are:

ρ	-	PPG
q	-	GPM
A	-	in ²
p	-	psi
C_d	-	0.95

- a) The pressure drop through the annulus located above the BHA was equal to 100 psi. Calculate it along the BHA. What is the equivalent circulating density at a depth of 2 500 m?
- b) The bit had 5 nozzles, each of a diameter of 14/32 inches. Pressure loss through the surface pipes was 200 psi. What pressure is required from the pump when drilling at a depth of 2 500 m? Compare the results with bit pressure loss estimated in SI-units.

$$\Delta p_{bit} = 1.11 \cdot \frac{1}{2} \rho v_{Av}^2$$

- c) Determine the pressure loss in the complete circulation system.

3.12 SWAB PRESSURE. CLING FACTOR

Due to the no-slip conditions on all surfaces, the mud will “cling” to the drill string. The cling factor is used during estimation of surge & swab pressure. How would you, in a stepwise fashion, go about to define and estimate the cling factor?

3.13 SWAB PRESSURE

Assume you are tripping out while simultaneously pumping. Your task is to start the process of deriving an expression of the swab pressure during laminar flow. When making a drawing of the process, use parameters like v_p (pipe), q_p (pump), R_w (wellbore), R_p (pipe), R_0 (the point where the flow velocity is zero), etc, as required for your explanation.

4 HYDRAULIC PROGRAM

The exercises which are related to the hydraulic program distinguish between two different approaches of preparing the hydraulic program:

- a) The standard method: Each liner represents the pump's capability. The hydraulic program is planned for one well section at a time.
- b) The extended method: All the piston sizes are treated as part of one process, and they are divided into two operating ranges. The hydraulic program is planned for all well sections in one common operation.

Both the methods are based on maximizing the ROP, which (in this book) is expressed through the following equation:

$$\text{ROP} = A \cdot (q / d_{\text{nozzle}})^{a8}$$

Excellent Economics and Business programmes at:



university of
 groningen



**“The perfect start
of a successful,
international career.”**

CLICK HERE
to discover why both socially
and academically the University
of Groningen is one of the best
places for a student to be

www.rug.nl/feb/education

4.1 MUD PUMP ISSUES

- Characterize a mud pump as detailed as possible with respect to
 - Effect
 - Efficiency
- Why are several mud pumps sometimes arranged in parallel or in series?
- Compare centrifugal to piston pumps
- Explain the term hydraulic knocking in pumps
- A tri-cone bit has 3 nozzles; each nozzle is $15/32^{\text{nd}}$ inch in diameter; $\rho_{\text{mud}} = 1.3$ kg/l; and you are drilling at a depth of 2 500 mMD. At two different pump rates (which are close to the actual operating flow rates), the following pressures (stand-pipe pressures) were recorded:

q_{pump} (lpm)	p_p (bar)
2 500	230
670	33

Determine the value of K_1 and m in the expression of the parasitic pressure in an oil well.

4.2 OPTIMAL NOZZLES? SECTION WISE

A tricone bit is equipped with $3 \cdot 15/32''$ nozzles. The following data are given:

$$\begin{aligned}
 p_{p1} &= 186 \text{ bar at } 2\,000 \text{ l/min (p is measured at the standpipe)} \\
 p_{p2} &= 120 \text{ bar at } 1\,750 \text{ l/min} \\
 p_{\text{bit}} &= 1.11 \cdot \frac{1}{2} \rho v_{\text{nozzle}}^2 \\
 p_{\text{pumpe,max}} &= 270 \text{ bar for piston in use} \\
 q_{\text{pumpe,max}} &= 2\,700 \text{ l/min for piston in use} \\
 q_{\text{min,ann}} &= 1\,700 \text{ l/min (below this value cuttings will accumulate in the well)} \\
 q_{\text{max,ann}} &= 2\,600 \text{ l/min (above this value the wellbore wall adjacent the BHA} \\
 &\text{will start to erode)} \\
 D &= 3\,000 \text{ m} \\
 \rho_{\text{mud}} &= 1\,400 \text{ kg/m}^3 \\
 q_{\text{opt}} &= \left[\frac{2p_{\text{pumpe,max}}}{K_1 D(m+2)} \right]^{1/m}
 \end{aligned}$$

- Determine the two constants in the parasitic pressure loss equation.
- Determine optimal flow rate at 3 000 m depth.
- What is the optimal nozzle size of the three nozzles at the depth of 3 000 m? (in terms of $x/32$ inch).

4.3 LINER SELECTION. SECTION WISE

The operating data of a National 12-P-160 (this number indicates a 1600 HP pump) triplex pump are presented in this exercise book's Chapter 6 – Supportive Information.

$$D = 2\,500\text{ m}$$

$$\rho = 1\,200\text{ kg/m}^3$$

$$K_1 = 1.6 \cdot 10^6$$

$$m = 1.7$$

$$q_r = 0.018\text{ m}^3/\text{s} \left(d_{bit} = 12\frac{1}{4}'' \right)$$

$$q_{\max}(turb) = 0.04\text{ m}^3/\text{s}$$

- Derive an expression of q_{opt}
- Select the most optimum liner at this depth
- Determine the optimal bit pressure when the 6" liner is used
- At what depth would you change from 6" to 5 3/4" liners?

4.4 HYDRAULIC PROGRAM. SECTION WISE (I.E. ALL LINERS ARE TREATED AS IF IN RANGE I)

- Assume the rate of penetration (ROP) is a function of bottom hole cleaning:

$$ROP = A \cdot \left(\frac{q}{d_e} \right)^{a_s}$$

Show that ROP will decrease with depth when the pump pressure is expressed through the equations below:

$$p_{pump} = p_{loss} + p_{bit}$$

$$p_{loss} = K_1 D q^m$$

$$p_{bit} = 1.11 \frac{1}{2} \rho \bar{v}^2$$

- The 12 1/4" section starts at the 13 3/8" casing shoe at 1950 m MD, and is planned to reach a depth of 4000 mMD before setting the next casing. The following is known:

$$K_1 = 2 \cdot 10^6$$

$$m = 1.65$$

$$q_{r, \text{ vertical l}} = 0.025\text{ m}^3/\text{s}$$

$$q_{r, \text{ horiz.}} = 0.040\text{ m}^3/\text{s}$$

$$q_{\max, \text{ vertical}} = 0.035\text{ m}^3/\text{s}$$

$$q_{\max, \text{ horiz.}} = 0.045\text{ m}^3/\text{s}$$

What flow rate and liner size would you recommend through this depth interval when drilling either a vertical well or a horizontal well? Use the 1600 HP pump as defined in Supportive Information.

4.5 OPTIMAL PARAMETERS FOR BHHP. OFU. SECTION WISE

This exercise includes Oil Field Units, just to indicate for you how much simpler it is to work with SI units.

The bit has $3 \cdot 12/32''$ nozzles, and $\rho_{\text{mud}} = 10$ PPG while drilling at 8 200 ftMD. The following pump rates and pump pressures ($q_r = 240$ GPM) were recorded while the bit was close to the bottom of the well:

q_{pump} (GPM)	p_p (psi)
500	3000
250	800

The pump is characterized through:

$$p_{\text{max}} = 3620 \text{ psi}, E_{p,\text{max}} = 1000 \text{ Hp}$$

American online
LIGS University
 is currently enrolling in the
 Interactive Online **BBA, MBA, MSc,**
DBA and PhD programs:

- ▶ enroll **by September 30th, 2014** and
- ▶ **save up to 16%** on the tuition!
- ▶ pay in 10 installments / 2 years
- ▶ Interactive Online education
- ▶ visit www.ligsuniversity.com to find out more!

Note: LIGS University is not accredited by any nationally recognized accrediting agency listed by the US Secretary of Education. More info [here](#).





Determine optimal pump rate and nozzle size when applying Bit Hydraulic HP (BHHP) as the optimization criteria. Assume also for this criteria that the rate of penetration is directly related to it. The pump volume efficiency is 0.9.

$$\text{BHHP} = \frac{\Delta p_{\text{bit}} \cdot q}{1714} \quad (\text{Hp})$$

Pressure drop in OFU are $(\rho(\text{PPG}), q(\text{GPM}), A(\text{in}^2), C_d = 0.952)$

$$\Delta p_{\text{bit}} = 8.311 \cdot 10^{-5} \cdot \rho [q / (C_d \cdot A_{\text{nozzle}})]^2$$

4.6 Liner selection. Complete well The characteristics of a 1600 HP piston pump are found in Chapter 6; Supportive Information, while the optimal operational functions are presented graphically in Figure 4-6. The optimal pump pressure values are in general the maximum ones, given for each liner size. Maximum values are the recommended values in the pump's liner table, which in fact are around 85 % of the absolute maximum. In Figure 4-6 the flow rates are in correct scale, while R_p -values are only qualitative. Hydraulic parameters, the bit program and minimum and maximum flow rates are presented below and in Table 4-6:

$$K_{\text{I in range II}} = 1.80 \cdot 10^6, m_{\text{II}} = 1.6$$

$$K_{\text{I in range I}} = 2.20 \cdot 10^6, m_{\text{I}} = 1.5$$

Bit diameter	Start depth	Permissible annular flow rate (m ³ /s)	
in	m	min	max
36	0	0.035	0.050
26	100	0.030	0.045
17 1/2	500	0.027	0.035
12 1/4	1500	0.015	0.030
8 1/2	3000	0.010	0.020

Table 4-6: Bit program and flow rate ranges

- a) Operating range I is defined as the pump operating range of the smallest liner, while range II is defined by the remaining liners. Show that the optimal flow rate, $q_{\text{opt II}}$, in pump area II, by maximizing the ROP (see the introduction of Chapter 4), is:

$$q_{optII} = \left[\frac{(E_p)_{\max}}{K_1 D(m+2)} \right]^{\frac{1}{m+1}}$$

- Determine at which depth Range II stops (while drilling downwards) and at what depth the maximum flow rate turns into the theoretical optimum flow rate of Range I.
- Draw also into the graph the optimal hydraulic program (the graph is a principal drawing of ROP vs. q and thus not a quantitatively correct drawing).
- What pump rate is optimum at 2 000 m.

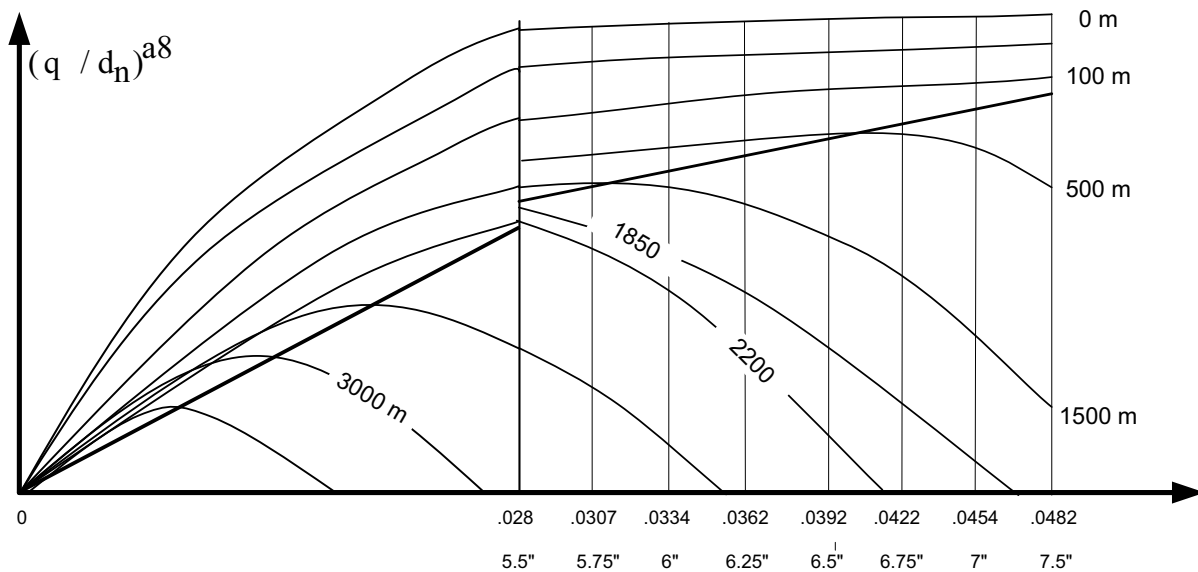


Figure 4-6: Hydraulic Data.

4.7 LINER SELECTION. COMPLETE WELL

A 1660 HP pump is used (see Supportive Info).

- Find at what depths the transition from operating area II to I occur. A 1660 HP pump is used (see Supportive Info. K_1 and m are the same for both ranges:
 $K_1 = 1.72 \cdot 10^6$
 $m = 1.51$
- Make a flow chart of a computer program of how to determine when to change from working area II to I during drilling.

5 WELL CHALLENGES

5.1 FILTRATION CONTROL

- How can we plan the mud composition in WBM to minimize the fluid loss through the filter cake?
- If the fluid loss shows an increasing tendency during drilling, how is it detected and how is the problem treated?
- Two sand formations of nearly equal pore pressure are encountered. Will filtrate invasion be greater in the sand of high permeability and high porosity, than in one with low porosity? The final filter cake permeability in both sands is assumed to end up at around 10^{-3} mD
- A reduction of water flow into shale is beneficial because this will reduce unwanted reaction between the drilling fluid's water phase and shale further away from the wall, where the water activity of the pore water may be different. How can the water-flow into clay be controlled?



DON'T EAT YELLOW SNOW

What will your advice be?

Some advice just states the obvious. But to give the kind of advice that's going to make a real difference to your clients you've got to listen critically, dig beneath the surface, challenge assumptions and be credible and confident enough to make suggestions right from day one. At Grant Thornton you've got to be ready to kick start a career right at the heart of business.

Sound like you? Here's our advice: visit [GrantThornton.ca/careers/students](https://www.grantthornton.ca/careers/students)

Scan here to learn more about a career with Grant Thornton.



 **Grant Thornton**
An instinct for growth™

© Grant Thornton LLP. A Canadian Member of Grant Thornton International Ltd

5.2 FILTRATION CONTROL

We want to obtain a physical picture of how far the filtrate and the particles penetrate a porous formation and gradually stops due to a tight filter cake. A 15" hole with open hole length of 4 000 ft is being drilled. The bottom 10 % of the borehole length is of porous formation (defining the filter area) with a porosity of 15 %. Assume that this porosity corresponds to the porosity of the laboratory filter paper. The filter area A of the filter press is 45 cm^2 ($r = 3.9 \text{ cm.}$).

A laboratory test of the mud showed an API water loss of 25 ml/30 min. The cumulative loss is proportional to the square root of time. Assume therefore that the accumulative fluid loss V_f is expressed as:

$$V_f = A \cdot \sqrt{\frac{k \cdot \Delta p}{\mu}} \cdot \sqrt{t} = A \cdot C \cdot \sqrt{t}$$

We assume the parameters C is constant.

- To simplify the fluid loss estimation imagine that the time of drilling the well is negligible. Construct a plot of filtration loss vs. time. Estimate the fluid loss after 24 hours.
- Calculate the radius of the invaded zone after 24 hours, assuming 100 % displacement of the pore fluid.
- We want to minimize the fluid loss to porous formation during overbalanced drilling, both with OBM and WBM.
 - How would you specify the drilling fluid (focus on the part related to filtrate loss)?
 - How would you follow up filtration control during the drilling phase?
 - Why is filtration control important?
 - The filtration of the mud (tested in the filter press) showed an increasing tendency during drilling. Why?

5.3 CUTTINGS CONCENTRATION I

A horizontal section has been drilled at more or less constant ROP and flow rate. The cuttings concentration generated at the bit during drilling is $c_1 = 0.02$. Discuss what could be the concentration at these positions:

- At the end of the horizontal section ($= c_2$)
- At the surface, when the mud is entering the return flow line ($= c_3$)
- What determines the cuttings bed height in the horizontal section?
- Why is cuttings accumulation in wellbore expansions (washouts) a problem during tripping?
- Mention 5 downhole problems related to poor solids control during drilling, and explain why or how poor solids control is the cause behind the problems.

5.4 CUTTINGS CONCENTRATION II

a) What forces and mechanisms are involved when cuttings are transported in horizontal wellbores?

b) Slip velocity of perfect spheres is:

$$V_{\text{settling}} = \frac{d^2_{\text{cutting}} \cdot g (\rho_{\text{cutting}} - \rho_{\text{mud}})}{6\pi\mu} f(c)$$

What is the meaning of $f(c)$ in the given equation? Present a graphical representation of $f(c)$ vs. particle concentration.

c) Figure out which height the cuttings bed will assume, and mention which forces are involved in cutting transportat in high-deviated wellbores.

d) Cleaning of horizontal wells is a challenge. Your task is to:

- Explain the principles of how cleaning works and which processes and parameters are involved.
- Why does the string-RPM need to be > 120 RPM before the cleaning process become really efficient?

5.5 DENSITY CONTROL

a) Define a weighted mud system (as opposed to un-weighted)? Explain how to clean weighted muds.

b) Derive a simple formula of necessary volume increase, ΔV_{add} , involving weight material with density ρ_{add} (4.3 kg/l) to increase the density from ρ_1 to ρ_2 . Use this formula to estimate how much mass (in kg) of barite must be added to increase mud density from 1.3 to 1.4 kg/l. Original mud volume was 60 m^3 .

c) 1.0 m^3 of mud has a density of 1.5 kg/l. Adjust the mud density to 1.72 by adding 100 l mud of density 1.8, 40 kg Bentonite (to adjust rheology) of density 2.3 kg/l and Barite of density 4.3 kg/l. Find how much Barite is needed to obtain a mud density of 1.72 kg/l. All ingrediences are added together simultaneously.

d) Different water based muds, defined below in terms of volume and density, are stored in three different mud pits. All 3 pits should be mixed into one tank and additional water added until the density becomes 1.55. How much volume of water must be added?

$$V_1 = 10 \text{ m}^3, \rho_1 = 1.5 \text{ kg/l}$$

$$V_2 = 20 \text{ m}^3, \rho_2 = 1.6 \text{ kg/l}$$

$$V_3 = 3 \text{ m}^3, \rho_3 = 1.9 \text{ kg/l}$$

5.6 DENSITY CONTROL

Sometimes the mud viscosity increases unintentionally due to accumulation of fines (inert solids) in the mud. These fines are referred to as Low Gravity Solids Content (LGSC). The fines are too fine to be removed by the cleaning equipment. Typical density of LGS is 2.4 kg/l. They are inert, but builds viscosity since particle size is small ($< 5 \mu$). Their unwanted effect can be reduced by diluting the mud with water. Here follows 3 problems:

- The mud volume is 100 m^3 with a density 1.8 kg/l. The fraction of low gravity solids is too high, 5 weight %, and has to be decreased to 3 % by water dilution. Calculate the mud volume to be discarded and the amounts of fresh water and Barite to be added. The original volume and density has to be unchanged.
- A tank containing 90 m^3 of mud has a density of 1.6 kg/l and should be increased to 1.7 kg/l. The volume fraction of low-gravity solids must also be reduced from 0.055 to 0.030 by water dilution. It is required that you first discard a part of the original mud volume, so that after adding of water, the volume of the mud is 90 m^3 before the Barite is added. How much Barite must be added, and, what exactly is the new LGSC?



The advertisement for e-learning for kids features a central image of a smiling teacher assisting two young students with a laptop. To the right, two circular insets show children engaged in learning activities: one with a girl and a boy looking at a book, and another with a group of children working on computers. The background is a vibrant yellow with orange and white abstract shapes. The e-learning for kids logo is in the top left corner. A green oval on the right contains three bullet points: 'The number 1 MOOC for Primary Education', 'Free Digital Learning for Children 5-12', and '15 Million Children Reached'. At the bottom, a text block provides details about the foundation's mission and contact information.

About e-Learning for Kids Established in 2004, e-Learning for Kids is a global nonprofit foundation dedicated to fun and free learning on the Internet for children ages 5 - 12 with courses in math, science, language arts, computers, health and environmental skills. Since 2005, more than 15 million children in over 190 countries have benefitted from eLessons provided by EFK! An all-volunteer staff consists of education and e-learning experts and business professionals from around the world committed to making difference. eLearning for Kids is actively seeking funding, volunteers, sponsors and courseware developers; get involved! For more information, please visit www.e-learningforkids.org.

- c) Calculate the volumes of old mud ($< 10 \text{ m}^3$) and Barite that has to be mixed in order to fill a 10 m^3 large pit with mud to balance a pore pressure of 410 bar in a depth of 3000 m. Barite has a density of 4.3 kg/l. The density of the old mud is 1.2 kg/l.

5.7 ECD. BARITE

Explain the reasons behind and suggest potential solution to the following problem:

This well was drilled with WBM, weighted by Barite to 15 PPG. While POOH to change the 12 1/4" bit, the driller experienced no problems. When GIH with the new bit some weight reductions (took weight) were experienced in the wellbore's build-up zone. It took around 5 h from the bit left the bottom of the well till it returned. After the bit reached the bottom, the well was circulated for some time, and the returning mud behaved strangely. The mud weight, which originally was 15 PPG displayed an initial sharp decrease, then increased again as shown in Figure 5-7, before finally stabilizing at 15 PPG.

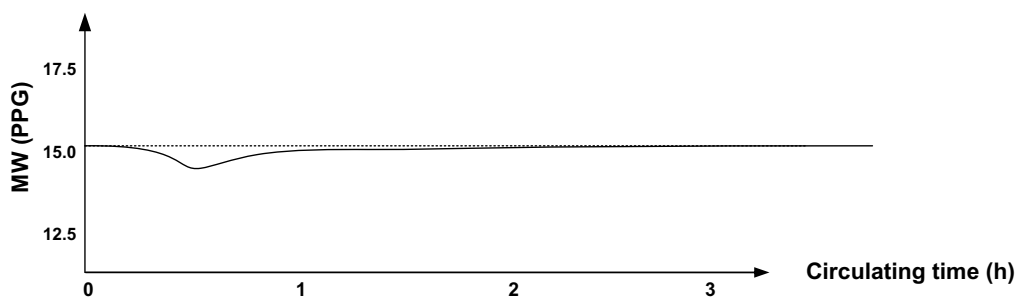


Figure 5-7: Density of returning mud after tripping.

5.8 ECD. FLUID AND FLOW

A 17 1/2" hole was drilled from the 20" casing shoe at 1100 mTVD to 2100 mTVD. The bottom hole assembly consisted of 120 m of 9 1/2" Drill Collars (DC). A 5 1/2" drillpipe (DP) was used.

Capacities:

- 17 1/2" open hole capacity: 155.2 l/m
- DC / Open hole capacity: 109.4 l/m
- DP Open hole capacity: 139.2 l/m
- DP / Casing capacity: 161.8 l/m
- 9 1/2" DC / capacity: 4.56 l/m
- 5 1/2" DP capacity: 10.77 l/m

Mud Parameters:

- Mud density: 1.25 kg/l
- Rheology: 600 / 300 rpm: 51.7 / 30.6 Pa
 200 / 100 rpm: 22 / 12 Pa
 6 / 3 rpm: 3 / 4 Pa
 Gel: 10 s / 10 min: 5 / 13 Pa

- a) Prior to drilling, the hole was circulated at 3 500 l/min. What is the annular pressure loss, and what is the corresponding ECD?
- b) The drilling commenced from 2 100 m. The same rheology and flow rate was applied as before. At 2 300 m the average drilling rate was 50 m/hr. Formation bulk density was 2.4 kg/l. What is the ECD in this situation? Transport ratio is 0.75. At the casing shoe at 1 800 m TVD the formation fracture pressure was 228 bar. Check if everything is OK.
- c) A new mud was being prepared for the 8 ½" section. The 13 3/8" csg shoe was located at 15 000 ft vertical depth. While drilling at 16 500 ft the well started losing mud and it was decided to lower the MW from 15 to 14 PPG. The well had a very narrow pressure window, and the equivalent pore pressure gradient at this depth was 13.5 PPG. The mud was mixed to 14 PPG with an effective viscosity of 40 and 30 cP at 600 and 300 RPM respectively, at an average surface mud temperature of 40 °C. After the new mud was circulated, the pump was shut off, and a flow-check indicated that the well was dead (no influx). While repairing the power swivel the well started to flow by itself, and soon afterwards the kicking well had to be shut in to avoid a complete unloading.
 How would you go about to estimate the pressure profile of an initially cold, static fluid column, as a function of time. You are asked to present the governing equations of heat transfer in a well on differential form, and work out a flow sheet of how to numerically solve this task.

5.9 WATER ACTIVITY

- a) Define water activity, A_w and how to determine A_w either as; a) salt water solutions or taken from; b) pore water in shale?
- b) Explain why water activity is a function of water salinity?
- c) Explain why high water activity causes clay swelling problems?
- d) How do you prevent clay swelling problem?
- e) How does water activity of the water phase in OBM influence wellbore stability?

5.10 SHALE STABILITY

In order to avoid water entering and causing shale to swell, the activity of the water in the mud (including the water phase in oil based mud) and in the shale must be equal.

The activity of the water in the water phase in shale cuttings is measured in the field using an electro hygrometer. The probe of the electro hygrometer is placed in the vapor above the sample being tested. The electrical resistance of the probe is sensitive to the amount of water vapor present. Since the test always is conducted at atmospheric pressure, the water vapor pressure is directly proportional to the volume fraction of water in the air/water vapor mixture. The instrument is normally calibrated with saturated solutions of known activity shown in Table 5-10.

Salt	Activity
ZnCl ₂	0.10
CaCl ₂	0.30
MgCl ₂	0.33
Ca(NO ₃) ₂	0.51
NaCl	0.75
(NH ₄) ₂ SO ₄	0.80
Pure water	1.00

Table 5-10 Saturated brines of different salts and its vapor's water activity.

Sodium chloride and calcium chloride are the salts mostly used to alter the activity of the water in the mud. Calcium chloride is quite soluble, allowing the activity to be varied over a wide range. In addition, it is relatively inexpensive. The resulting water activity for various concentrations of NaCl and CaCl₂ are shown in Fig. 5-10.

- a) The activity of a sample of shale cuttings drilled with OBM (no foreign fluid invasion) is determined to be 0.69 by an electro hygrometer. Determine the concentration of calcium chloride needed in the water phase of the mud in order to have the activity of the mud equal to the activity of the shale.

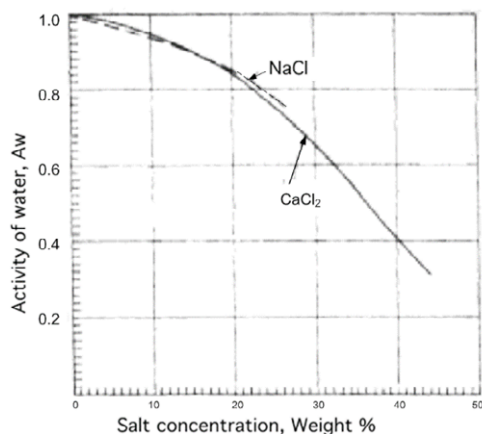


Figure 5-10: Water activity in calcium chloride and sodium chloride at room temperature.

- b) A core is taken from a swelling formation. Can you retrieve any useful information from its specific weight, useful with respect to avoid swelling while drilling through it?
- c) Explain why wellbores and cuttings stability is so much better when applying OBM as compared to WBM. As part of the answer, please explain the principal function of the two different types of surface active additives that are always added to Oil based mud.

.....Alcatel-Lucent 

www.alcatel-lucent.com/careers

What if you could build your future and create the future?

One generation's transformation is the next's status quo. In the near future, people may soon think it's strange that devices ever had to be "plugged in." To obtain that status, there needs to be "The Shift".

5.11 SHALE STABILITY

- a) When drilling into swelling clay, problems like sloughing shale and stuck pipe may occur. Explain how/why this can be avoided by means of the proper oil based drilling fluid and specify the ingredients in the drilling fluid.
- b) Why is KOH preferred over NaOH?
- c) What significance does the K^+ concentration have for the shale?
- d) Can water flow through shale be hindered?
- e) How is the salt concentration in the water phase in Oil Based Mud determined?

While drilling in the 8 ½ " section, at a depth of 1 500 mTVD / 6 000 mMD, in overbalance, the ECD will fluctuate and at times be high in this long well. Previous experience from that area indicates that instable, swellable shale will be penetrated. Your task now is the following:

- f) Define what wellbore stability-related processes may take place in the shale while drilling through it with WBM.
- g) Which type of inhibitive mud will you suggest in order to maximize wellbore stability? Explain how this mud type will affect the wellbore.
- h) Does fluctuating ECD have any implications for the stability of the wellbore?

5.12 WELLBORE PROBLEM

- a) What are the dominating mechanisms or factors leading to mechanically stuck pipe. Explain the mechanisms of differential sticking in porous/permeable formation.
- b) What are the consequences of stuck pipe and how do you suggest combating the problem?
- c) What is the most likely stuck pipe mechanism while drilling in salt formations? In the case of presence of halite type salts, what type of mud would you select for safe drilling in such salt sections.
- d) Wellbore breathing (ballooning) and seepage losses: Include the headings; Definition, Explanation, Detections, Repair activity. Discuss the phenomenon Ballooning.

6 SUPPORTIVE INFORMATION

6.1 PUMP (NATIONAL 12-P-160) AND HYDRAULIC PROGRAM DATA

Line size	in	5 ½	5 ¾	6	6 ¼	6 ½	6 ¾	7	7 ½
Discharge pressure	Psi 10 ⁵ ·Pa	5555 383.0	5085 350.6	4670 322.0	4305 296.8	3980 274.4	3690 254.4	3430 236.5	3200 220.2
Pump rated at 120 spm	GPM m ³ /s	444 0.0280	486 0.0307	529 .0334	574 .0362	621 .0392	669 .0422	720 .0454	772 .0482
HP		1439.0	1441.8	1441.3	1441.7	1442.0	1440.3	1440.8	1441

Power of Efficiency = $1441.7 \cdot 745.7 = 1.0748 \cdot 10^6$ or $322 \cdot 10^5 \cdot 0.0334 = 1.0755 \cdot 10^6$ (watt)

$$ROP_{q/d_n} = C \cdot (q/d_n)^{a_8}$$

$$ROP_{BHHP} = C \cdot (BHHP)^{a_8} \quad BHHP = \Delta p_{bit} \cdot q$$

$$P_p = q \cdot p_p \text{ (Power)}$$



Maastricht University *Leading in Learning!*

**Join the best at
the Maastricht University
School of Business and
Economics!**

Top master's programmes

- 33rd place Financial Times worldwide ranking: MSc International Business
- 1st place: MSc International Business
- 1st place: MSc Financial Economics
- 2nd place: MSc Management of Learning
- 2nd place: MSc Economics
- 2nd place: MSc Econometrics and Operations Research
- 2nd place: MSc Global Supply Chain Management and Change

Sources: Keuzegids Master ranking 2013; Elsevier 'Beste Studies' ranking 2012; Financial Times Global Masters in Management ranking 2012

**Maastricht University is
the best specialist
university in the
Netherlands
(Elsevier)**

Visit us and find out why we are the best!
Master's Open Day: 22 February 2014

www.mastersopenday.nl



$$p_p = \Delta p_{bit} + \Delta p_d$$

$$\Delta p_d = K_1 \cdot D \cdot q^m$$

$$p_{bit} = 1.11 \frac{1}{2} \rho v^2$$

$$q_{opt_{I-q/d_n}} = \left(\frac{2p_p}{(m+2)K_1 D} \right)^{\frac{1}{m}}$$

$$q_{opt_{II-q/d_n}} = \left[\frac{(E_p)_{\max}}{K_1 \cdot D(m+2)} \right]^{\frac{1}{m+1}}$$

6.2 PRESSURE LOSS EQUATIONS

	Newtonian fluid	Bingham model	Power law model
Lam/ pipe	$\Delta p_p = \frac{32 \bar{v} \mu L}{d^2}$	$\Delta p_p = \frac{32 \mu_{pl} \cdot L \cdot \bar{v}}{d^2} + \frac{16 L \tau_o}{3d}$	$\Delta p_p = 4K \left(\frac{8\bar{v}}{d} \cdot \frac{3n+1}{4n} \right)^n \cdot \frac{L}{d}$
Lam/ annulus	$\Delta p_a = \frac{48 \bar{v} \mu L}{(d_o - d_i)^2}$	$\Delta p_a = \frac{48 \mu_{pl} \cdot L \cdot \bar{v}}{(d_o - d_i)^2} + \frac{6 L \tau_o}{d_o - d_i}$	$\Delta p_a = 4K \left(\frac{12\bar{v}}{d_o - d_i} \cdot \frac{2n+1}{3n} \right)^n \cdot \frac{L}{d_o - d_i}$
Turb/ pipe/ ann	$\Delta p = \frac{0.092 \rho_m^{0.8} \bar{v}^{1.8} \mu^{0.2} L}{d_h^{1.2}}$	$\Delta p = \frac{0.073 \rho_m^{0.8} \cdot \bar{v}^{1.8} \cdot \mu_{pl}^{0.2} \cdot L}{d_h^{1.2}}$	$\Delta p = a \cdot N_{Re}^{-b} \cdot \frac{4L}{d_h} \cdot \frac{1}{2} \rho \bar{v}^2$ $a = (\log n + 3.93)/50$ $b = (1.75 - \log n)/7$
Eff. visc. pipe	$\mu_{eff} = \tau/\gamma$	$\mu_{eff} = \mu_{pl} + \frac{\tau_o d}{6\bar{v}}$	$\mu_{eff} = \left(\frac{8\bar{v}}{d} \cdot \frac{3n+1}{4n} \right)^n \cdot \frac{Kd}{8\bar{v}}$
Eff. visc. ann	$\mu_{eff} = \tau/\gamma$	$\mu_{eff} = \mu_{pl} + \frac{\tau_o (d_o - d_i)}{8\bar{v}}$	$\mu_{eff} = \left(\frac{12\bar{v}}{d_h} \cdot \frac{2n+1}{3n} \right)^n \cdot \frac{Kd_h}{12\bar{v}}$
Shear-r. pipe	$\dot{\gamma} = \frac{8\bar{v}}{d}$	$\dot{\gamma} = \frac{8\bar{v}}{d} + \frac{\tau_o}{3\mu_{pl}}$	$\dot{\gamma} = \left(\frac{8\bar{v}}{d} \cdot \frac{3n+1}{4n} \right)$
Shear-r. ann.	$\dot{\gamma} = \frac{12\bar{v}}{d_o - d_i}$	$\dot{\gamma} = \frac{12\bar{v}}{d_o - d_i} + \frac{\tau_o}{2\mu_{pl}}$	$\dot{\gamma} = \left(\frac{12\bar{v}}{d_o - d_i} \cdot \frac{2n+1}{3n} \right)$
General $N_{re,pipe}$	$N_{Re} = \frac{d^n \cdot \bar{v}^{2-n} \cdot \rho}{K_p \cdot (8^{n-1})}$	$K_p = K \cdot \left(\frac{3n+1}{4n} \right)^n$	Fanning $f_{lam} = 16/N_{re}$
General $N_{re,ann}$	$N_{Re} = \frac{d^n \cdot \bar{v}^{2-n} \cdot \rho}{K_a \cdot (12^{n-1})}$	$K_a = K \cdot \left(\frac{2n+1}{3n} \right)^n$	Fanning $f_{lam} = 24/N_{re}$

Continuity equation: $-\frac{\partial \rho}{\partial t} = \nabla \cdot (\rho \mathbf{v})$

Microscopic Cylindrical coordinates $-\frac{\partial \rho}{\partial t} = \frac{1}{r} \frac{\partial}{\partial r} (\rho r v_r) + \frac{1}{r} \frac{\partial}{\partial \theta} (\rho v_\theta) + \frac{\partial}{\partial z} (\rho w)$

Macroscopic $\frac{d \int v \rho dV}{dt} = -\Delta \rho \bar{v} A = \rho_1 \bar{v}_1 A_1 - \rho_2 \bar{v}_2 A_2$

Momentum equation $\rho \frac{D\mathbf{v}}{Dt} = \rho \mathbf{g} - \nabla p - \nabla \cdot \boldsymbol{\tau}$

Microscopic Cylindrical coordinates (only the r-component)

$$\rho \left(\frac{\partial v_z}{\partial t} + v_z \frac{\partial v_r}{\partial r} + \frac{v_\theta}{r} \frac{\partial v_z}{\partial \theta} + v_z \frac{\partial v_z}{\partial z} \right) = -\frac{\partial p}{\partial z} + \mu \left[\frac{\partial}{\partial r} \left(\frac{1}{r} \frac{\partial}{\partial r} (r v_z) \right) + \frac{1}{r^2} \frac{\partial^2 v_z}{\partial \theta^2} + \frac{\partial^2 v_z}{\partial z^2} \right] + \rho g_z$$

Macroscopic $\frac{d}{dt} \int \rho dV = \rho_1 \bar{v}_1^2 A_1 - \rho_2 \bar{v}_2^2 A_2 + p_1 A_1 - p_2 A_2 - F + Mg$

The steady state, one dimensional pipe flow form is: $p_1 A_1 - p_2 A_2 - F = Mg \sin \theta$.

Energy equation

Macroscopic $\left(\frac{p}{\gamma} + \frac{\bar{v}^2}{2g} + z \right)_{in} + h_{pump} = \left(\frac{p}{\gamma} + \frac{\bar{v}^2}{2g} + z \right)_{out} + h_{friction}$

6.3 CONVERSION FACTORS AND FORMULAS:

1 Hp:	745.7 W
Shear stress:	$\tau_{OFU} = \Theta \cdot 1.067$ (Fann VG readings = Θ)
Shear stress:	1 lb/100ft ² (OFU) = 0.4788 Pa (SI)
τ_{SI} :	$\tau_{OFU} \cdot 0.4788$
Shear rate:	$\dot{\gamma} (s^{-1}) = RPM \cdot 1.703$
1 inch:	0.0254 m
1 bar:	10 ⁵ Pa
1cP:	10 ⁻³ Pas
P (effect):	q · p (Watt)
A_{sphere} :	4 · πr ²
V_{sphere} :	4/3 · πr ³

SOLUTIONS TO EXERCISES IN DRILLING FLUID ENGINEERING

Content:

1. Fluid Properties
2. Rheological models
3. Drilling fluid dynamics
4. Bit hydraulics
5. Wellbore challenges



The logo for BI Norwegian Business School features a central blue square with the letters 'BI' in white. Radiating from this center are numerous colorful, 3D bar-like shapes in various colors (red, orange, yellow, green, blue, purple, pink, etc.). Each shape has a label for a business program: 'Business', 'Strategic Marketing Management', 'International Business', 'Leadership & Organisational Psychology', 'Shipping Management', 'Financial Economics', and 'Business'.

Empowering People. Improving Business.

BI Norwegian Business School is one of Europe's largest business schools welcoming more than 20,000 students. Our programmes provide a stimulating and multi-cultural learning environment with an international outlook ultimately providing students with professional skills to meet the increasing needs of businesses.

BI offers four different two-year, full-time Master of Science (MSc) programmes that are taught entirely in English and have been designed to provide professional skills to meet the increasing need of businesses. The MSc programmes provide a stimulating and multi-cultural learning environment to give you the best platform to launch into your career.

- MSc in Business
- MSc in Financial Economics
- MSc in Strategic Marketing Management
- MSc in Leadership and Organisational Psychology

BI NORWEGIAN BUSINESS SCHOOL

EFMD
EQUIS
ACCREDITED

www.bi.edu/master

1 FLUID PROPERTIES - SOLUTIONS

1.1 RHEOLOGY CONTROL - SOLUTION

- a) The mean size of Barite is typically 20 μm . The particles will be uniformly dispersed in the drilling fluid and they will lead to increased viscosity. PV and μ_{eff} will increase. YP will be unaffected or decrease, since the smallest Barite particles will behave as physical dispersants.
- b) In order to:
- Suppress Ca^{++} from dissolving.
 - Keep anionic colloidal particles dispersed.
 - Suppress corrosion, H_2S - and CO_2 - attack.
- c) Polymers are polymerized monomers. They can be of organic origin or be manufactured synthetically. Polymers have high molecular weight and come mostly as charged particles $\rightarrow$ they will bind water molecules $\rightarrow$ increase the hydrodynamic volume $\rightarrow$ influence viscosity and filter behaviour. Some types of polymers can attract or bind charged particles (clay), and therefore influence the swelling process and contribute to selective flocculation (clear water drilling). The purpose of polymers are mainly to:
- increase fluid viscosity
 - reduce fluid viscosity in turbulent flow (drag reducer)
 - control flocculation
 - improve both the filter cake itself and the fluid loss through it
- d) The description of the three expressions are:
- Pseudo plastic fluids exhibit altered apparent viscosity whenever the shear rate is changed.
 - The fluid displays a reduction in viscosity over time at constant shear rate as indicated in Figure 1-1.
 - Rheopectic fluids are rare. They exhibit increased shear stress at increasing shear time (at constant shear rate).

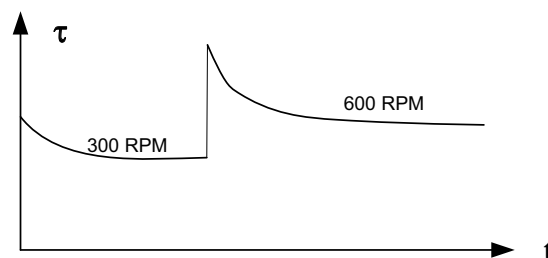


Figure 1-1: Behavior of thixotropic fluids after stillstand (left) and at constant shear rates.

- e) Clay particles have a static, negative surface charge localized on the particle edges, but with weakly positively sites on the surface of the platelets. This triggers water! When studying the repulsive - attractive forces, it is experienced that at low salt concentration or high colloidal concentration, a very slow flocculation will take place. When edges come sufficiently close to the surfaces of other Montmorillonite particles, they join.

1.2 RHEOLOGY CONTROL - SOLUTION

- a) Bentonite particles attract water molecules (dipoles) in multiple of layers onto each of its charged surface. Swelled Na-Bentonite sheets separate readily when exposed to shear forces. Salt will reduce the charges on the Bentonite surfaces. In addition the salt (ions) will bind much of the bulk water (reduce the water activity).
- b) At still-stand many layers of water molecules are attached to the Bentonite surface, and particles flocculate slowly → viscosity increases. When the dispersion is stirred or pumped, the resulting shear stress will remove the outer, weakly attached water layers. Additionally, they will break up the flocks. Dispersed Bentonite with many free water molecules, torn off due to high shear stress, has lower viscosity than at stillstand.
- c) Drilling in sediments of high yield (premium) clay produces the following clay concentration: Fraction of solids by weight = f

$$f = \frac{q_{clay} \cdot \rho_{clay}}{q_{pump} \cdot \rho_{mud}} = \frac{ROP \cdot A_{bit} \cdot \rho_{clay}}{q_{pump} \cdot \rho_{mud}} = \frac{0.0097 \cdot 0.34 \cdot 2400}{0.05 \cdot 1025} = 0.154$$

$$ROP = 35 \text{ m/t} = 35 / (60 \cdot 60) = 0.0097 \text{ m/s}$$

$$q_{pump} = 3000 \text{ l/min} = 3000 / (1000 \cdot 60) = 0.05 \text{ m}^3/\text{s}$$

$$A_{bit} = \pi/4 \cdot (d_{bit})^2 = \pi/4 \cdot 0.662^2 = 0.34 \text{ m}^2$$

$$d_{bit} = 26'' = 26 \cdot 0.0254 = 0.662 \text{ m}$$

Drilled clay contributes to a weight increase of 15.4 % and produces a viscosity of 42 cP, which is above the required viscosity of 15cP.

- d) The yield of Bentonite is defined by how many m^3 of mud at 15 cP that the amount of one ton Bentonite is able to produce. From Figure 1-6 one ton of Bentonite will produce 6 weight % = 16.666 m^3 of 15 cP mud.
- e) From Figure 1-6 we see that a viscosity of max. 50 cP will correspond to 7.5 w % of Bentonite.

$$\rho_{bentonite} = 2400 \text{ kg/m}^3$$

To find the density of the mixture of 100 kg mud $\Rightarrow$ 7.5 kg Bentonite + 92.5 kg water, we need to find the volume:

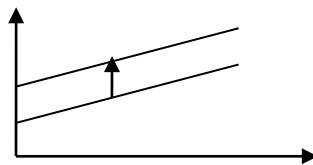
$$Volume = V_{bentonite} + V_{water} = \frac{7.5 \text{ kg}}{2400 \text{ kg/m}^3} + \frac{92.5 \text{ kg}}{1000 \text{ kg/m}^3} = 0.0955 \text{ m}^3$$

$$\rho_{mud} = \frac{m}{V} = \frac{100 \text{ kg}}{0.0955 \text{ m}^3} = 1047 \text{ kg/m}^3$$

This shows that mud density cannot be increased much higher than 1047 kg/m^3 by the addition of Bentonite.

1.3 FLOCCULATION - SOLUTION

- a) When two Bentonite flakes are sufficiently near each other they are electrostatically attracted and will join edge to surface.
- b) The cement is not by far hardened and contains a high concentration of lime (CaOH). Lime dissociates and one Ca^{++} ion can crosslink two charged clay platelets. This binding cannot be broken by hydraulic means (shear stress), and the flocculated mud has to be dumped after having been circulated to the surface.
- c) The factors which enhance flocculation:
 - High concentration of charged colloids (Bentonite or anionic polymer)
 - High concentration of Ca^{++} ions (from dissolved salt and carbonates)
 - High Temperature (Brownian movements of the water molecules contribute to bringing the colloidal particles more frequently in contact with each other)



Need help with your dissertation?

Get in-depth feedback & advice from experts in your topic area. Find out what you can do to improve the quality of your dissertation!

Get Help Now



Go to www.helpmyassignment.co.uk for more info



- d) WBM behaves shear thinning:
- Amount of water dipoles attached to each charged colloidal is a function of the shear force. High flow rate $\rightarrow$ high shear rate $\rightarrow$ water molecules are sheared off and become free $\rightarrow$ lower viscosity of the suspension
 - Weak flocculation occurs, especially at low shear stress. At high shear stress the flocks break up $\rightarrow$ lower yield point
- e) The shearing action explained in d) above also is **time dependent**. Layer by layer are sheared off in consecutive order.
- f) The surface of clay colloids are positively charged by the loosely bonded Na-ions and represents therefore a weak bond compared to the electrostatic bond of double valence cations, mainly Ca^{++} , and to the strongly negative charged colloids at their edges.

1.4 MUD CONTAMINATION - SOLUTION

- a) Contaminations are dissolved salt and chalk; drilled-through cement etc. all produce Ca^{++} ions which lead to flocculation. Also fines are acting as pollutants. At the surface (on the rig) the mud can be treated with thinners. Low gravity (2.4 kg/l) solids content (LGSC) is reduced by running the mud through centrifuges.
- b) Rheology monitoring. First we plot the evolution of the rheology vs. time, as shown in Figure 1-4a.

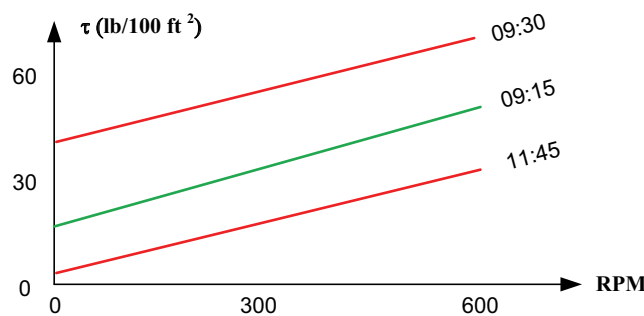


Figure 1-4a: The rheology of the mud at 3 time points

Then to evaluate the mentioned changes of the Bingham field rheology-model the plot is perfect. We estimate the Bingham constants:

$$\begin{aligned}
 \mu_{pl} &= 42 - 28 = 14 \text{ cP} \\
 &= 41 - 27 = 14 \text{ cP} \\
 &= 68 - 54 = 14 \text{ cP} \\
 &= 31 - 17 = 14 \text{ cP}
 \end{aligned}$$

We observe that the mud is dispersed at first. Salt will dissolve and Ca^{++} contaminates the mud. We now see that the viscosity is constant, while the yield point (YP) has changed like this:

$$\begin{aligned} \text{YP} &= 28 - 14 &= 14 \\ &= 27 - 14 &= 13 \\ &= 54 - 14 &= 40 \\ &= 17 - 14 &= 3 \end{aligned}$$

The PV is constant (constant inner friction means solids content is constant). Δ YP is caused by higher attractive forces, caused by drilling into a salty formation. Initially, low concentration of Ca^{++} ions leads to strong cross binding (flocculation). Later, when the Ca^{++} concentration has been high for a while the Ca^{++} ions have exchanged the Na^{+} -ions in the Bentonite plates, leading to aggregation of clay platelets. A high concentration of Ca ions will over time lead to lower shear stress than originally due to cation exchange. The development is seen in Figure 1-4b.

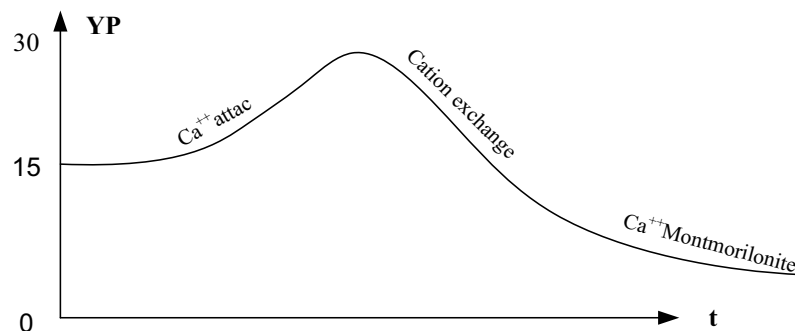


Figure 1-4b: Shear stress vs. time after encountering high concentration of contaminants.

Countermeasures: Add dispersants (or use Gyp mud) or use a high pH level in the mud when contaminations are expected. This is how to avoid flocculation and aggregation.

- c) The edge-to-face flocculation is caused by weak electrostatic forces and is easily broken when sheared. The Ca^{++} ion binds two clay platelets in a much stronger grip, and is not easily broken as indicated in Figure 1-4c.

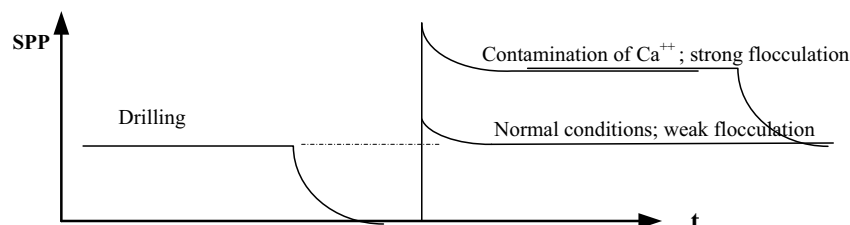


Figure 1-4c: Rheological response at the rig floor when drilling into contaminants.

1.5 FLOCCULATION - SOLUTION

- a) Consider the force balance between shear and gravity acting on a particle:

$$A_p \cdot \tau_y = m_p \cdot g = V_p \cdot (\rho_p - \rho_{fl}) g$$

$$4 \pi d_p^2 \cdot \tau_y = \frac{1}{6} \pi d_p^3 (\rho_p - \rho_{fl}) g$$

Solve for yield point:

$$\tau_y = \frac{d_p}{24} (\rho_p - \rho_{fl}) g = \frac{0.005}{24} (2\,300 - 1\,100) 9.81 = 2.45 \text{ Pa}$$

Now solve the same balance of force while particles are settling, with respect to particle diameter:

$$d_p = \tau_y \cdot 24 / [(\rho_p - \rho_{fl}) g] = 15 \text{ Pa} \cdot 24 / [(2\,300 - 1\,100) \cdot g] = 0.0304 = 30.4 \text{ mm}$$

- b) The gel structure inside the drill string could have broken either by just pumping, by hitting the pipe with a hammer, or by inserting a heavy pill in the upper part of the drill string (U-tube the level in the drill string downwards). Consider the force balance between shear force and gravity acting on the fluid column inside the pipe:

$$A_{\text{fluid}} \cdot \tau_y = \rho g \cdot \Delta h$$

$$\pi d_{\text{pipe}} \cdot L \cdot \tau_y = \rho g \cdot \Delta h$$

Solve for Δh , the additional hoisting height before gravity breaks the gel:

$$\Delta h = \pi \cdot d_{\text{pipe}} \cdot L \cdot \frac{\tau_y}{\rho \cdot g} = \pi \cdot 4.127 \cdot 0.0254 \cdot 2\,100 \cdot 14.4 / (1\,100 \cdot 9.81) = 0.3 \text{ m}$$



Brain power

By 2020, wind could provide one-tenth of our planet's electricity needs. Already today, SKF's innovative know-how is crucial to running a large proportion of the world's wind turbines.

Up to 25 % of the generating costs relate to maintenance. These can be reduced dramatically thanks to our systems for on-line condition monitoring and automatic lubrication. We help make it more economical to create cleaner, cheaper energy out of thin air.

By sharing our experience, expertise, and creativity, industries can boost performance beyond expectations.

Therefore we need the best employees who can meet this challenge!

The Power of Knowledge Engineering

Plug into The Power of Knowledge Engineering.
Visit us at www.skf.com/knowledge

SKF

1.6 FLUID ADDITIVES - SOLUTION

a)

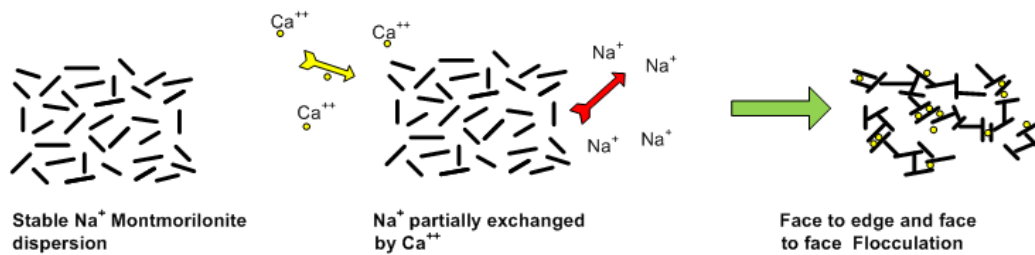
Material	Definition	Relevance
Anhydrite	CaSO_4 = sedimentary salt	Dissolves in water $\rightarrow \text{Ca}^{++}$
caustic soda	NaOH , Sodium hydroxide = lye	Adjust pH (dispersant)
Ca SO_4	Anhydrite	Contaminator, leads to flocculation
Gypsum	$\text{Ca SO}_4 \cdot \text{H}_2\text{O}$ Sedimentary salt	Restructure from Na- to Ca-Bentonite; shale control
CEC	Cation Exchange Capacity	Ability of reactive clay to exchange cations
CMC	Natural polymer	Filter loss/viscosifiers
Chalk	CaCO_3 = sedimentary salt	Dissolves in water $\rightarrow \text{Ca}^{++}$
Colloid	Particles of size $< 2 \mu$, clay, silt	Build viscosity
Deflocculator	Dispersion of colloids	Reduce/neutralize electrostatic attraction
Dispergator	Spreading of colloids	Thinner
HEC	Aatural polymer	Viscosifyer, filtrate reducer, deflocculant
Lignite	Anionic polymer	Thinner, filtrate reducer
Lignosulphonate	Anionic polymer	Thinner (dispergator)
Dispergator	Thinner	Hinder particles to coalesce
MBT	Methylene Blue Test	Determines amount of reactive clay in mud. Clays present in the mud will adsorb MB
PAC	Natural polymer	Filter reducer, shale control
PHPA	Synthetic polymer	Shale control, Bentonite extender
Prehydrated	Bentonite hydrated in water	
Salt	Ionic compound, NaCl	Dissolves in water $\rightarrow \text{Na}^+$
SAPP	Anionic polymer	Thinner (dispergator)
Starch	----- " -----	----- " -----
Xanthan	Natural polymer	Viscosifyer

- b) A drag reducer consists of long-chained, neutral polymers added in small amounts to the viscous fluid. In a turbulent flow regime, the fluid molecules move in a random manner, causing much of the energy applied to them to be wasted as eddy currents (and corresponding high pressure loss). Due to shear stress the polymers are stretched out where the shear is high (close to the wall). In out-stretched state the diffusion is higher due to the polymer's lower effective surface area and thus lower resistance to movements. The polymers diffuse more in the direction of the pipe centre since the wall hinders diffusion in the opposite direction (no polymers are coming from the wall). The concentration will therefore become low after some flowing distance. The small concentration of stretched long polymers along the wall will tend to turn the turbulent flow into laminar or streamlined flow.
- c) The higher concentration, the more K^+ is exchanged with Na^+ shale, the less shale swelling is seen. K^+ is geometrically suitable and leads to high platelet attraction.
- d) Figure 1-6 shows both how a Ca-attack is changing the dispersed mud, but also how Gyp mud is made. Bentonite is composed mainly of the mineral called Montmorillonite. It is an aluminium silicate in which the silicon-oxygen sandwich is a layer of aluminium hydroxide. Some of the aluminium in the lattice structure is, during creation, replaced by ions of a lower charge (lower electron valence) such as magnesium (from 3 to 2). The *substitution*, without any other change of structure, creates negative surface charges in the lattice.

The negative charge sites created in the clay sheet are partly balanced by close association of positively charged ions (cation), normally Na^+ . The creation of these charged ions and charged clay surfaces creates very strong attractive forces for polar water molecules that readily force themselves in between the unit layers.

Gypsum is added to prevent shale swelling (at least in the old days). When lime or gypsum is added to Bentonite-treated mud, sodium Montmorillonite will convert to calcium Montmorillonite, which first produces flocculation and eventually aggregation of the Montmorillonite (see Figure 1-4b above). Caustic soda is added for pH control to suppress further dissolution of Ca^{++} . Lignosulphate is added for deflocculating. CMC may be added for fluid control. Then we get Gyp mud.

If a lot of swellable clays have to be drilled through, apply gypsum mud; Pre-hydrate Na^+ - Bentonite Add gypsum to the mud. Gypsum ($Ca SO_4$) dissolves and Ca^{++} ions are formed. First reaction causes flocculation. Over time Ca^{++} replaces Na^+ in Bentonite platelets, to make Ca^{++} - Bentonite and they aggregate and viscosity goes down. But from now on, there is an excess of Ca^{++} in the mud (and in the filtrate). No new flocculation will occur, and swellable clay does not swell much.



Ion-exchange is dependent on Ca^{++} concentration. Low concentration $\rightarrow$ Partly cation exchange, high concentration $\rightarrow$ complete cation exchange. Partly exchange leads to flocculation tendency.

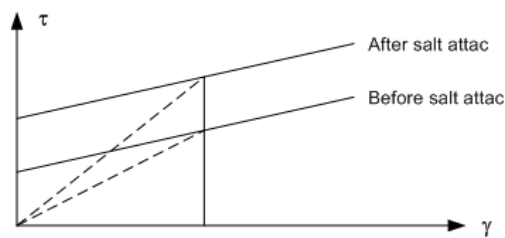


Figure 1-6. Clay behavior.

TURN TO THE EXPERTS FOR SUBSCRIPTION CONSULTANCY

Subscribe is one of the leading companies in Europe when it comes to innovation and business development within subscription businesses.

We innovate new subscription business models or improve existing ones. We do business reviews of existing subscription businesses and we develop acquisition and retention strategies.

Learn more at [linkedin.com/company/subscribe](https://www.linkedin.com/company/subscribe) or contact Managing Director Morten Suhr Hansen at mha@subscribe.dk

SUBSCRIBE - to the future

1.7 FLUID ADDITIVES - SOLUTION

The pH value of WBM is held at 9 – 11 to increase the solubility of anionic compounds.

- a) The change in OH^- concentration required to increase the pH from a particular value to another is given by:

$$\Delta [\text{OH}^-] = \Delta [\text{OH}^-]_{\text{final}} - \Delta [\text{OH}^-]_{\text{initial}}$$

$$\Delta [\text{OH}^-] = 10^{(11-14)} - 10^{(7.5-14)} = 0.001 - 0.000000316 = 0.00099 \text{ mol/l}$$
- b) Mass of NaOH in g/l = concentration molecular weight (of Caustic Soda)

$$= 0.00099 \text{ moles/l } (23 + 16+1) \text{ g/moles} = 0.0198 \text{ g /l}$$
- c) K^+ is geometrically suiting in between the Na-Montmorillonite platelets, and leads to higher platelet attraction (low swelling) than for Na-Montmorillonite. Recall in your chemistry or periodic table (Group 1) that potassium (atom # 20) is more reactive than sodium (atom # 11). Why? The atomic radius of potassium is larger than that of sodium. Therefore, the single valence electron that exists for all alkali metal is located further away from the nucleus for potassium than sodium. This results in less energy required to remove that valence electron from potassium than from sodium, leading to increased reactivity. This trend continues as you move down Group 1 on the periodic table; i.e. Rubidium is more reactive than K.
- d) The mud must have sufficient viscosity & velocity to exceed the settling velocity of the cuttings.
- e) The mud must be thixotropic, i.e. it must have the ability to gel when stationary or when at low laminar flow, but becomes less viscous during circulation or when rigorously shaken by the shale shaker.
- f) A large proportion of the mechanical energy (in the form of WOB and rotation) and hydraulic energy will generate friction and is dissipated as heat. Drilling fluid, which has a high heat capacity, is voluminous (typically 100 m^3) and absorbs this heat and allows the drill bit and the rest of the drill string not to be intensely heated.
- g) The drilling fluid prevents blowouts by providing a hydrostatic pressure at least greater than the formation pressure.

2 RHEOLOGICAL MODELS - SOLUTION

2.1 BINGHAM / POWER-LAW - SOLUTION

a) Field method: $\mu_{pl} = PV = \theta_{600} - \theta_{300} = 106.4 - 75.0 = 31.4 \text{ cP}$
 $YP = \theta_{300} - PV = 75 - 31.4 = 43.6 \text{ lb/100 ft}^2 = 43.6 \cdot 1.06 \cdot 0.4788 = 22.1 \text{ Pa}$

Standard method: $\mu_{pl} = \frac{\Delta\tau}{\Delta\dot{\gamma}} = \frac{54.0 - 38.1}{511} = 0.0311 \text{ Pas} = 31.1 \text{ cP}$
 $YP = \tau_{300} - \mu_{pl} \cdot \dot{\gamma} = 38.1 - 0.0311 \cdot 511 = 22.2 \text{ Pa}$
 $\mu_{\text{Newton}} = \frac{\tau_{600}}{\dot{\gamma}_{600}} = \frac{54.0}{1022} = 0.053 \text{ Pas}$
 $n = 3.32 \log(54 / 38.1) = 0.50$
 $K = 38.1 / 511^{0.5} = 1.69$

b) $100 \text{ PPM} = 100 \cdot 1.703 = 170 \text{ s}^{-1}$

At a shear rate of 170 s^{-1} the shear stress is seen in Table 2-1 to be 21.5 Pa . To answer the question please estimate the shear stress at this shear rate and compare.

$$\tau_{\text{B-H},170} = 27.4 \text{ Pa}$$

$$\tau_{\text{P-L},170} = 21.5 \text{ Pa}$$

P-L is obviously best.

c) To answer the question we need to know at which shear rate to compare the two models. Given data gives us $\bar{v} = q/A = [1000 / (1000 \cdot 60)] / \frac{\pi}{4} \cdot 0.1^2 = 2.12 \text{ m/s}$
 This results in shear rates for the three models, taken from Chapter 6.2 in this exercise book. Pressure loss equations, equal to:

$$\dot{\gamma}_{\text{newt}} = 8 \frac{v}{d} = 8 \cdot \frac{2.12}{0.1} = 170 \text{ s}^{-1}$$

$$\dot{\gamma}_{\text{bingh}} = 8 \frac{v}{d} + \frac{\tau_0}{3\mu_{pl}} = 170 + \frac{22.1}{(3 \cdot 0.0311)} = 407 \text{ s}^{-1}$$

$$\dot{\gamma}_{\text{PL}} = 8 \frac{v}{d} \cdot \frac{3n+1}{4n} = \frac{8 \cdot 2.12}{0.1} \cdot \frac{3 \cdot 0.5+1}{4 \cdot 0.5} = 212 \text{ s}^{-1}$$

Checking the three models theoretically, at the estimated shear rates:

$$\tau_{\text{newt}} = \mu \dot{\gamma} = 0.0601 \cdot 170 = 10.2 \text{ Pa}$$

$$\tau_{\text{Bingh}} = \tau_0 + \mu_{pl} \cdot \dot{\gamma} = 22.1 + 0.0311 \cdot 407 = 34.7 \text{ Pa}$$

$$\tau_{\text{PL}} = K \cdot \dot{\gamma}^n = 1.63 \cdot 212^{0.5} = 24.4 \text{ Pa}$$

Then the recorded; From the graph we read the following shear stress:

Model	Shear rate	Read	Theoretically	Δ
Newton	170	21.5	10.2	-11.3
P-L	212	23.4	24.4	+1.0
Bingham	407	33.2	34.9	+1.7

From this investigation we may conclude that the P-L and Bingham model predict the rheology rather well at this flow rate.

2.2 BINGHAM / POWER-LAW - SOLUTION

- a) The flow curve (τ vs. $\dot{\gamma}$) data show obviously closer nearness to the Power-law model, especially for low shear rates. The Bingham model reads about 12 Pa higher than the measured data. To verify we need model constants:

$$n = \frac{\log(71.05 / 49.75)}{\log(1022 / 511)} = \frac{\log 1.428}{\log 2} = 0.51 \quad K = \frac{\tau}{\dot{\gamma}^n} = \frac{71.05}{1022^{0.51}} = 2.07 \text{ Pas}^{-n}$$

$$\begin{aligned} \mu_{pl} = \theta_{600} - \theta_{300} &= 140 - 98 = 42 \text{ cP}, & \tau_0 = \theta_{300} - \mu_{pl} &= 98 - 42 = 56 \\ & & &= 56 \cdot \text{lb}/100\text{ft}^2 \\ & & &= 56 \cdot 1.06 \cdot 0.478 = 28.42 \text{ Pa} \end{aligned}$$

Verification at 100 RPM (170 s^{-1}), where we read shear stress to be 27.39

$$\tau_{100,PL} = K \cdot \dot{\gamma}^n = 2.07 \cdot 170^{0.51} = 28.41 \text{ Pa}$$

$$\tau_{100,BH} = \tau_0 + \mu_{pl} \cdot \dot{\gamma} = 35.6 \text{ Pa} = 28.42 + 0.042 \cdot 170 = 35.56 \text{ Pa}$$

We observe that the Bingham over-predict as expected, while P-L fits well.



What do you want to do?

No matter what you want out of your future career, an employer with a broad range of operations in a load of countries will always be the ticket. Working within the Volvo Group means more than 100,000 friends and colleagues in more than 185 countries all over the world. We offer graduates great career opportunities – check out the Career section at our web site www.volvogroup.com. We look forward to getting to know you!

VOLVO
AB Volvo (publ)
www.volvogroup.com

VOLVO TRUCKS | RENAULT TRUCKS | MACK TRUCKS | VOLVO BUSES | VOLVO CONSTRUCTION EQUIPMENT | VOLVO PENTA | VOLVO AERO | VOLVO IT
VOLVO FINANCIAL SERVICES | VOLVO 3P | VOLVO POWERTRAIN | VOLVO PARTS | VOLVO TECHNOLOGY | VOLVO LOGISTICS | BUSINESS AREA ASIA

- b) This is a time-effect which occurs while performing rheological readings in the lab. The time being spent while performing the test at low speed gives the colloidal clay particles the possibility to flocculate (edge to face). The flocculation process is much pronounced at low shear rates.

2.3 BINGHAM / POWER-LAW. REGRESSION - SOLUTION

- a) All model constants are necessary for plotting of the three models:

Newtonian model: We initially select the 300 rpm reading

$$\mu = \frac{\tau}{\dot{\gamma}} = \frac{42 \cdot 0.4788}{300 \cdot 1.703} = 0.039 \text{ Pas}$$

Bingham model (field procedure):

$$\mu_{pl} = \theta_{600} - \theta_{300} = 60.4 - 39.6 = 20.8 \text{ cP} = 0.021 \text{ Pas}$$

$$\tau_y = \tau_{300} - \mu_{pl} = 39.6 - 20.8 = 18.8 \frac{\text{lb}}{100} \text{ft}^2 = 18.8 \cdot 1.06 \cdot 0.4788 = 9.6 \text{ Pa}$$

Bingham standard procedure:

$$\mu_{pl} = \frac{\Delta\tau}{\Delta\dot{\gamma}} = (30.6 - 20.2) / 511 = 0.021 \text{ Pas}$$

$$\tau_y = \tau_{300} - \mu_{pl} \cdot \dot{\gamma} = 20.2 - 0.021 \cdot 511 = 9.5 \text{ Pa}$$

Both procedures gave the same answers. This assumes that the factor 1.06 (or 1.067 to be exact) is taken into consideration in standard procedures.

Exponent model:

$$n = \frac{\log \tau_{600} - \log \tau_{300}}{\log \dot{\gamma}_{600} - \log \dot{\gamma}_{300}} = \frac{\log \frac{\tau_{600}}{\tau_{300}}}{\log \frac{\dot{\gamma}_{600}}{\dot{\gamma}_{300}}} = \frac{\log \frac{64}{42}}{\log \frac{600 \cdot 1.703}{300 \cdot 1.703}} = \frac{\log \frac{64}{42}}{\log 2} = 0.60$$

$$K = \frac{\tau}{\dot{\gamma}^n} = \frac{64 \cdot 0.4788}{(600 \cdot 1.703)^{0.608}} = 0.454 \text{ Pas}^n$$

To plot the three curves (see Figure 2-3.1), τ is calculated at 50, 100 and 800 rpm:

Bingham:	τ	=	$9.5 + 0.021 \cdot 50 \cdot 1.703 = 11.3 \text{ Pa}$
		=	$9.5 + 0.021 \cdot 800 \cdot 1.703 = 37.8 \text{ Pa}$
Power-law:	τ	=	$0.454 \cdot (50 \cdot 1.703)^{0.61} = 6.8 \text{ Pa}$
	τ	=	$0.454 (100 \cdot 1.703)^{0.61} = 10.4 \text{ Pa}$
	τ	=	$0.455 (800 \cdot 1.703)^{0.61} = 36.5 \text{ Pa}$

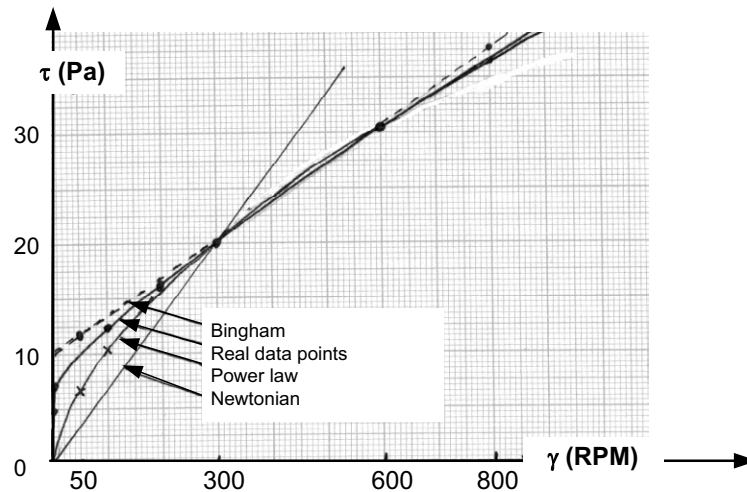


Figure 2-3.1: Rheogram (flow curve) interpreted through 3 rheological models

Readings from the flow curve:

50 rpm	= 10.0 Pa
100 rpm	(already measured)
800 rpm	= 36.5 Pa (extrapolated)

From this we see that the Bingham model suits the mud flow curve best at 50 s^{-1} , since $\tau_{50\text{B-M}}$ is much closer to the real data than $\tau_{50\text{P-L}}$, while at higher shear rates the Power law is the better one.

- b) Plug flow will occur at any laminar flow since shear stress is low in the middle of the pipe. The Bingham model predicts an $YP = 9.1 \text{ Pa}$. This is a theoretical value, but given time at steady-state laminar flow, gel strength will develop, in fact approaching the level of the YP . Shear stresses below this level will lead to gel (flocculation) as shown in Figure 2-3.2.

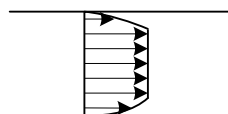


Figure 2-3.2: Plug flow of a Binghamian fluid.

2.4 EFFECTIVE VISCOSITY - SOLUTION

- a) The effective viscosity (Newtonian model):

$$\text{For 600 rpm: } \mu = \frac{\tau}{\dot{\gamma}} = \frac{43 \cdot 0.4788 \cdot 1.06}{600 \cdot 1.703} = 0.021 \text{ Pas} = 21.2 \text{ cP}$$

For 3 rpm: $\mu = \frac{\tau}{\dot{\gamma}} = \frac{3.2 \cdot 0.4788 \cdot 1.06}{3 \cdot 1.703} = 0.318 \text{ Pas} = 318 \text{ cP}$

These and more data points result in Figure 2-4:

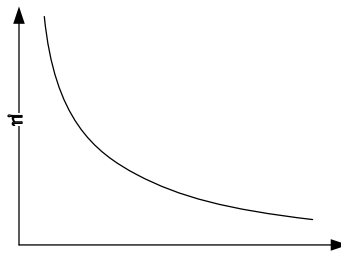


Figure 2-4: Viscosity for a non-Newtonian fluid.

b) When determining the effective viscosity we assume the fluid is closest to a Power law fluid:

2 data points-procedure

$$n = \frac{\log \tau_2 / \tau_1}{\log \dot{\gamma}_2 / \dot{\gamma}_1} = \frac{\log 43 / 30}{\log 2} = 0.52, \quad K = \frac{\tau}{\dot{\gamma}^n} = \frac{43 \cdot 0.4788 \cdot 1.06}{(600 \cdot 1.703)^{0.52}} = 0.59 \text{ Pa s}^{-n}$$

Type equation here.

$$\bar{v} = q / A = \frac{4 \cdot 6000 / (1000 \cdot 60)}{\pi \cdot 0.102^2} = 12.33 \text{ m/s}$$

gaiteye[®]
Challenge the way we run

**EXPERIENCE THE POWER OF
FULL ENGAGEMENT...**

.....

**RUN FASTER.
RUN LONGER..
RUN EASIER...**

**READ MORE & PRE-ORDER TODAY
WWW.GAITEYE.COM**

- c) Always check the Reynold's number:

$$N_{Re} = \frac{\rho \bar{v} d}{\mu_{eff}} = \frac{1100 \cdot 12.3 \cdot 0.102}{0.024} = 57\,500 \rightarrow \text{turbulent}$$

$$\mu_{eff} = \left(8 \frac{\bar{v}}{d} \cdot \frac{3n+1}{4n} \right)^n \cdot \frac{Kd}{8v} = \left(\frac{8 \cdot 12.33}{0.012} \cdot \frac{3 \cdot 0.52 + 1}{4 \cdot 0.52} \right)^{0.52} \cdot \frac{0.59 \cdot 0.102}{8 \cdot 12.33} = 0.024 \text{ Pas}$$

Use therefore a turbulent pressure loss model:

$$\Delta p = a N_{Re}^{-b} \cdot 4 \frac{L}{d} \cdot \frac{1}{2} \rho v^2$$

- d) High YP is caused by slow flocculation/gelling. At long still-stand (10 min or more) the gel strength will approach the YP.

2.5 ALL MODELS - SOLUTION

- a) $\mu_{pl} = (55-40) / 511 = 0.0294 \text{ Pas} = 29 \text{ cP}$

$$\tau_y = \tau - \dot{\gamma} \cdot \mu_{pl} = 55 - 1022 \cdot 0.0294 = 25.4 \text{ Pa}$$

$$n = 3.32 \cdot \log 55/40 = 0.459$$

$$K = \tau/\dot{\gamma} = 55 / 1022^{0.459} = 2.28 \text{ Pas}^n$$

- b) H & B:
1. Field approach: Take τ_3 as τ_y , and n and K from the Power law model
 2. Standard: 3 points; iteration; select the 3 data points closest to actual shear rate, normally the three upper points
 3. Nonlinear regression: 6 data points

- c) Compare the two laminar friction expressions $\Delta p_{Newton} = \Delta p_{Bingham}$, and solve for $\mu_{Newton} (= \mu_{eff})$

- d) Increased PV is an indicator of more suspended, inert fine particles (more mechanical friction).

Increased YP is an indicator of more surface interaction between surface active colloidal particles.

2.6 ALL MODELS. REGRESSION - SOLUTION

- a) Standard 2 data points:

$$\text{Bingham: } \mu_{pl} = (25.4-17.2) / 511 = 0.016 \text{ Pas} = 16 \text{ cP}$$

$$\tau_0 = \tau_{300} - \dot{\gamma}_{300} \cdot \mu_{pl} = 17.2 - 0.016 \cdot 511 = 9 \text{ Pa}$$

$$\text{Power-law: } n = \log (\tau_2/\tau_1) / \log \dot{\gamma}_2/\dot{\gamma}_1 = 3.32 \cdot \log 25 / 17 = 0.56$$

$$K = \tau_{600} / \dot{\gamma}_{600}^n = 53 \cdot 0.4788 / 1022^{0.56} = 0.52 \text{ Pas}^n$$

- b) Regression results for Bingham (straight line) and Power law (curved line) models are presented in Figure 2-6:

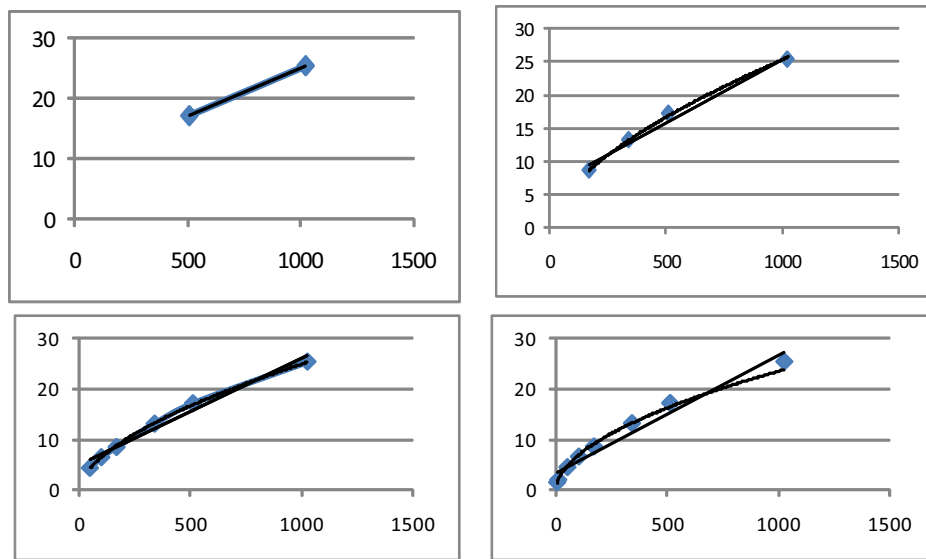


Figure 2-6: Regression result as a function of # of viscometer data points. (2, 4, 6, and 8 data points).

A summary of the results of # of data points:

Data points	Bingham model			Power Law mode		
	PV	YP	R2	n	K	R2
2	0.0160	9.0	-	0.56	0.52	-
4	0.0192	6.3	0.983	0.61	0.39	0.999
6	0.0212	4.8	0.977	0.58	0.45	0.999
8	0.0232	3.4	0.960	0.53	0.59	0.997

The 4 upper points are the most reliable data points. The two lower ones (at 3 and 6 RPM) are influenced by the time delay inflicted by the test procedure (see Task 2.2).
 c1) In the H-B model the constants are found through elimination;

$$\tau_2 = \tau_y + K \cdot \dot{\gamma}_1^n \quad 25.4 = \tau_y + K \cdot 1022^n \quad (1)$$

$$\tau_2 = \tau_y + K \cdot \dot{\gamma}_2^n \quad 17.3 = \tau_y + K \cdot 511^n \quad (2)$$

$$\tau_2 = \tau_y + K \cdot \dot{\gamma}_3^n \quad 13.2 = \tau_y + K \cdot 340^n \quad (3)$$

$$\text{Use (1) and (2): } \tau_y = K \cdot 1022^n - 25.4 = K \cdot 511^n - 17.2 \quad (4)$$

$$\text{to find K: } K = \frac{25.4 - 17.2}{1022^n - 511^n} \quad (5)$$

$$\text{Enter (5) in (2): } 17.2 = \tau_y + \frac{8.1}{1022^n - 511^n} \cdot 511^n \quad (6)$$

$$\text{and in (3): } 13.2 = \tau_y + \frac{8.1}{1022^n - 511^n} \cdot 340^n \quad (7)$$

$$\text{Set (6) = (7): } (-\tau_y =) \frac{8.1}{1022^n - 511^n} \cdot 511^n - 17.2 = \frac{8.1}{1022^n - 511^n} \cdot 340^n - 13.2 \quad (8)$$

$$\tau_y \text{ and } K \text{ are now eliminated: } \frac{8.1}{1022^n - 511^n} \cdot (511^n - 340^n) = 17.3 - 13.2 = 4.1 \quad (9)$$

$$\frac{8.1}{4.1} \cdot (511^n - 340^n) = (1022^n - 511^n) \quad (10)$$

To solve equation (10) we suggest iteration. Start with $n = 0.5$, and we get:

$$\begin{aligned} 1.976 (22.6 - 18.4) &= 32.0 - 22.6 \\ 8.3 &= 9.4 \quad -1.1 \end{aligned}$$

Now try $n = 0.52$:

$$\begin{aligned} 1.976 (25.6 - 20.7) &= 36.7 - 25.36 \\ 9.6 &= 11.1 = -1.5 \end{aligned}$$

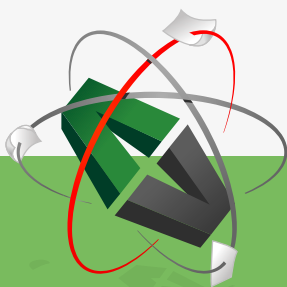
We are moving away. Try $n = 0.48$:

$$\begin{aligned} 1.976 (20.0 - 16.4) &= 27.8 - 20 \\ 7.01 &= -7.8 = -0.7 \end{aligned}$$

Further iteration with decreasing n to 0.35 gives a deviation close to 0 $\rightarrow n = 0.35$. When n is found, the other constants can be found easily. Now $K = 3.4$, resulting in $\tau_y = -13 \text{ Pa}$

c2) Non-linear regression: Please refer to textbook Chapter 10.6 of how to step-wise go about in Excel to determine the constants.

This e-book
is made with
SetaPDF



PDF components for PHP developers

www.setasign.com



2.7 ALL MODELS - SOLUTION

The rheological data are plotted in Fig. 2-7.

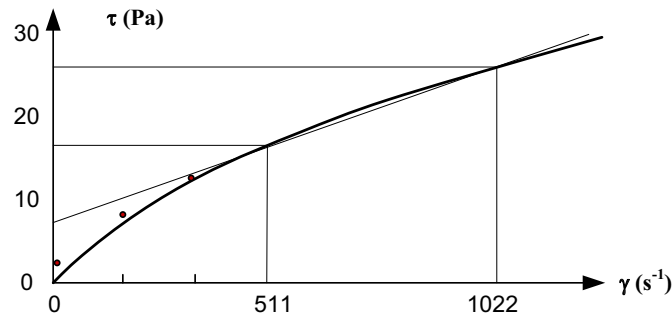


Figure 2-7: The Bingham and the power-law model together with raw-data.

We see that the Bingham model overpredicts and P-L underpredicts. This observation we test below at 10 s^{-1} .

Bingham Field procedure: From the two upper viscometer data points, we obtain:

$$\mu_{pl} = \theta_{600} - \theta_{300} = (52.2 - 35.5) \cdot \frac{1}{1.06} = 15.8 \text{ cP}$$

$$\tau_o = \theta_{300} - \mu_{pl} = \frac{35.5}{1.06} - 15.8 = 17.7 \text{ lb/100ft}^2 = 17.7 \cdot 1.06 \cdot 0.4788 = 9 \text{ Pa}$$

Bingham standard SI-procedure:

$$\mu = \frac{25 - 17}{511} = 0.0157 \text{ Pas}$$

$$\tau_o = 25 - 0.0157 \cdot 1022 = 8.9 \text{ Pa}$$

Power-law, two upper data points:

$$n = 3.32 \cdot \log 25/17 = 0.556$$

$$K = \frac{25}{1022^{0.556}} = 0.52$$

Herschel-Bulkley is determined through the field method: iteration and elimination, based on the three upper readings;

$$\tau = \tau_o + K \cdot \dot{\gamma}^n = 2 + 0.52 \cdot \dot{\gamma}^{0.556}$$

Now we test the models at $\dot{\gamma} = 10 \text{ s}^{-1}$

$$\begin{aligned}\tau_{PL} &= 0.52 \cdot 10^{0.556} &= 1.9 \text{ Pa} \\ \tau_{BH} &= 8.9 + 0.0157 \cdot 10 &= 9.1 \text{ Pa} \\ \tau_{HB} &= 2 + 0.52 \cdot \dot{\gamma}^{0.556} &= 3.1 \text{ Pa}\end{aligned}$$

Since the solution is 3.1 Pa the H-B is closest. The Bingham model is relatively far away, as expected, since its theoretical model is based only on the two upper readings, which are far from the tested shear rate. Therefore it is, as stated in the text book, recommended to apply the data points closest to the actual shear rate of the model. Since these specifics are not always known ahead of time, the next best is to use all the data points (regression), not only the two upper ones or a few selected ones.

3 DRILLING FLUID DYNAMICS - SOLUTION

3.1 VELOCITY PROFILE. CONTINUITY EQUATION - SOLUTION

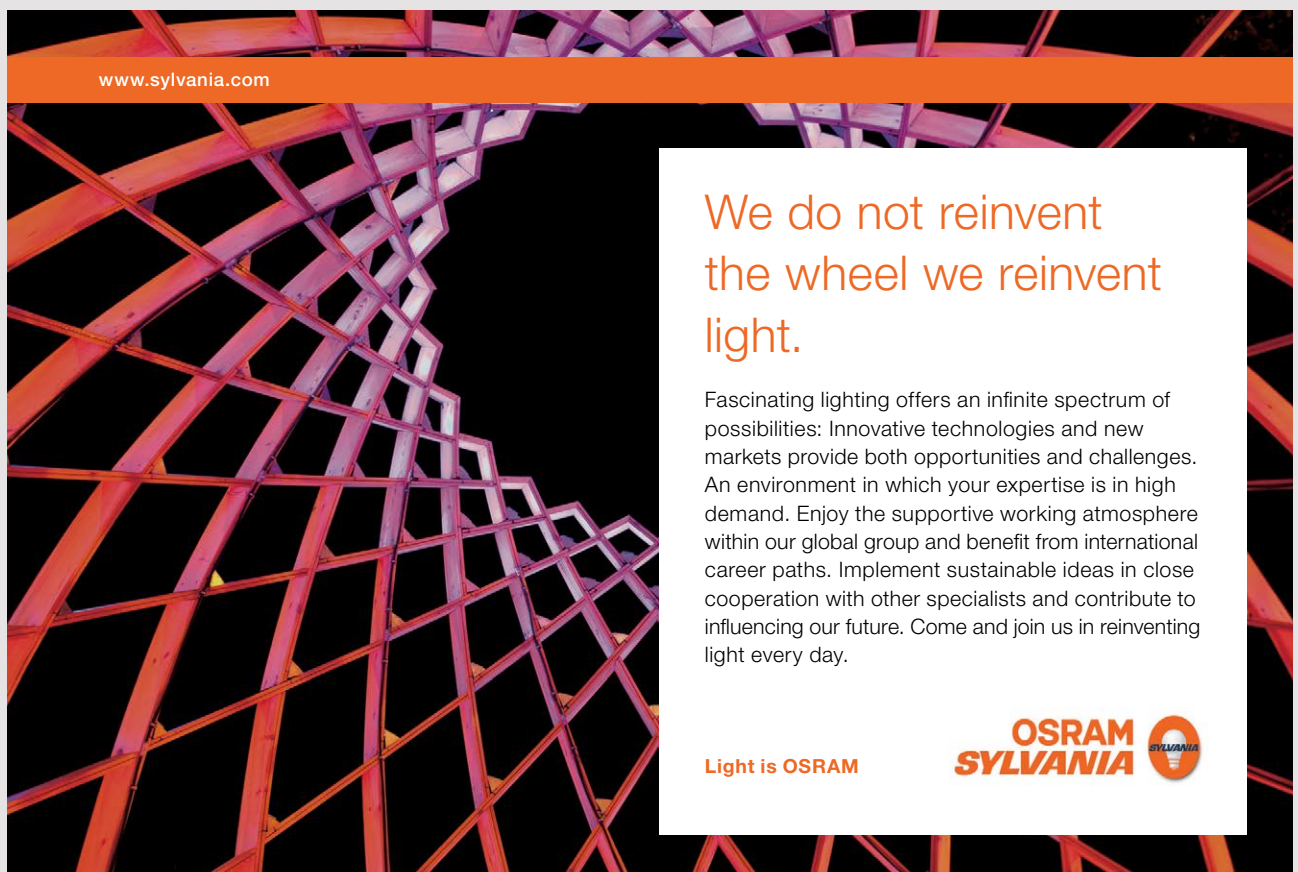
Define cross sectional flow area and discretize in the z-direction and then integrate velocity over the A.

$$A = z \cdot b \rightarrow dA = b \cdot dz$$

Average velocity:

$$\bar{v} = \frac{1}{A} \int az(z_0 - z)b \cdot dz$$

$$\bar{v} = \frac{ab}{z_0 b} \int (z_0 z - z^2) dz$$



www.sylvania.com

We do not reinvent the wheel we reinvent light.

Fascinating lighting offers an infinite spectrum of possibilities: Innovative technologies and new markets provide both opportunities and challenges. An environment in which your expertise is in high demand. Enjoy the supportive working atmosphere within our global group and benefit from international career paths. Implement sustainable ideas in close cooperation with other specialists and contribute to influencing our future. Come and join us in reinventing light every day.

Light is OSRAM

OSRAM SYLVANIA 

$$\bar{v} = \frac{a}{z_0} \cdot \left[\frac{z_0}{2} z^2 - \frac{1}{3} z^3 \right]$$

$$\bar{v} = \frac{a}{z_0} \left(\frac{z_0^3}{2} - \frac{z_0^3}{3} \right) = az_0^2 \left(\frac{1}{2} - \frac{1}{3} \right) = az_0^2 \cdot \frac{1}{6}$$

$v_{\max}$ is found when the derivative of $v(z)' = 0$

$$\frac{dv}{dz} = \frac{d(azz_0 - az^2)}{dz} = az_0 - 2az = 0$$

$$2az = az_0 \rightarrow \max \text{ at } z = \frac{z_0}{2}$$

$$v_{\max} = a \frac{z_0}{2} \left(z_0 - \frac{z_0}{2} \right) = \frac{az_0^2}{4}$$

Find $v_{\max}$ when: $\bar{v} = 8 \text{ cm/s}$ and $z_0 = 4 \text{ cm}$

$$\bar{v} = az_0^2 \cdot \frac{1}{6}$$

$$8 = a \cdot 16 \cdot \frac{1}{6}$$

$$a = \frac{8 \cdot 6}{16} = \frac{12}{4} = 3 \text{ m/s}$$

$$\text{Finally: } v_{\max} = \frac{3 \cdot 4^2}{4} = 12 \text{ cm/s}$$

3.2 VELOCITY PROFILE. MOMENTUM FLUX - SOLUTION

a) To find the pressure distribution: We start with Navier-Stokes in the z-direction, cylindrical coordinates:

$$v \frac{\partial v}{\partial z} = -\frac{1}{\rho} \frac{\partial p}{\partial z} + \frac{\mu}{\rho} \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 v}{\partial \theta^2} + \frac{\partial^2 v}{\partial z^2} \right] + g_z$$

Under stationary laminar flow the equation reduces to:

$$0 = -\frac{1}{\rho} \frac{\partial p}{\partial z} + \frac{\mu}{\rho} \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v}{\partial r} \right) \right]$$

$$\frac{\partial p}{\partial z} = \mu \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v}{\partial r} \right)$$

To replace the latter part of the equation with manageable parameters we go through 3 steps:

Step 1: Define $\partial v / \partial r$ from $v(r)$: $v = v_{\max} \left(1 - \frac{r^2}{R^2} \right)$, $v_{\theta} = v_r = 0$

Step 2: $\frac{\partial v}{\partial r} = v_{\max} \left(-\frac{2r}{R^2} \right)$

Step 3: Now we derive the part $r \cdot \frac{\partial v}{\partial r}$ with respect to r:

$$\frac{\partial}{\partial r} r \cdot v_{\max} \left(-\frac{2r}{R^2} \right) = -\frac{v_{\max} \cdot 2}{R^2} \cdot 2r$$

The pressure distribution or pressure gradient now becomes:

$$\frac{\partial p}{\partial z} = \mu \cdot \frac{1}{r} \cdot \left(-\frac{v_{\max} \cdot 4r}{R^2} \right)$$

Total pressure loss along z:

$$\int_{p(o)}^{p(z)} \partial p = - \int_0^z \frac{4\mu v_{\max}}{R^2} \partial z$$

$$\Delta p = - \left(0 - \frac{4\mu v_{\max} z}{R^2} \right) = 4\mu v_{\max} z / R^2$$

The shear stress is found as: $\tau = -\mu \cdot \frac{\partial v}{\partial r} = \mu v_{\max} \left(\frac{2r}{R^2} \right)$.

The maximum of τ is found when $r = R$, i.e. at the wall as always. Navier Stoke deals with incompressible fluids; density does not change.

$$\tau_{\max} = \mu \cdot v_{\max} \cdot \frac{2}{R}$$

b1) Wall shear stress: The wall shear follows from the definition of a Newtonian fluids:

The x and r direction must be replaced by y and z respectively.

$$\tau_w = \tau_{wxywall} = \mu \left(\frac{\partial v_z}{\partial y} + \frac{\partial v_{xy}}{\partial z} \right) |_{y=\pm h} = \mu \frac{\partial}{\partial y} \left[\left(-\frac{dp}{dz} \right) \left(\frac{h^2}{2\mu} \right) \left(1 - \frac{y^2}{h^2} \right) \right] |_{y=\pm h}$$

$$\tau_w = -\mu \frac{\partial v_z}{\partial y} \quad (\text{since } v_{y=0})$$

$$\tau_w = \pm \mu \left(-\frac{dp}{dz} \right) \cdot \frac{h^2}{2\mu} \left(-\frac{2y}{h^2} \right) = \frac{dp}{dx} h = \frac{dp}{dx} (h - -h) = 2h \frac{dp}{dx}$$

$v_{\max}$ is reached when $y = 0$:

$$v_{\max} = \frac{dp}{dx} \cdot \frac{h^2}{2\mu} \rightarrow \frac{dp}{dx} = v_{\max} \cdot \frac{2\mu}{h^2}$$

b2) Average velocity:

It is defined as $\bar{v} = q/A$, where $q = \int v \, dA$, over the cross section.

For our particular distribution: $A = b \cdot y \rightarrow dA = b \cdot dy$,

$$\bar{v} = \frac{1}{A} \int v \, dA = \frac{1}{b(2h)} \int_{-h}^{+h} \frac{dp}{dz} \cdot \frac{h^2}{2\mu} \left(1 - \frac{y^2}{h^2} \right) b \, dy$$

$$= \frac{1}{2h} \cdot v_{\max} \int \left(1 - \frac{y^2}{h^2} \right) dy = \frac{v_{\max}}{2h} \left[h - \frac{h^3}{3h^2} - \left(-h - \frac{-h^3}{3h^2} \right) \right] = \frac{2}{3} v_{\max}$$

In plane Poiseulle flow between parallel plates, the average velocity is two-thirds of the maximum value.

3.3 FLOW PROFILE - SOLUTION

- The equation represents the conservation of the momentum for stationary, incompressible, curl free, laminar pipe flow, also called the Navier Stoke equation.
- From the momentum equation and the stated condition;

$$0 = -\frac{\partial p}{\partial x} + \mu \left[\frac{1}{r} \cdot \frac{\partial}{\partial r} \left(\frac{\partial(rv)}{\partial r} \right) \right]$$

From boundary condition, rearranging/integrating twice, $v(r)$ is found.

Alternatively, start with the shear stress vs. friction pressure for laminar pipe flow; or, one step later, the general shear stress equation:

$$\tau = \frac{r}{2} \frac{dp}{dx} = -\mu \frac{dv(r)}{dr}$$

$$dv(r) = -\frac{1}{2\mu} \cdot r \frac{dp}{dx} \cdot dr$$

$$v(r) = -\frac{1}{2\mu} \cdot \frac{dp}{dx} \frac{r^2}{2} + C_1$$

Here a typo; dp/dr should be dp/dx

$$v(R) = 0, C_1 = \frac{1}{4\mu} \cdot R^2 \frac{dp}{dx}$$

$$v(r) = \frac{1}{4\mu} \frac{dp}{dx} (R^2 - r^2)$$

dp/dx is the local pressure gradient. Since it is constant, the integrated pressure gradient is equal to the total pressure loss over the total length; $\Delta p/L$

c) Average velocity is found by taking the areal average of the integrated velocity $v(r)$:

$$\bar{v} = \frac{1}{A} \int v dA = \frac{1}{\pi R^2} \frac{dp/dx}{4\mu} \int_0^R (R^2 - r^2) 2\pi r dr = \frac{R^2}{8} \cdot \frac{dp/dx}{\mu}$$

To compare $v_{\max}$ and $\bar{v}$ we need first to express $v_{\max}$;

$$v_{\max} = v(r = 0) = \frac{1}{4\mu} \cdot \frac{dp}{dx} R^2$$



Discover the truth at www.deloitte.ca/careers

Deloitte.

© Deloitte & Touche LLP and affiliated entities.



By comparing the two we find an expression of axial dispersion:

$$\frac{v_{max}}{\bar{v}} = \frac{1 \cdot dp/dx \cdot R^2 \cdot \mu}{4\mu \cdot R^2 / 8 \cdot dp/dx} = 2$$

From this evaluation we can conclude that axial dispersion is independent of the factors shown above and that it is always positive; the max velocity is twice the average velocity.

d) The wall shear stress is found in two steps:

$$\text{Step 1: } dp/dx = 0.09 \text{ MPa/1 000 m} = 90 \text{ Pa/m}$$

$$\text{Step 2: } \tau_w = \frac{dp}{dx} \cdot \frac{R}{2} = \frac{0.09}{2} \cdot 90 = 2.25 \text{ Pa}$$

$$\bar{v} = \frac{R^2}{8} \cdot \frac{dp/dx}{\mu} = \frac{0.05^2}{8} \cdot \frac{90}{0.0538} = 0.52 \text{ m/s}$$

3.4 PRESSURE LOSS VS. RHEOLOGY I - SOLUTION

a) Average velocity

Average velocity is u_o

$$\bar{u} = \frac{1}{A} \int u(r) dA = u_o \quad A = \pi r^2 \rightarrow dA = 2\pi r dr$$

$$= \frac{1}{\pi R^2} u_{max} \int \left(1 - \frac{r}{R}\right)^{1/4} \cdot 2\pi r dr = 2 \frac{u_{max}}{R^2} \int () r dr \quad (\text{typo: } 2 \text{ pdr should be } 2 \text{ prdr})$$

Substitution is the solution method:

$$\int_0^R \left(1 - \frac{r}{R}\right)^m r dx =$$

$$y = \left(1 - \frac{r}{R}\right) \rightarrow r = (1 - y)R \quad r/R \text{ vs. } Y: 0 \text{ vs. } 1, 1 \text{ vs. } 0$$

$$dr = -dy \cdot R$$

$$\bar{y}^m = \int y^m \cdot (1 - y)R (-dyR) = -R^2 \int y^m (1 - y) dy$$

$$-R^2 \int y^m dy + R^2 \int y^{m+1} dy$$

$$= R^2 \left(-\frac{y^{m+1}}{m+1} + \frac{y^{m+2}}{m+2} \right) \Big|_0^1$$

$$= R^2 \left(-\frac{\left(1 - \frac{r}{R}\right)^{m+1}}{m+1} + \frac{\left(1 - \frac{r}{R}\right)^{m+2}}{m+2} \right) \Big|_0^R$$

$$= R^2 \left(-\frac{0}{m+1} + \frac{0}{m+2} - \left(-\frac{1}{m+1} + \frac{1}{m+2} \right) \right)$$

$$= R^2 \left(\frac{1}{m+1} - \frac{1}{m+2} \right) = \frac{R^2}{(m+2)(m+1)} = \frac{R^2}{\frac{9}{4} \cdot \frac{5}{4}} =$$

$$\bar{y}^{1/4} = 0.355 R^2$$

$$\bar{u} = \frac{2U_m \cdot 0.355 R^2}{R^2} = 0.71 U_m$$

$$\tau_w = \mu \cdot \frac{du}{dr} \rightarrow \frac{du}{dr} = \frac{-U_m}{R} \frac{\left(1 - \frac{1}{R}\right)}{\left(1 - \frac{r}{R}\right)^{3/4}} \quad r \rightarrow R, \quad \tau \rightarrow \infty$$

b) To find pressure loss we first need to check the Reynolds number:

$$(\mu_{pl} = 0.016, \tau_o = 9 \text{ Pa}, n = 0.56, K = 0.52)$$

$$N_{Re} = \rho v d / \mu_{eff}$$

$$\bar{v} = \frac{q}{A} = \frac{\frac{1}{60}}{\frac{\pi}{4} 0.1^2} = 2.12 \text{ m}^3/\text{s}$$

$$N_{Re} = \frac{d^n \cdot \bar{v}^{2-n} \cdot \rho}{K_p [(3n+1)/4n]^n \cdot 8^{n-1}} = \frac{0.1^{0.56} \cdot 2.12^{1.44} \cdot 1000}{0.52 \cdot \left(\frac{3 \cdot 0.56 + 1}{4 \cdot 0.56}\right)^{0.56} \cdot 8^{-0.44}} = 3500 \Rightarrow \text{Turbulent, but in this exercise we}$$

need to assume laminar flow

For the Newtonian model we determine the viscosity at the estimated shear rate

$$\gamma = 8v/d = 8 \cdot 2.12 / 0.1 = 169.6 \text{ s}^{-1}. \text{ Here the viscosity is:}$$

$$\mu = \tau / \gamma = 8.6 \text{ (from Task 2.6)} / 169.6 = 0.0507 \text{ Pas}$$

Laminar pressure loss equations give these results:

$$\text{Newton: } \Delta p_N = 32 \mu L v / d^2 = 32 \cdot 0.0507 \cdot 1000 \cdot 2.12 / 0.10 = 3.4 \cdot 10^5 \text{ Pa}$$

$$\text{Power-law: } \Delta p_{PL} = 4K(8v/d \cdot (3n+1)/4n)^n \cdot 1/d \cdot L$$

$$= 4 \cdot 0.52 (8 \cdot 2.12 / 0.1 \cdot 2.68/2.24)^{0.56} \cdot 1/0.1 \cdot 1000 = 4.1 \cdot 10^5 \text{ Pa}$$

$$\text{Bingham: } \Delta p_{BH} = 32 \cdot 0.016 \cdot 1000 \cdot 2.12 / 0.1^2 + 16 \cdot 1000 \cdot 9 / 3 \cdot 0.1 = 5.9 \cdot 10^5 \text{ Pa}$$

We observe that Bingham “aims” high at low shear rates, and will always produce higher results than the Power-law model at low shear rates.

c) Calculated shear rate for all models:

$$\gamma_{Newt} = 8v/d = 8 \cdot 2.12 / 0.1 = 170 \text{ s}^{-1}$$

$$\gamma_{PL} = 8v/d \cdot (3n+1)/4n = 170 \cdot (3 \cdot 0.56 + 1) / 4 \cdot 0.56 = 203 \text{ s}^{-1}$$

$$\gamma_{BH} = 8v/d + \tau_o / (3\mu_{pl}) = 8 \cdot 2.12 / 0.1 + 9 / (3 \cdot 0.016) = 170 + 188 = 358 \text{ s}^{-1}$$

We read from Figure 3-4 for all the models;

$$\tau_N = 8.5 \text{ Pa at } 170 \text{ s}^{-1};$$

$$\tau_{PL} = 10 \text{ Pa at } 203 \text{ s}^{-1};$$

$$\tau_{BH} = 14 \text{ Pa at } 358 \text{ s}^{-1};$$

And the resulting pressure loss becomes:

$$\Delta p_N = 8.5 \cdot 1000 / 0.1 \cdot 4 = 3.4 \cdot 10^5 \text{ Pa}$$

$$\Delta p_{P-L} = 10 \cdot 1000 / 0.1 \cdot 4 = 4.0 \cdot 10^5 \text{ Pa}$$

$$\Delta p_{BH} = 14 \cdot 1000 / 0.1 \cdot 4 = 5.6 \cdot 10^5 \text{ Pa}$$

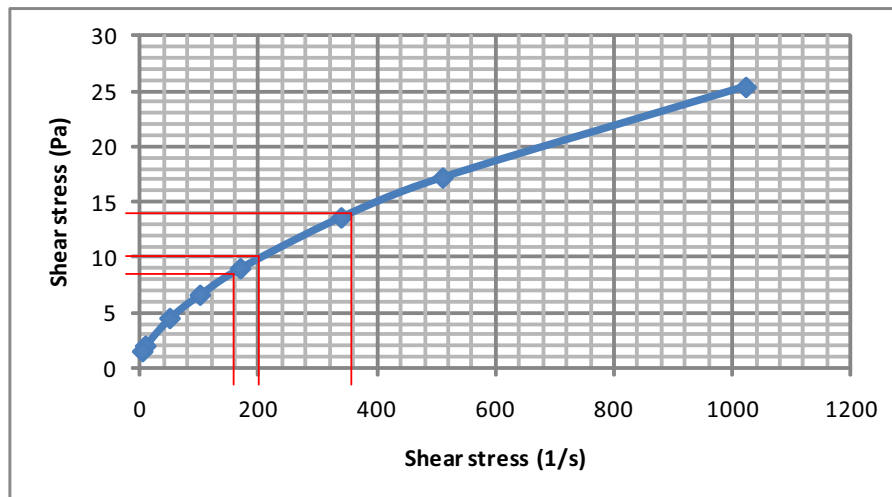


Figure 3-4: Graphical presentation of viscometer data and reading of shear stress for individual shear rates.

Cynthia | AXA Graduate

**AXA Global
Graduate Program**

Find out more and apply

redefining / standards



Model	$\dot{\gamma}$ (s ⁻¹)	Read from Fig. 3-4 (Pa)	Estimated from universal. eqn (bar)	Estimated from ordinary model (bar)
Newton	170	8.5	3.4	3.4
Power-law	203	10	4.0	4.3
Bingham	358	14	5.2	5.9

One conclusion is that the two non-Newtonian ordinary and universal models give similar results. But the different models give different results. The best fit is as expected the P-L.

d) Force Balance:

$$\tau \cdot 2\pi \cdot \Delta L = \Delta p \cdot \pi r \quad \rightarrow \quad \tau_w = \frac{1}{2} R \cdot \frac{\Delta p}{\Delta L}$$

And solving $\Delta p_{\text{Newton}} = \Delta p_{\text{Bingham}}$ for μ_{eff} gives the answer.

e) A uniform pipe has an entrance length. Increasing length with increasing N_{Re}
Undeveloped flow at the entrance is turbulent and has higher shear until boundary layer expands and meets in the middle.

3.5 PRESSURE LOSS VS. RHEOLOGY II - SOLUTION

RPM	$\dot{\gamma}$	θ		τ	τ
rpm	s ⁻¹	-		lb/100 ft ²	Pa
600	1022	66.0		70	33.5
300	511	47.2		50	23.9
100	170	25.5		27	12.9
6	10	9.4		10	4.8

$$\mu_{pl} = \theta_{600} - \theta_{300} = 66 - 47.2 = 18.8 \text{ cP} = 0.019 \text{ Pas}$$

$$\tau_0 = \theta_{300} - \mu_{pl} = 47.2 - 18.8 = 28.4 \frac{\text{lb}}{100} \text{ ft}^2 = 28.4 \cdot 1.06 \cdot 0.4788 = 14.4 \text{ Pa}$$

$$\mu_{pl} = \frac{\Delta \tau}{\Delta \dot{\gamma}} = \frac{33.5 - 23.9}{511} = 0.0188 \text{ Pas}$$

$$\tau_0 = \tau_{300} - \mu_{pl} \cdot \dot{\gamma} = 33.5 - 0.0188 \cdot 1022 = 14.3 \text{ Pa}$$

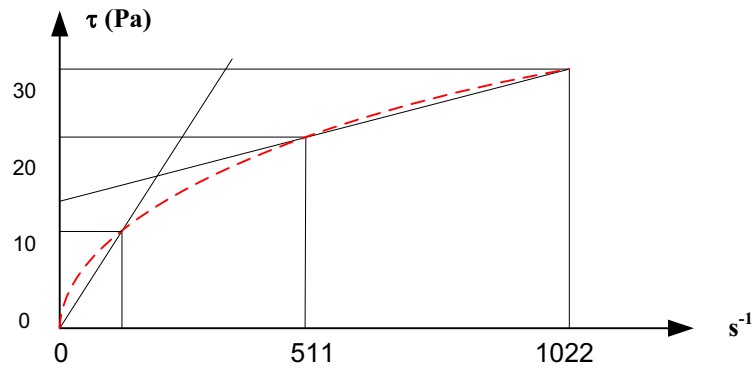


Figure 3-5: Rheogram for relevant rheology.

The Newton model can also be based on the two upper readings like for the non-Newtonian. Use then the average values.

- a) At this low flow rate we assume laminar flow, but still we have to check;

$$\bar{v} = q/A = \frac{4}{\pi} \cdot \frac{q}{d^2} = \frac{4}{\pi} \cdot \frac{800}{0.109^2 \cdot 1000 \cdot 60} = 1.425 \text{ m/s}$$

$$N_{re} = \frac{\rho v d}{\mu_{eff}} = 1100 \cdot 1.425 \cdot 0.109 / 0.2 = 855$$

$$\text{Above we need: } \mu_{eff} = \mu_{pl} + \frac{\tau_0 \cdot d}{6\bar{v}} = 0.0188 + \frac{14.3 \cdot 0.109}{6 \cdot 1.425} = 0.2 \text{ Pas}$$

$$\Delta p_{pipe} = \frac{32\mu_{pl} \cdot L \cdot \bar{v}}{d^2} + \frac{16L\tau_0}{3d} = \frac{32 \cdot 0.0188 \cdot 1.425 \cdot 1000}{0.109^2} + \frac{16 \cdot 1000 \cdot 14.3}{3 \cdot 0.109} = 7.8 \cdot 10^5 \text{ Pa}$$

- b) To compare the two we need to compute Newtonian pressure loss at the correct shear rate.

$$\dot{\gamma}_{Newt} = \frac{8\bar{v}}{d} = \frac{8 \cdot 1.425}{0.109} = 105 \text{ s}^{-1}$$

$$\dot{\gamma}_{BH} = \frac{8\bar{v}}{d} + \frac{\tau_0}{3\mu_{pl}} = 105 + \frac{14.3}{3 \cdot 0.019} = 356 \text{ s}^{-1}$$

Read from Figure 3-5 that $\tau = 10$ and 25 Pa at the two shear rates 105 and 356 s^{-1} respectively.

$$\Delta p_{univ,N} = 4\tau_w \cdot \frac{L}{d} = 4 \cdot 10 \cdot \frac{1000}{0.109} = 3.7 \cdot 10^5 \text{ Pa}$$

$$\Delta p_{univ,BH} = 4 \cdot 25 \cdot \frac{1000}{0.109} = 9.2 \cdot 10^5 \text{ Pa}$$

Bingham model gives the best answers. This is natural since the mud has a typical Binghamian characteristic at laminar flow. We could also have compared the two models by using the normal pressure loss models. We must then first determine the specific viscosity, just like for the universal models. See also Exercise 3.4 in this regard.

3.6 PRESSURE LOSS. POWER LAW - SOLUTION

a) Power law: $\tau = k \cdot \gamma^n$, $\gamma = -\frac{dv}{dr}$

From force balance we derive:

$$\tau \cdot 2\pi r L = (p_1 - p_2) \pi r^2 \quad \rightarrow \quad \tau = \frac{\Delta p \cdot r}{2L}$$

Using Power law model, we obtain:

$$K \cdot \gamma^n = \frac{\Delta p \cdot r}{2L} \quad \rightarrow \quad \gamma = \left(\frac{\Delta p}{2LK} \right)^{\frac{1}{n}} \cdot r^{\frac{1}{n}}$$

Knowing that $\gamma = dv/dr$ we can find $v(r)$ from:

$$\int_{v(r)}^0 dv = \int_r^R \left[\frac{\Delta p}{2LK} \right]^{\frac{1}{n}} r^{\frac{1}{n}} dr$$

$$v(r) = \left[\frac{\Delta p}{2LK} \right]^{\frac{1}{n}} \cdot \frac{n}{n+1} \left[R^{\frac{n+1}{n}} - r^{\frac{n+1}{n}} \right]$$

We need to integrate over the cross sectional area:

$$q = \bar{v} \pi r^2 \quad \rightarrow \quad dq = v(r) \pi 2r dr$$

$$\begin{aligned} q &= \int_0^R \left[\frac{\Delta p}{2LK} \right]^{\frac{1}{n}} \cdot \frac{n}{n+1} \left[R^{\frac{n+1}{n}} - r^{\frac{n+1}{n}} \right] \pi \cdot 2 \cdot r dr = \pi \cdot 2 \left[\frac{\Delta p}{2LK} \right]^{\frac{1}{n}} \frac{n}{n+1} \left[R^{\frac{n+1}{n}} \cdot \frac{R^2}{2} - \frac{n}{3n+1} \cdot R^{\frac{3n+1}{n}} \right] \\ &= \pi \cdot 2 \left[\frac{\Delta p}{2LK} \right]^{\frac{1}{n}} \frac{n}{n+1} \left[\frac{1}{2} R^{\frac{3n+1}{n}} - \frac{n}{3n+1} \cdot R^{\frac{3n+1}{n}} \right] = \pi \cdot 2 \left[\frac{\Delta p}{2LK} \right]^{\frac{1}{n}} \frac{n}{n+1} \left[\frac{n+1}{2(3n+1)} - \frac{2n}{2(3n+1)} \right] R^{\frac{3n+1}{n}} \end{aligned}$$

I joined MITAS because
I wanted **real responsibility**

The Graduate Programme
for Engineers and Geoscientists
www.discovermitas.com



Month 16

I was a construction supervisor in the North Sea advising and helping foremen solve problems

Real work
International opportunities
Three work placements



MAERSK

With this expression of q_{tot} we set up this relationship:

$$q = \pi R^2 \cdot \bar{v} \Rightarrow \pi R^2 \cdot \bar{v} = \pi \left[\frac{\Delta p}{2LK} \right]^{\frac{1}{n}} \cdot n \cdot \left[\frac{n}{3n+1} \cdot R^{\frac{3n+1}{n}} \right]$$

and solved finally for Δp :

$$\Delta p = 4K \left[\frac{8\bar{v}}{d} \cdot \frac{3n+1}{4n} \right] \cdot \frac{L}{d}$$

b) Enter effective (Newtonian) viscosity for Power law fluids into the N_{Re} expression:

$$\mu_{eff,PL} = \left(\frac{8\bar{v}}{d} \right)^{n-1} \cdot K_p \text{ where } K_p = K \cdot \left(\frac{3n+1}{4n} \right)^n$$

$$N_{Re} = \frac{\rho \cdot \bar{v} d}{\mu_{eff}} = \frac{d^{n-1+1}}{v^{n-1-1}} \cdot \frac{\rho}{K_p \cdot 8^{n-1}} = \frac{d^n \cdot \bar{v}^{2-n} \cdot \rho}{K_p \cdot 8^{n-1}} = N_{Re,pipe}$$

$$\begin{aligned} \text{c) Power law fluids: } \frac{d_h^n \cdot v^{2-n} \cdot \rho}{K_a \cdot 12^{n-1}} &= \frac{\rho}{K_a (12^{n-1})} \cdot (d_o - d_i)^n \cdot \left(\frac{q}{\frac{\pi}{4} (d_o^2 - d_i^2)} \right)^{2-n} = C \frac{(d_o - d_i)^n}{(d_o^2 - d_i^2)^{2-n}} = \\ &= \frac{(d_o - d_i)^{2n}}{(d_o^2 - d_i^2)^2} = \frac{(d_o - d_i)^{2n}}{(d_o - d_i)(d_o + d_i)} = \frac{(d_o - d_i)^{2n-1}}{(d_o + d_i)} \end{aligned}$$

Newtonian fluids:

$$N_{Re,Newt} = \frac{\rho_1 v \cdot d_h}{\mu} = \frac{c_1 4q (d_o - d_i)}{c_2 \pi \cdot d_h (d_o - d_i)^2} = \frac{\rho_1 \cdot 4 \cdot q}{\mu} \cdot \frac{d_o - d_i}{(d_o - d_i)(d_o + d_i)} = \frac{c}{d_o + d_i}$$

N_{Re} increases for Newtonian fluids when d_i increases, while for Power law fluids it is reversed! The physical explanation for this behavior is the forced streamlining of the flow in narrow gaps. Out in the ocean, on the other hand, ocean water turns turbulent at very low shear rates.

3.7 PRESSURE LOSS. TURBULENT FLOW. ENERGY EQUATION - SOLUTION

Average velocity:

$$\bar{v} = \frac{q}{\pi R^2} = \frac{0.2 \text{ m}^3 / \text{s}}{\pi (0.1 \text{ m})^2} = 6.4 \text{ m} / \text{s}$$

$$N_{Re} = \frac{\rho \bar{v} d}{\vartheta} = \frac{\bar{v} d}{\mu} = \frac{6.4 \cdot 0.2}{0.00001} = 128\,000 \rightarrow \text{turbulent (Kinematic viscosity; } \vartheta = \mu/\rho)$$

From Chapter 4.3 in the Textbook we find $\varepsilon = 0.26 \text{ mm}$ for cast-iron pipe. Then

$$\frac{\varepsilon}{d} = \frac{0.26 \text{ mm}}{200 \text{ mm}} = 0.0013$$

Enter the Moody chart (Figure 4-12 in the Textbook) on the right hand side at $\varepsilon/d = 0.0013$ (need to interpolate), and move to the left to intersect with $N_{Re} = 128\,000$. Read: $f = 0.0225$. The head loss becomes:

$$h_f = f \frac{L}{d} \cdot \frac{\bar{v}^2}{2g} = (0.0225) \frac{500\text{ m}}{0.2\text{ m}} \cdot \frac{(6.4\text{ m/s})^2}{2 \cdot (9.81\text{ m/s}^2)} = 117\text{ m}$$

3.8 PRESSURE LOSS VS. FLOW RATE - SOLUTION

From exercise 2-7 we copy these data and present the flow curve in Figure 3-8a:

$$n = 0.56, K = 0.52\text{ Pa s}^{0.56}$$

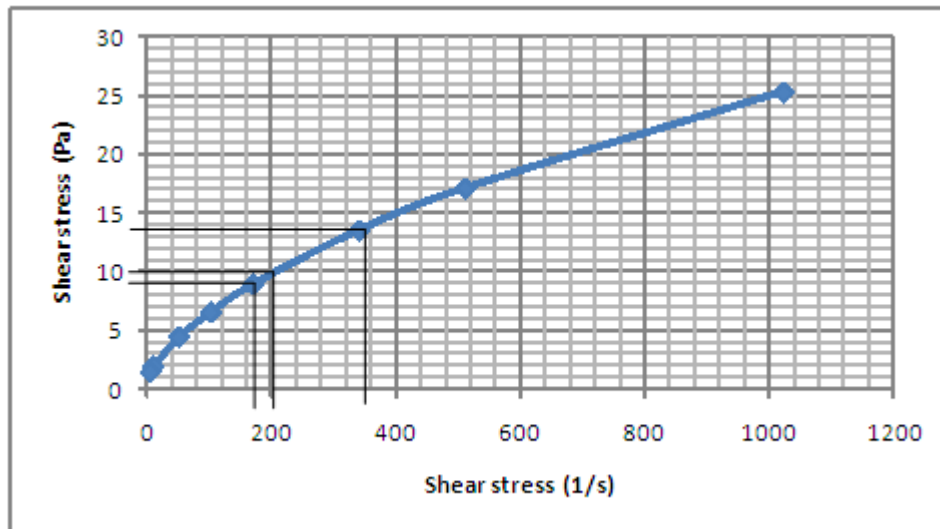


Figure 3-8a: Flow curve.

The pressure loss equations:

$$\Delta p_{lam} = 4 K \left(\frac{8\bar{v}}{d} \cdot \frac{3n+1}{4K} \right)^n \frac{1}{d} \cdot \Delta L = 4 \cdot 0.52 \left(\frac{8 \cdot v}{0.1} \cdot \frac{2.68}{2.24} \right)^{0.56} \frac{1}{0.1} \cdot 1000 = 267\,553 \cdot v^{0.56}$$

$$\Delta p_{turb} = a \cdot N_{Re}^{-b} \cdot \frac{4L}{d_h} \cdot \frac{1}{2} \rho \bar{v}^2 = 1.619 \cdot 10^6 \cdot N_{Re}^{-0.214} \cdot v^2$$

$$a = (\log n + 3.93) / 50 = (\log 0.56 + 3.93) / 50 = 0.0736, b = 0.286$$

$$b = (1.75 + \log n) / 7 = (1.75 + \log 0.56) / 7 = 0.286$$

$$\bar{v} = \frac{q}{A} = \frac{q}{\pi/4 \cdot 0.1^2} = 127.4\, q$$

$$N_{Re} = \frac{\rho \cdot \bar{v} d}{\mu_{eff}} = \frac{d^n \cdot \bar{v}^{2-n} \cdot \rho}{K_p \cdot 8^{n-1}} = \frac{0.1^{0.56} \cdot v^{1.44} \cdot 1100}{0.56 \cdot \left(\frac{3 \cdot 0.56 + 1}{4 \cdot 0.56} \right)^{0.56} \cdot 8^{-0.44}} = 1\,206 \cdot v^{1.44}$$

Select three data points in the laminar region and three at higher flow / turbulent regime and plot the result (Figure 3-8b):

Symbol	q		v	N _{Re}	Δp_{lam}	Δp_{turb}
Unit	l/min	m ³ /s	m/s	-	MPa	MPa
Data	100	0.00170	0.22	136	0.11	
	250	0.00417	0.53	1083	0.18	
	500	0.00833	1.06	2170	0.28	0.20
	1000	0.017	2.12	4340	0.41	0.66
	1500	0.025	3.18	6380		1.34
	2000	0.033	4.25	8687		2.19



ie business school

93%
OF MIM STUDENTS ARE
WORKING IN THEIR SECTOR 3 MONTHS
FOLLOWING GRADUATION

MASTER IN MANAGEMENT

- STUDY IN THE CENTER OF MADRID AND TAKE ADVANTAGE OF THE UNIQUE OPPORTUNITIES THAT THE CAPITAL OF SPAIN OFFERS
- PROPEL YOUR EDUCATION BY EARNING A DOUBLE DEGREE THAT BEST SUITS YOUR PROFESSIONAL GOALS
- STUDY A SEMESTER ABROAD AND BECOME A GLOBAL CITIZEN WITH THE BEYOND BORDERS EXPERIENCE

Length: 10 MONTHS
Av. Experience: 1 YEAR
Language: ENGLISH / SPANISH
Format: FULL-TIME
Intakes: SEPT / FEB

5 SPECIALIZATIONS
PERSONALIZE YOUR PROGRAM

#10 WORLDWIDE
MASTER IN MANAGEMENT
FINANCIAL TIMES

55 NATIONALITIES
IN CLASS

www.ie.edu/master-management | mim.admissions@ie.edu | [f](#) [t](#) [i](#) Follow us on IE MIM Experience

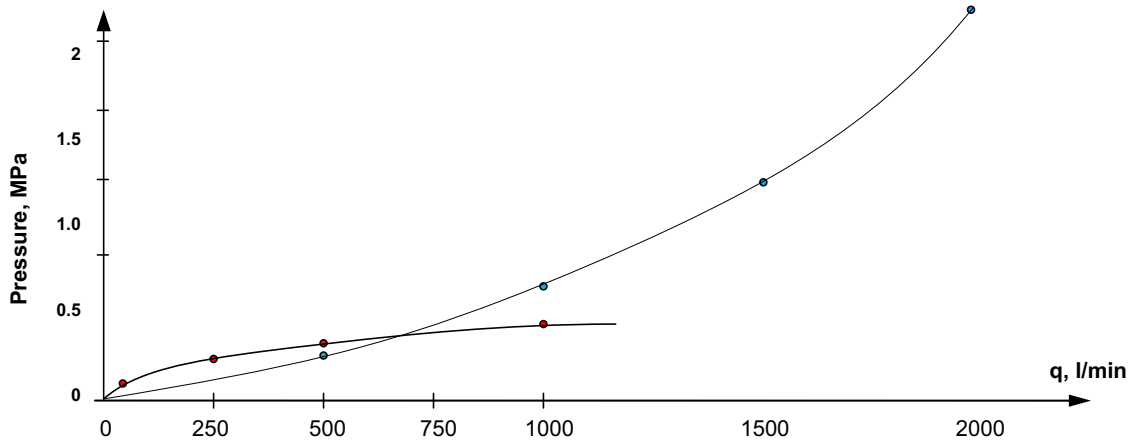


Figure 3-8b: Laminar and turbulent pressure loss.

3.9 PRESSURE LOSS. FIELD DATA - SOLUTION

Check first the solution at 5 spm. Then check for the remaining speeds. Here a check is made only for the 5 spm case. Here we think the flow is laminar. Pressure reading at 5 spm = 13 bars. To check theoretical D_p at 5 spm we go through these steps:

Step 1: Rheology: $n = 0.50$, $K = 1.63 \text{ Pas}^{-n}$

Step 2: Check flow regime: $N_{Re} = \frac{\rho v d}{\mu_{eff}}$

$$\mu_{eff,DP} = \left(\frac{8v}{d} \cdot \frac{3n+1}{4n} \right)^n \cdot \frac{Kd}{8v} = \left(\frac{8 \cdot 0.15}{0.105} \cdot \frac{3 \cdot 0.5 + 1}{4 \cdot 0.5} \right)^{0.5} \cdot \frac{1.63 \cdot 0.105}{8 \cdot 0.15} = 0.54 \text{ Pas}$$

$$\mu_{eff,Ann} = \left(\frac{12v}{d_o - d_i} \cdot \frac{2n+1}{3n} \right)^n \cdot \frac{Kd}{12v} = \left(\frac{12 \cdot 0.02}{0.188} \cdot \frac{2 \cdot 0.5 + 1}{3 \cdot 0.5} \right)^{0.5} \cdot \frac{1.63 \cdot 0.188}{12 \cdot 0.02} = 1.47 \text{ Pas}$$

$$v = \frac{q}{A}, \quad d = 4.127 \cdot 0.0254 = 0.105 \text{ m}$$

$$q = 15.29 \cdot 10^{-3} \cdot 5 = 0.0013 \text{ m}^3/\text{s}$$

$$A_{0p} = \pi/4 \cdot 0.105^2 = 0.0087 \text{ m}^2$$

$$A_{Ann} = (12.40^2 - 5^2) \cdot 0.0254^2 = 0.065 \text{ m}^2$$

$$v_{dp} = \frac{q}{A_{0p}} = 0.0013/0.0087 = 0.15 \text{ m/s}$$

$$v_{Ann} = \frac{q}{A_{Ann}} = 0.0013/0.065 = 0.02 \text{ m/s}$$

$$d_o - d_i = (12.4 - 5) \cdot 0.0254 = 0.188 \text{ m}$$

$$N_{Re,DP} = \frac{\rho \cdot d \cdot \bar{v}}{\mu_{eff}} = \frac{1120 \cdot 0.15 \cdot 0.105}{0.54}$$

= 32 (since it is so low it is assumed laminar also in the annulus)

Step 3: Find total pressure drop in flow system: $\Delta p = \Delta p_{dp} + \Delta p_{ann}$

$$\Delta p_{dp} = 32v\mu_{eff} \cdot \frac{L}{d^2} = 32 \cdot 0.15 \cdot 0.54 \cdot \frac{4500}{0.105^2} = 10.6 \cdot 10^5 Pa$$

$$\Delta p_{ann} = 48v\mu_{eff} \cdot \frac{L}{d_u^2} = 32 \cdot 0.02 \cdot 0.147 \cdot \frac{4500}{0.188^2} = 1.2 \cdot 10^5 Pa$$

$$\Delta p_{tot} = \Delta p_{dp} + \Delta p_{ann} = (10.6 + 1.2)10^5 = 11.8 \cdot 10^5 Pa$$

The task was to evaluate and compare the estimated pressure with the recorded pump pressure. As exemplified at 5 spm flow, the theory compared to reality, 11.8 vs. 13; it differed by -9 %. One possible explanation for this difference is that the theoretical Power law underestimates the real shear stress. Other error sources exist; selecting the correct rheology model for instance; fluid is very Binghamian. When does flow turn from laminar to turbulence? In real wells it turns turbulent earlier than theoretically predicted, due to high level of roughness and uneven annular flow path. Turbulent pressure loss is highly empirical.

3.10 PRESSURE LOSS. EFFECTS OF ROTATION - SOLUTION

During rotation of the pipe, external energy is added to the fluid (from the top drive). If the pipe is exposed to strict, controlled rotation the mud will be stirred (like in a viscometer). The mud is non-Newtonian and shear-thinning (for $n < 1.0$) during laminar flow. For laminar flow at SPM = 5, the friction loss will be reduced from 13 at pure flow to 8 bars at added rotation.

To check this fact we will try to estimate the reduction in effective viscosity. Assume the fluid behaves according to the Power-Law.

Step 1: Find $\bar{v}_{rot}$ = peripheral velocity of pipe. One rotation corresponds to the length $2\pi r$. The outer wall velocity is zero. Divide by 2 to obtain the average of the two extreme velocities:

$$v = \left(2\pi r \cdot RPM \cdot 1 \frac{min}{60} s + 0 \right) / 2 = 2\pi \cdot 5/2 \cdot 0.0254 \cdot \frac{100}{60} \cdot \frac{1}{2} = 0.33 m/s$$

Step 2: Translate the rotational velocity variation to shear rate:

$$\dot{\gamma} = \frac{12v}{d_o - d_i} \cdot \frac{2n+1}{3n} = \left(\frac{12 \cdot 0.33}{13.4 - 5} \cdot \frac{2 \cdot 0.5 + 1}{3 \cdot 0.5} \right) = 30 s^{-1}$$

Step 3: Calculate the shear rate caused by pure axial flow at 5 SPM: v_{ann} at 5 spm was found to be 0.02 m/s in the solution of Task 3.9 above.

$$\gamma = \frac{12v}{d_o - d_i} \cdot \frac{2n+1}{3n} = \left(\frac{12 \cdot 0.02}{13.4 - 5} \cdot \frac{2 \cdot 0.5 + 1}{3 \cdot 0.5} \right) = 1.5 \text{ s}^{-1}$$

Step 4: Effective viscosity: In Figure 3-10 the shear rate has been increased from 1.5 to additionally 30 s^{-1} (the two rates were assumed to be additive). We compare the effect of rotation in terms of changes in the Newtonian viscosity: Use the flow curve in Figure 3-10. Here we are left to assume the shear stress at these low shear rate values. From the rheological data in Task 2-2 we select the smallest recordable one, 3 Pa.

$$\mu_{5 \text{ spm}} = \tau / \gamma = 1 / 1.5 = 0.67 \text{ Pas}$$

$$\mu_{5 \text{ spm} + \text{rotation at 100 rpm}} = \tau / \gamma = 8 / (1.5 + 30) = 0.25 \text{ Pas}$$

We see that the effective viscosity has reduced to less than half of its original value at that flow rate. Note also that the shear stress seen from the pump (SPP) is not increased, it is “for free”, only the effective viscosity is decreased, as shown in Figure 3-10.



"I studied English for 16 years but...
...I finally learned to speak it in just six lessons"

Jane, Chinese architect

ENGLISH OUT THERE

Click to hear me talking before and after my unique course download

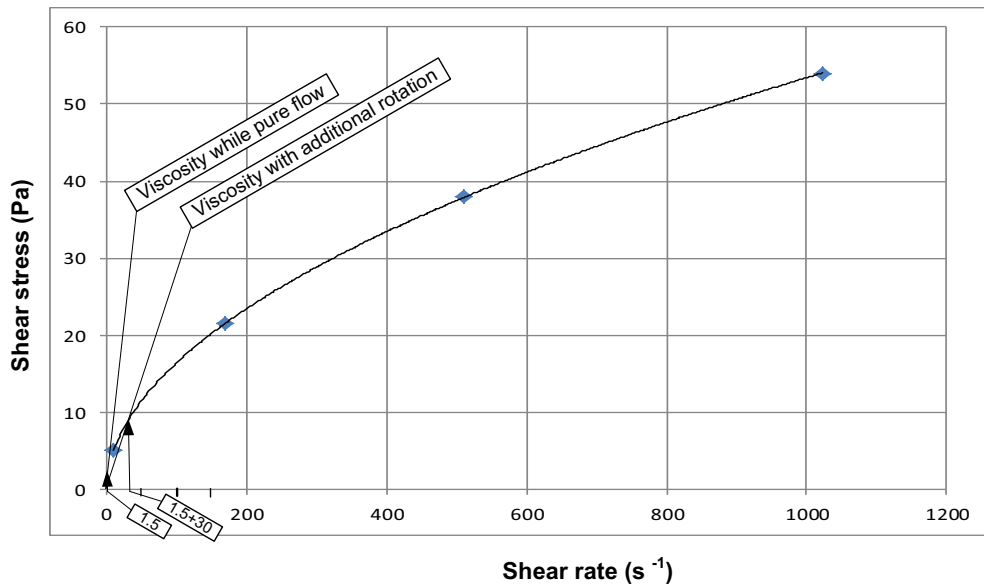
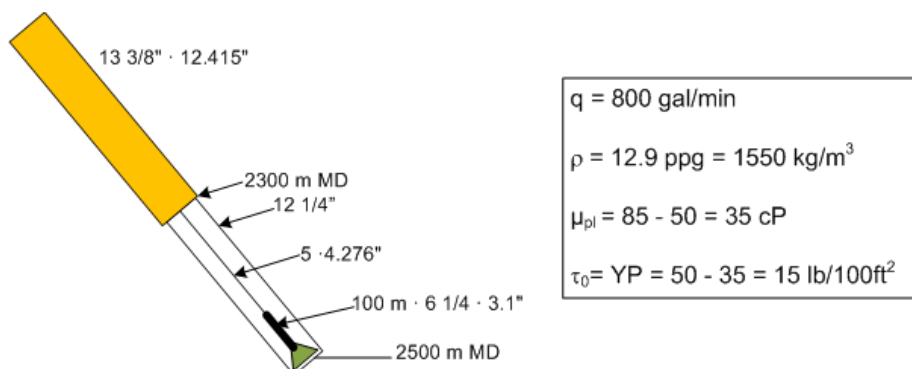


Figure 3-10: Effect of rotations on the rheology results in new ECD at the low shear stress of 10 Pa.

If the pipe is exposed to vigorous rotation and possibly vibrations, which often is the case in a real well, then additional turbulence will introduce **higher** pressure loss, not a lower one. However, at the highest pump speed (100 spm) flow is already turbulent and the complex motion of the drill string will therefore only negligibly influence the pressure.

3.11 PRESSURE LOSS. BIT NOZZLE. OFU - SOLUTION

The exercise information is summarized below:



- a) In order to estimate the annular pressure drop, both the mud velocity, the effective viscosity and the Reynolds number are needed, valid for the BHA-annulus, while drilling at a depth of 2500 m:

$$\bar{v} = \frac{q}{A} = \frac{q \cdot \frac{\text{Gal}}{\text{min}} \cdot \frac{0.1377 \text{ ft}^3 / \text{gal}}{60 \text{ s} / \text{min}}}{\frac{\pi}{4} d \left(\text{in} \cdot \frac{1}{12 \text{ in} / \text{ft}} \right)^2} = 0.40856 \frac{q}{d_h^2} = \frac{q}{2.448 d_h^2} = \frac{800}{2.448 (12.25^2 - 6.25^2)} \rightarrow 2.94 \text{ ft/s}$$

First check the flow regime before estimating Δp :

$$N_{\text{Re}} = \frac{757 \rho \bar{v} (d_2 - d_1)}{\mu_{\text{eff}}} = \frac{757 \cdot 12.9 \cdot 2.94 (12.25 - 6.25)}{\mu_{\text{eff}}} = 945 \Rightarrow \text{not turbulent}$$

$$\mu_{\text{eff}} = \mu_{\text{PL}} + \frac{5 \tau_y \cdot d_b}{\bar{v}} = 35 + \frac{5 \cdot 15 \cdot (12.25 - 6.25)}{2.94} = 179 \text{ cP}$$

$$\frac{\Delta p}{\Delta l_{\text{dc}}} = \frac{\mu_{\text{pl}} \cdot \bar{v}}{1000 (d_2 - d_1)^2} + \frac{\tau_y}{200 (d_2 - d_1)} = 0.0154 \text{ psi} / \text{ft} \Rightarrow 0.0154 \cdot \frac{100}{0.3048} = 5.05 \text{ psi}$$

Eqv. ρ in 2500 MD:

$$\rho_{\text{ekv}} = \rho + \frac{\Delta p_{\text{ann}}}{0.052 \cdot L} = 12.9 + \frac{5.05 + 100}{0.052 \cdot \frac{2500}{0.3048}} = 13.15 \text{ PPG}$$

- b) Bit pressure drop in OFU and in SI-units:

$$\Delta p_{\text{bit-OFU}} = \frac{8.311 \cdot 10^{-5} \cdot 12.9 \cdot 800^2}{0.95^2 \cdot \left(5 \cdot \frac{\pi}{4} \cdot \left(\frac{14}{32} \right)^2 \right)} = 1346 \text{ psi}$$

$$\Delta p_{\text{bit}} = 1.11 \cdot \frac{1}{2} \cdot 1550 \left[\frac{800 \cdot \frac{3.78533}{60 \cdot 1000}}{5 \cdot \frac{\pi}{4} \left(\frac{14}{32} \cdot 0.0254 \right)^2} \right]^2 = 9.318 \text{ MPa} = 1369 \text{ psi}$$

Conclusion: Choice of units does not make any difference for this formula.

- c) Total pressure loss in the system:

$$\text{DP: } \bar{v} = \frac{800}{2.448 \cdot 4.276^2} = 17.87 \text{ ft/s}$$

$$\text{DC: } \bar{v} = \frac{800}{2.448 \cdot 3.1^2} = 34.0 \text{ ft/s}$$

Turbulent or laminar in largest area?

$$N_{\text{Re}} = \frac{928 \rho \bar{v} d}{\mu_{\text{eff}}} = \frac{928 \cdot 12.9 \cdot 17.87 \cdot 4.276}{35 +} = 26136 \rightarrow \text{turbulent by far}$$

Pressure losses, turbulent:

$$\text{DP: } \Delta p_{\text{turb}} / \Delta l = \frac{\rho^{0.75} \mu_{\text{pl}}^{0.25} \bar{v}^{1.75}}{1800 d^{1.25}} = \frac{12.9^{0.75} \cdot 17.87^{1.75} \cdot 85^{0.25}}{1800 \cdot 4.276^{1.25}} = 0.29 \text{ psi} / \text{ft}$$

Total pressure loss in the circulating system (not all details shown):

$$\Delta p_{\text{tot}} = \Delta p_{\text{DP}} + \Delta p_{\text{dc}} + \Delta p_{\text{bit}} + \Delta p_{\text{ann1}} + \Delta p_{\text{ann2}}$$

$$\Delta p_{\text{tot}} = 2320 + 300 + 1346 + 5 + 100 = 4071 \text{ psi}$$

3.12 SWAB PRESSURE. CLINGING FACTOR - SOLUTION

Step 1. Make a detailed drawing. The clinging fluid is defined by R_{cling} in Figure 3-12, causing a certain volume to accompany the string upwards.

Step 2. Identify an expression of the fluid velocity profile with the correct boundary condition;

$$\begin{aligned} v(r)_{r=R_0} &= 0 \\ v(r)_{r=R_{cling}} &= 0 \\ v(r)_{r=R_i} &= v_p \end{aligned}$$

From the velocity profile we can obtain the cling volume pr. unit time:

$$q_{cling} = \int_{R_{cling}}^{R_i} v(r) 2\pi r dr$$

Step 3. Mass balance: $q_{up} = v_{pipe} \cdot A_{pipe} + q_{cling}$. An equivalent fluid mass has to move down

Step 4. Cling factor = q_{cling} / q_{down}

Excellent Economics and Business programmes at:



university of
 groningen




**“The perfect start
of a successful,
international career.”**

CLICK HERE
to discover why both socially
and academically the University
of Groningen is one of the best
places for a student to be

www.rug.nl/feb/education

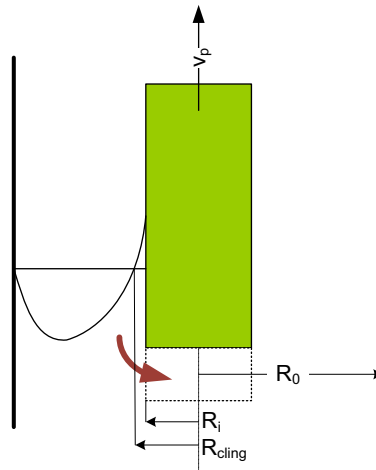


Figure 3-12: Flow streaming down the annulus when pulling a closed-end drill string upwards. The resulting frictional pressure loss causes a pressure deficit below the string's bottom end.

3.13 SWAB PRESSURE – SOLUTION

The V_{cling} will be added to the fluid volume displaced by the drill string.

$$q_{\text{DS}} = A_{\text{DS}} \cdot v_{\text{DS}}, v_{\text{displaced}} = q_{\text{DS}} / A_{\text{flow}}$$

$$V_{\text{total}} = V_{\text{pump}} - V_{\text{displaced}} - V_{\text{cling}}$$

Step 1. Understand the physics and forces. Make a Drawing

Step 2. Make a control box and enter exiting forces.

$$\Delta p \cdot \pi r^2 = \tau \cdot 2\pi r \Delta L$$

$$\Delta p / \Delta L \cdot r = 2\tau$$

Step 3. Differentiate: $\Delta p / \Delta L \cdot dr = 2 d\tau$

Step 4. Integrate over the control volume (along r)

4 HYDRAULIC PROGRAM – SOLUTION

4.1 MUD PUMP ISSUES – SOLUTION

a) Characteristic diagrams of mud pumps are shown in Figure 4-1:

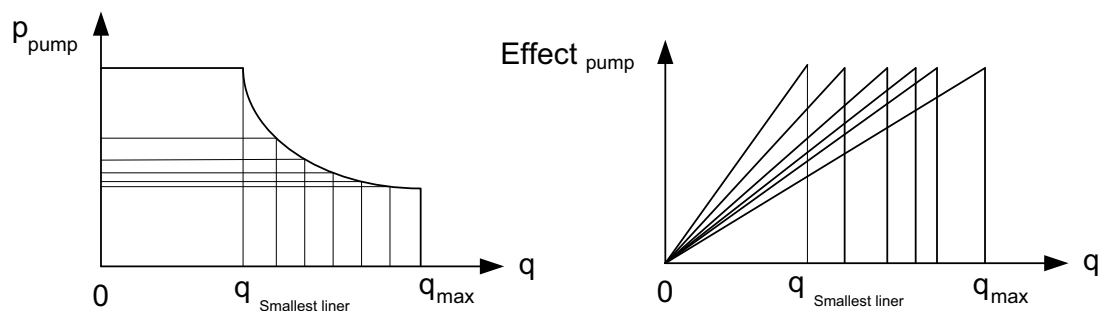


Figure 4-1: Maximum pump pressure for each liner (left) and maximum effect for the same liners (right)

Power or effect = $E = p \cdot q$, is expressed in Horse Power (HP) or in watt (W). As shown in Figure 4-1 (to the right) the maximum effect is constant for all liners

Volumetric efficiency = 0.96 for new pumps. When it has reduced to 0.93 the pump has to be upgraded (replace valves and / or piston / liner)

- Optimize the pumps in parallel $\rightarrow$ higher q ; used for upper wellbore sections. Coupled in series $\rightarrow$ higher p (only for very special application, not done for mud pumps).
- Centrifugal pumps can deliver high flow rate but limited pressure (max 3 bars) since there is an open slot between statot and rotor.
- Knocking is a result of too high acceleration. At the highest acceleration the water is not able to fully follow the high acceleration, and the following takes place: $\rightarrow$ vacuum effect $\rightarrow$ vapor pressure is surpassed and water starts boiling (vapor bubbles are formed on the steel surface) $\rightarrow$ implosion of vapor bubbles during retardation of piston movement $\rightarrow$ repeated shock waves weakens the steel.
- Find first $\Delta p_d = \Delta p_p - \Delta p_{bit}$

Bit pressure loss can be determined since nozzle sizes are known:

$$p_{bit} = 1.11 \frac{1}{2} \rho v^2 = 1.11 \cdot \frac{1}{2} \cdot 1300 \cdot 100^2 = 72.15 \cdot 10^5 \text{ Pa}$$

$$\bar{v} = q / A_{nozzle}$$

$$A_{nozzles} = (\pi/4) d_e^2 = \pi/4 \cdot 0.0206^2 = 3.3333 \cdot 10^{-4} \text{ m}^2$$

$$d_e = \sqrt{d_1^2 + d_2^2 + d_3^2} = \sqrt{3} \cdot d_1 = \sqrt{3} \cdot \frac{15}{32} \cdot 0.0254 = 0.0206 \text{ m}$$

$$q_1 = 2500 / (1000 \cdot 60) = 0.04167 \text{ m}^3/\text{s} \quad v_1 = q_1 / A = 0.04167 / 3.33 \cdot 10^{-4} = 125.2 \text{ m/s}$$

$$q_2 = 670 / (1000 \cdot 60) = 0.011 \text{ m}^3/\text{s} \quad v_2 = q_2 / A = 0.011 / 3.33 \cdot 10^{-4} = 33.5 \text{ m/s}$$

Resulting in these values:

Parameter	q	p _p	Δp _{bit}	Δp _d
Unit	lpm	bar	bar	bar
Data	2500	230	72	157.9
	670	33	8.1	24.9

K_1 and m are determined from: $\Delta p_d = K_1 D q^m$. Selecting the operator $\ln$ or $\log$ does not make any difference here.

$$m = \ln (\Delta p_{d1} / \Delta p_{d2}) / \ln (q_1 / q_2) = \ln (157.9 / 24.9) / \ln (2500 / 670) = 1.6$$

$$K_1 = \Delta p_d / q^m \cdot D = 157.9 \cdot 10^5 / (0.04167^{1.69} \cdot 2500) = 2 \cdot 10^6$$

American online LIGS University

is currently enrolling in the
Interactive Online **BBA, MBA, MSc,**
DBA and PhD programs:

- ▶ enroll **by September 30th, 2014** and
- ▶ **save up to 16%** on the tuition!
- ▶ pay in 10 installments / 2 years
- ▶ Interactive Online education
- ▶ visit www.ligsuniversity.com to
find out more!

Note: LIGS University is not accredited by any
nationally recognized accrediting agency listed
by the US Secretary of Education.
More info [here](#).



4.2 NOZZLE SELECTION. SECTION WISE – SOLUTION

- a) Existing parasitic pressure loss and its parameters (assume 3 identical nozzles):

$$d_e = \sqrt{d_1^2 + d_2^2 + d_3^2} = \sqrt{3} \cdot d_1 = \sqrt{3} \cdot \frac{15}{32} \cdot 0.0254 = 0.0206 \text{ m}$$

$$v_{nozzle,1} = \frac{q}{A} = \frac{2000}{1000 \cdot 60 \cdot \frac{\pi}{4} \cdot 0.0206^2} = \frac{0.0333}{0.000333} = 100.2 \text{ m/s}$$

$$v_{nozzle,2} = 87.7 \text{ m/s}$$

$$p_{bit1} = 1.11 \cdot 1/2 \cdot 1400 \cdot 100^2 = 78 \cdot 10^5 \text{ Pa} / 59.8 \cdot 10^5 \text{ Pa} \text{ (represents pump rate 1/rate 2)}$$

$$\Delta p_{loss} = 186 - 121.8 = 108.2 \text{ bar}$$

$$\Delta p_{loss} = 120 - 59.8 = 60.2$$

$$\Delta p_{loss} = K_1 D \cdot q^m$$

$$m = \frac{\log(\Delta p_{loss1} / \Delta p_{loss2})}{\log(q_1 / q_2)} = \frac{\log(108.2 / 60.2)}{\log(2500 / 1750)} = 1.64$$

$$K_1 = \frac{108.2 \cdot 10^5}{2500 \cdot 0.0333^{1.64}} = 1.16 \cdot 10^6$$

- b) From existing hydraulic program we obtain:

$$q_{opt} = [2p_{pump,m} / (m+2) K_1 D]^{1/m} = [2 \cdot 270 \cdot 10^5 (1.64+2) \cdot 1.16 \cdot 10^6 \cdot 3 \cdot 0.000]^{1/1.64} = 0.0043^{0.61} = 0.0358 \text{ m}^3/\text{s}$$

Check the flow rate at the boundary conditions (in SI-units to be able to compare):

$$q_{max,p} = 2700 \text{ lpm} = 2700 / (1000 \cdot 60) = 0.045 \text{ m}^3/\text{s}$$

$$q_r = 1700 / (1000 \cdot 60) = 0.028 \text{ m}^3/\text{s}$$

$$q_{max,ann} = 2600 / 60000 = 0.0433 \text{ m}^3/\text{s}$$

Since q_{opt} is in between q_r and $q_{max,ann}$, 0.0358 is the optimal solution at this depth.

- c) The optimal bit pressure loss is given by this equation:

$$\Delta p_{bit} = p_{max,p} \cdot m / (m + 2) = 0.458 \cdot 270 \cdot 10^5 \cdot 1.64 / (3.64) = 121.6 \cdot 10^5 \text{ Pa}$$

To find the optimal nozzle, solve pressure drop equation vs. optimal bit pressure drop:

$$1.11 \cdot \frac{1}{2} \rho \left(\frac{q_{opt}}{\frac{\pi}{4} d_e^2} \right)^2 = 121.6 \cdot 10^5 \text{ Pa}$$

$$d_e^4 = \frac{1.11 \cdot 0.5 \rho \cdot q^2}{\left(\frac{\pi}{4} \right)^2 \cdot 121.6 \cdot 10^5}$$

$$d_e^4 = \sqrt[4]{\frac{1.11 \cdot 0.5 \cdot 1400 \cdot 4^2 \cdot 0.0358^2}{\pi^2 \cdot 121.6 \cdot 10^5}} = 0.019 \text{ m}$$

Nozzle diameter is not optimal at 3000 meters depth but close to. It should have been:

$$d_{SI} = \frac{d_e}{\sqrt{3}} = \frac{0.019}{\sqrt{3}} \Rightarrow d_{OFU} = \frac{0.019}{\sqrt{3}} \cdot \frac{32}{0.0254} = 0.011 \cdot \frac{32}{0.0254} = 13.9 \text{ (32nds in)}$$

To stay below maximum pump pressure we select:

$$14/32", 14/32", 14/32"$$

4.3 LINER SELECTION. SECTION WISE – SOLUTION

- a) To optimize q_{opt} you need criteria; maximize ROP. First find a suitable expression of ROP:

$$ROP = A \cdot (q/d_{nozzle})^{0.8}$$

Further we need to know the boundaries:

$$p_p = \Delta p_{loss} + \Delta p_{bit}$$

$$p_p = K_1 D q^m + K_{bit} \cdot \left(\frac{q}{d_e}\right)^2 \rightarrow$$

$$p_p = K_1 D q^m + K_{bit} \cdot \left(\frac{q}{d_e}\right)^2 \cdot q^2$$

$$p_p \cdot q^2 = K_1 D q^{m+2} + K_{bit} \cdot \left(\frac{q}{d_e}\right)^2 q^2$$

$$\frac{q}{d_e} = (p_p^2 - K_1 D q^{m+2})^{0.5} \cdot \frac{1}{K_{bit}^{0.5}}$$

Entering the expression of q/d into the ROP expression, differentiate and find maximum (at $dROP/dq = 0$), result in an optimal expression:

$$2p_p q - K_1 D(m+2)q^{m+1} = 0$$

- b) In order to cover the complete range of possible flow rates, we see from the data and the pump characteristics that the 6 3/4" liner has a q_{max} of 0.0422. Only this liner is large enough to supply the q_{max} of 0.04 m³/s if necessary. Intuitively we would select the smallest liner possible, the 5 1/2 ", since it has the highest available pressure. This is what we also recommend. Alternatively we will check what optimal flow rate each liner produce at this depth:

$$q_{opt5.5} = \left[\frac{2(p_p)_m}{K_1 \cdot D(m+2)} \right]^{\frac{1}{m}} = \left[\frac{2 \cdot 383 \cdot 10^5}{1.6 \cdot 10^6 \cdot 2500(1.7+2)} \right]^{\frac{1}{1.7}} = 0.0454 \text{ m}^3 / \text{s}$$

$$q_{opt6} = \left[\frac{2(p_p)_m}{K_1 \cdot D(m+2)} \right]^{\frac{1}{m}} = \left[\frac{2 \cdot 322 \cdot 10^5}{1.6 \cdot 10^6 \cdot 2500(1.7+2)} \right]^{\frac{1}{1.7}} = 0.0405 \text{ m}^3 / \text{s}$$

$$q_{opt6.5} = \left[\frac{2(p_p)_m}{K_1 \cdot D(m+2)} \right]^{\frac{1}{m}} = \left[\frac{2 \cdot 274 \cdot 10^5}{1.6 \cdot 10^6 \cdot 2500(1.7+2)} \right]^{\frac{1}{1.7}} = 0.0369 \text{ m}^3 / \text{s}$$

$$q_{opt7.5} = \left[\frac{2(p_p)_m}{K_1 \cdot D(m+2)} \right]^{\frac{1}{m}} = \left[\frac{2 \cdot 220 \cdot 10^5}{1.6 \cdot 10^6 \cdot 2500(1.7+2)} \right]^{\frac{1}{1.7}} = 0.0324 \text{ m}^3 / \text{s}$$

We observe that the optimal flow rate is outside the boundaries for 5.5, 5.75 and 6. We could claim that the 6.5 " liner is the smallest liner with its optimum within the range and therefore select that one.

An expression of optimal bit pressure is found from the same optimal solution as above. Substitute $p_d = K_1 D q^m$:

$$2p_p - (m+2)p_d = 0$$

$$2p_p - (m+2)(p_p - p_{bit}) = 0$$

Optimum bit pressure drop is thus: $\rightarrow p_{bit} = \frac{m}{m+2} p_p$

From pump data of 6" liner we read: $p_{pump, max} = 322 \cdot 10^5 \text{ Pa}$

$$p_{bit,opt} = \frac{1.7}{3.7} \cdot 322 \cdot 10^5 \text{ Pa} = \underline{150 \cdot 10^5 \text{ Pa}}$$

- c) The depth of when to alter the liner is found when of the 6" liner reaches the $q_{\max}$ of liner 5 3/4". This is $0.0307 \text{ m}^3/\text{s}$

$$\left[\frac{2(p_p)_{\max}}{K_1 \cdot D(m+2)} \right]^{\frac{1}{m}} = 0.0307 \Rightarrow K_1 \cdot D(m+2) = \frac{2(p_p)_{\max}}{(0.0307)^m}$$

$$D = \frac{2(p_p)_{\max}}{K_1 \cdot (m+2)(0.0307)^m} = (2 \cdot 322) / [1.6 \cdot 10^6 \cdot (3.7 \cdot (0.0307)^{1.7})] = 3841 \text{ m}$$

4.4 HYDRAULIC PROGRAM. SECTION WISE – SOLUTION

- a) By including all the variables in the ROP equation we might succeed.

$$ROP = A(q/d_e)^{a_8}$$

$$p_p = \Delta p_{\text{loss}} + \Delta p_{\text{bit}}$$

$$p_p = K_1 D q^m + 1.11 \cdot 0.5 \rho \left(\frac{q}{d_e^2} \right)^2 \cdot \frac{1}{(\pi/4)^2} \rightarrow k_{\text{bit}} = 1.11 \cdot 0.5 \cdot \rho / (\pi/4)^2$$

$$p_p = K_1 D q^m + k_{\text{bit}} \cdot \left(\frac{q}{d_e^2} \right)^2 \rightarrow \frac{q}{d_e} = (p_p - k_1 D q^m)^{0.5} \cdot \frac{1}{k_{\text{bit}}^{0.5}}$$

$$\text{Substitute into the ROP equation: } ROP = A \left[(p_p - k_1 D q^m)^{0.5} \cdot \frac{1}{k_{\text{bit}}^{0.5}} \right]^{a_8} = \left(\frac{1}{k_{\text{bit}}^{0.5}} \right)^{a_8} \cdot A \cdot (p_p - k_1 D q^m)^{0.5 a_8}$$

DON'T EAT YELLOW SNOW

What will
your advice
be?

Some advice just states the obvious.

But to give the kind of advice that's going to make a real difference to your clients you've got to listen critically, dig beneath the surface, challenge assumptions and be credible and confident enough to make suggestions right from day one. At Grant Thornton you've got to be ready to kick start a career right at the heart of business.



Grant Thornton

An instinct for growth™

Sound like you? Here's our advice: visit
GrantThornton.ca/careers/students

Scan here to learn more about a career with Grant Thornton.



© Grant Thornton LLP. A Canadian Member of Grant Thornton International Ltd

From this equation we see that for increasing depth the ROP-function will decrease.

- b) Only the case of vertical wells is presented here. The horizontal case is solved identically, only the flow rate has higher importance / higher upper boundaries. Within the narrow flow rate interval for vertical wells, the 6 ¼" liner covers the maximum flow rate. First check what is the optimum flow rate for each of the liners, from 6 ¼" and downwards at 1 950 mMD. Since the boundary conditions do not change with depth, intuitively we would suggest that the smallest liner possible should be selected, which we do; the 5 ½" liner. Just for curiosity we also check the optimal flow rate at the two depths:

$$q_{opt,1950,5.5"} = \left[\frac{2 \cdot \Delta p_p}{(m+2)K_1 D} \right]^{1/m} = \left[\frac{2 \cdot 383 \cdot 10^5}{(1.65 + 2)2 \cdot 10^6 \cdot 1950} \right]^{1/1.65} = 0.0418 \text{ m}^3/\text{s}$$

$$ROP = C \cdot BHHP = \frac{c}{1714} \cdot \Delta p_{bit} \cdot q = c_1(p_p - \Delta p_{loss}) \cdot q$$

We observe that when drilling at 4 000 m the hydraulic program is inside the theoretical limits, but not while drilling at 1 950 m. Our suggestion is therefore to use the q_{max} , 0.028, until a depth at which q_{opt} is reached:

$$D = \frac{2 \cdot \Delta p_p}{(m+2) K_1 q^m} = \frac{2.383 \cdot 10^5}{(1.65 + 2) 2 \cdot 10^6 \cdot 0.028^{1.65}} = 3\,829 \text{ m}$$

Then use q_{opt} till TD. If change of liner is allowed with increasing depth, then a better solution is to select the liner corresponding to optimum flow rate.

4.5 OPTIMAL PARAMETERS WITH BHHP. OFU. SECTION WISE – SOLUTION

Optimum parameters for this criterion can be derived as follows:

$$ROP = C \cdot BHHP = \frac{c}{1714} \cdot \Delta p_{bit} \cdot q = c_1(p_p - \Delta p_{loss}) \cdot q$$

$$ROP = c_1(p_p \cdot q - K_1 D q^m \cdot q)$$

Only the derivation of the core of the above expression produces a sensible answer.

$$\frac{dROP}{dq} = p_p - (m+1)K_1 D q^m = 0$$

$$\Delta p_{p,opt} = (m+1)K_1 D q^m \Rightarrow q_{opt} = \left[\frac{p_p}{(m+1) \cdot K_1 D} \right]^{1/m}$$

We observe also that optimal parasitic and bit pressure drop can be derived from the equation above:

$$\Delta p_{loss} = p_p \frac{1}{m+1}, \quad \Delta p_{bit,opt} = \frac{m}{m+1} p_p$$

To estimate q_{opt} , $K_1 D$ and m must first be determined from: $\Delta p_{loss} = K_1 D q^m$

Input		Output	
q (GPM)	p _p (psi)	Δp _{bit} (psi)	Δp _d (psi)
500	3 000	2 097.0	903.0
250	800	524.3	275.7

$$m = \frac{\ln(\Delta p_{loss1}/\Delta p_{loss2})}{\ln(q_1/q_2)} = \frac{\ln(903/275.7)}{\ln(500/250)} = 1.712$$

$$K_1 D = \Delta p_{loss}/q^m = \frac{903}{500^{1.712}} = 0.02168 \text{ (psi/GPM}^m\text{)}$$

Now q_{opt} can be found (note that the units are correct):

$$q_{opt} = \left[\frac{\Delta p_{p,max}}{(m+1)K_1 D} \right]^{1/m} = \left[\frac{3620}{(1.71 + 1) 0.0217} \right]^{1/1.712} = 627 \text{ GPM}$$

Including the volumetric efficiency factor, e_{vol} , the practical q_{opt} is:

$$q_{opt} = 627 \cdot 0.9 = 564 \text{ GPM}$$

Now the bit nozzles can be estimated from $Dp_{bit,opt} = Dp_{bit}$:

$$\frac{m}{m+1} \cdot p_{p,max} = 8.311 \cdot 10^{-5} \cdot \rho \cdot q^2 / C_d^2 \cdot A_{nozzle}$$

$$A_{nozzle,opt} = \sqrt{\frac{8.311 \cdot 10^{-5} \cdot \rho q_{opt}^2}{C_d^2 \cdot \Delta p_{bit}}} = \sqrt{\frac{8.311 \cdot 10^{-5} \cdot 564^2}{0.95^2 \cdot 2284}} = 0.33 \text{ in}^2$$

$$p_{bit,opt} = \frac{m}{m+1} \cdot 3620 = \frac{1.71}{1.71+1} \cdot 3620 = 2284 \text{ psi}$$

Finally the area can be expressed as:

$$A = \sqrt{3} \cdot \frac{\pi}{4} \left(\frac{d_e}{32} \right)^2 \rightarrow d_e^2 = \frac{A \cdot 4 \cdot 32^2}{\pi \sqrt{3}} \rightarrow$$

$$d_e = \sqrt{\frac{0.33 \cdot 4 \cdot 32^2}{\sqrt{3} \cdot \pi}} = x \text{ (32nd in)}$$

Assume $x = 15.8 \rightarrow 16/32''$, $16/32''$, $16/32''$

Assume $x = 16.8 \rightarrow 16/32''$, $17/32''$, $17/32''$

4.6 LINER SELECTION. COMPLETE WELL – SOLUTION

- a) Optimal flow rate in pump range II is derived initially from Exercise 4.4.

$$ROP = K \cdot \left(\frac{q}{d_{nozzle}} \right)^{a_8} = \frac{K}{K_{bit}} (p_p q^2 - K_1 D \cdot q^{m+2})^{\frac{a_8}{4}}$$

In this equation we substitute $q \cdot p = E$

$$ROP_{II} = \frac{K_a}{K_{bit}} (p_{max} \cdot q^2 - K_1 D \cdot q^{m+2})^{a_8/4} = K' (E_p \cdot q - K_1 D q^{m+2})^{a_8/4}$$

$$\frac{\partial ROP_{II}}{\partial q} = \frac{K' (E_p - (m+2) K_1 D q^{m+1})^{\frac{a_8}{4}}}{\left(\right)^{\frac{a_8}{4} - 1}} = 0 \quad q_{opt,II} = \left[\frac{E_p}{K_1 \cdot D (m+2)} \right]^{\frac{1}{m+1}}$$

- b) Range II stops to exist when flow rate is decreasing and reaches $q_{opt,II} = q_{5,5'',max}$, while range I stops at increasing flow rates, when $q_{opt,I} = q_{5,5'',max}$.

$$q_{opt,II} = \left(\frac{E_p}{K_1 D (m+2)} \right)^{1/(m+1)} \Rightarrow D_{II} = 1852 \text{ m}$$

$$q_{opt,I} = \left(\frac{2p_p}{(m+2)K_1 D} \right)^{1/m} = \left(\frac{2 \cdot 383 \cdot 10^5}{3.5 \cdot 2.20 \cdot 10^6 \cdot D} \right)^{1/1.5} = 0.028 \Rightarrow D_I = 2123 \text{ m}$$

- c) The graphical solution speaks for itself:

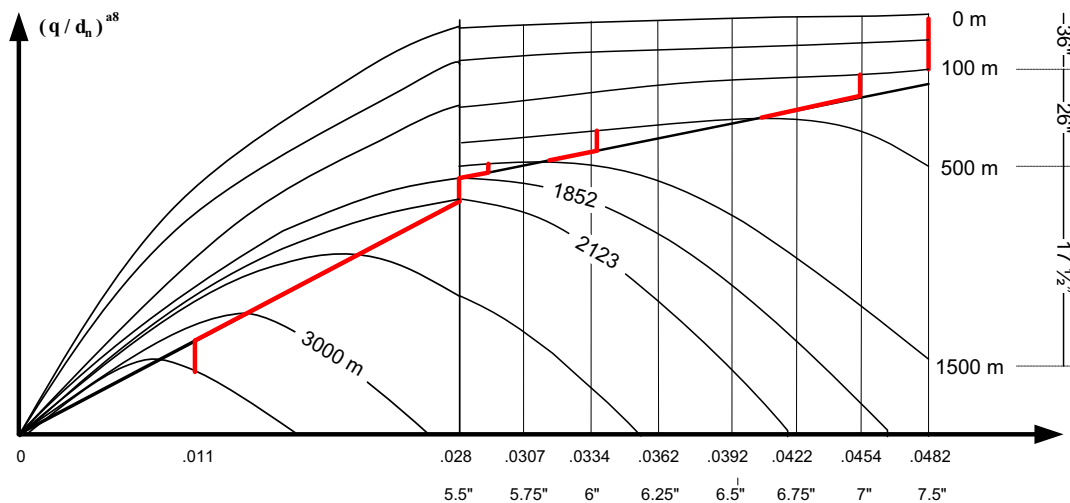


Figure 4-6: Graphical solution.

- d) From Table 4-6 in the Task section above we can see that at a depth between 1 500 and 3 000 m there are two potential options. However, from Figure 4-6 above we already know that while drilling past 1 852 m we enter pump range I, and starts applying the 5 ½ “ liner. We also see that the maximum flow rate of the 5 ½” liner is the optimum one for most of its operational time. This has already been shown in task b) above.

4.7 LINER SELECTION. COMPLETE WELL – SOLUTION

- a) Find first which working area prevails in the boundary zone between pump area II and I, which are valid as indicated in Figure 4-7.1. Area II ends with the 5.75" liner when $q_{\max, 5.5}$ is reached:

$$q_{opt,II} = 0.028 = \left[\frac{E}{K_1 D(m+2)} \right]^{1/(m+1)} = \left[\frac{1.076 \cdot 10^6}{1.72 \cdot 10^6 \cdot D \cdot 3.52} \right]^{1/2.52} = D_{II-I} = 1457 \text{ m}$$

At 1 457 m depth the pump area I is entered, coming from II. From the pump chart we note that 5 1/2" liner has $p_{\max} = 383$ bar. Solving $q_{opt,I}$ eqn. for D we find where $q_{opt,I}$ starts.

$$q_{opt,I} = 0.028 = \left[\frac{2p_p}{K_1 D(m+2)} \right]^{1/m} = \left[\frac{2 \cdot 383 \cdot 10^5}{1.72 \cdot 10^6 \cdot D \cdot 3.52} \right]^{1/1.52} \Rightarrow D_{I-opt} = 2900 \text{ m}$$

- b) In Figure 4-7.1 we see the division between the two pump areas. A preliminary solution of how to distinguish between them is given in Figure 4-7.2, its upper part.



e-learning for kids

- The number 1 MOOC for Primary Education
- Free Digital Learning for Children 5-12
- 15 Million Children Reached

About e-Learning for Kids Established in 2004, e-Learning for Kids is a global nonprofit foundation dedicated to fun and free learning on the Internet for children ages 5 - 12 with courses in math, science, language arts, computers, health and environmental skills. Since 2005, more than 15 million children in over 190 countries have benefitted from eLessons provided by EFK! An all-volunteer staff consists of education and e-learning experts and business professionals from around the world committed to making difference. eLearning for Kids is actively seeking funding, volunteers, sponsors and courseware developers; get involved! For more information, please visit www.e-learningforkids.org.

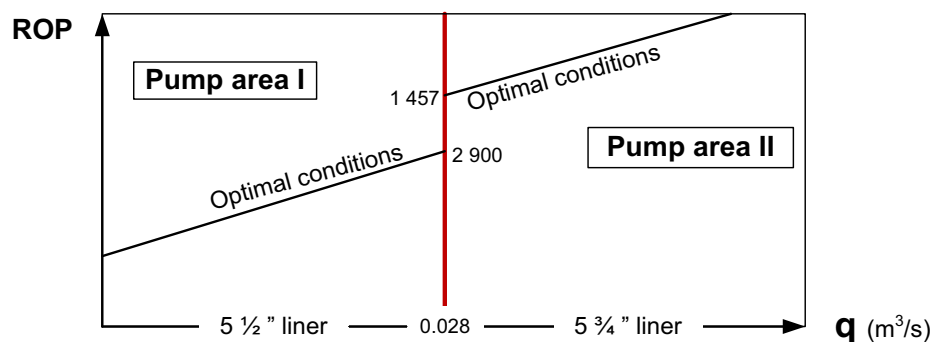


Figure 4-7.1: Boundary area between pump area II and I.

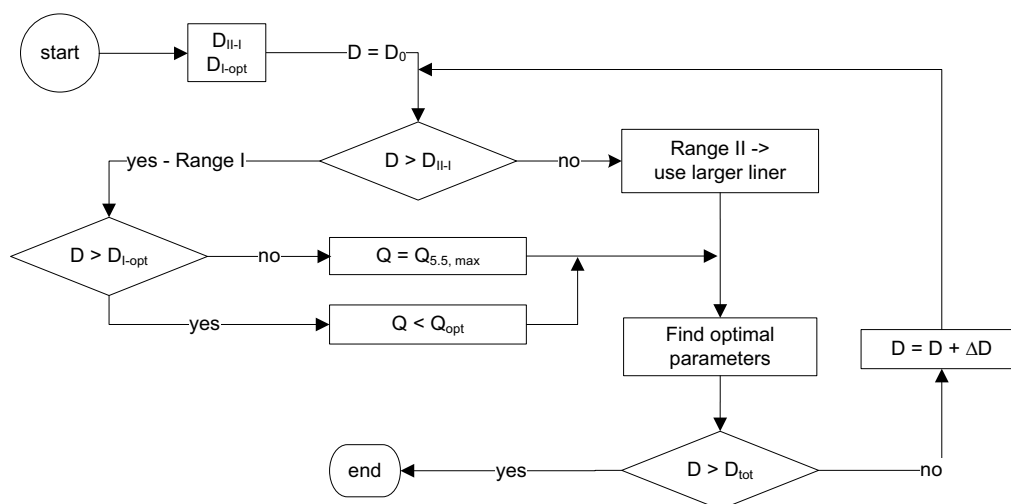


Figure 4-7.2: Flow chart of estimating hydraulic parameters while in the boundary zone between the two pump areas.

5 WELLBORE CHALLENGES – SOLUTIONS

5.1 FLUID PROPERTIES - SOLUTIONS

5.1.1 FILTRATION CONTROL – SOLUTION

- a) Fluid loss can be optimized in three ways:
 1. Ensure a good filter in the wellbore wall by including a wide range of particles in the mud (Bentonite, Barite and cuttings are already there. It may be enough)
 2. Ensure a good filter cake by making sure the mud is dispersed
 3. Losses through the filter cake in WBM are treated by increasing the viscosity of the fluid phase. Use starch, CMC and sodium polyacrylate. OBM rarely requires such additives
- b) Increased fluid loss is detected through filter press tests. Depending on the fluid loss, its rheology and other test results, you normally find out which of the 3 qualities in question a) above are the problem. See more details in the Textbook Chapter 2.
- c) Filtrate will lead to approximately the same invasion depth (typically 3 feet). Particles will invade both sands typically 1 ft, assuming the particle size distribution of the added or the existing particles in the mud covers at least the range of $1/7^{\text{th}}$ to $1/3^{\text{rd}}$ of the pore size distribution. That assumption is normally fulfilled through the presence of Bentonite / polymers + Barite + cuttings.
- d) Water-flow into the shale can be lowered by
 1. Increasing the viscosity of the fluid phase
 2. Establishing a filter; same principles as in c) above

5.2 FILTRATION CONTROL – SOLUTION

- a) Standard fluid loss = filtrate volume in ml after 30 min

$$V_f = AC \cdot \sqrt{t}$$

$$\text{API filter press } A_1 = 45 \text{ cm}^2 = 45 \cdot 10^{-4} \text{ m}^2$$

Flow into porous formation:

$$\text{Effective formation height (10 \%)} h = 4000 \text{ ft} \cdot 0.3048 \cdot 0.10 = 122 \text{ m}$$

$$\text{Wellbore surface area } A_2 = \pi \cdot d \cdot L = 15 \cdot 0.0254 \cdot \pi \cdot 122 = 149 \text{ m}^2$$

Assuming that an identical filter is built up on the sandstone surface, the loss during the first 30 minutes can be estimated:

$$\frac{V_{f_2}}{V_{f_1}} = \frac{A_2}{A_1}$$

$$V_{f_{2,0.5}} = V_{f_1} \cdot \frac{A_2}{A_1} = 25 \cdot 10^{-6} \cdot \frac{149}{45 \cdot 10^{-4}} = 0.83 \text{ m}^3$$

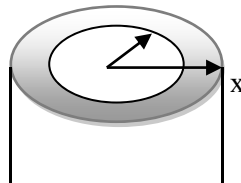
$$V_{f_{2.24}} = V_{f_{2,0.5}} \cdot \frac{\sqrt{24}}{\sqrt{0.5}} = 0.83 \cdot 6.93 = 5.74 \text{ m}^3$$

The filter will have the same progress and the same constants.

- b) Intrusion after 24 h with 100 % displacement of 5.74 m³. Since only the pores are invaded, the affected volume to be invaded will be accordingly larger.

$$\text{Affected volume} = V_{eff} = \frac{V_f}{0.15}$$

$$\text{Hole radius: } r_{hole} = \frac{15}{2} \cdot 0.0254 = 0.19 \text{ m}$$



.....Alcatel-Lucent 

www.alcatel-lucent.com/careers

What if you could build your future and create the future?

One generation's transformation is the next's status quo. In the near future, people may soon think it's strange that devices ever had to be "plugged in." To obtain that status, there needs to be "The Shift".

Effectuated or invaded volume can be expressed by means of the radius, $r_{invaded}$

$$V_{eff} / \emptyset = (\pi \cdot r_{invaded}^2 - \pi \cdot r_{hole}^2) \cdot h$$

$$\pi \cdot r_{invaded}^2 \cdot h = V_{eff} / \emptyset + \pi \cdot r_{hole}^2 \cdot h$$

$$R_{inv} = \sqrt{(V_{eff} / \emptyset + \pi \cdot r_{hole}^2) \cdot 1 / (\pi h)}$$

$$R_{inv} = \sqrt{5.74 / 0.15 + \pi \cdot 0.59^2 - 122} / (\pi \cdot 122) = 0.369 \text{ m (which is around 1 ft)}$$

c) Obtain knowledge of the sandstone's pore size distribution. Apply:

- Particles in the mud with a mean size = 1/3 of the pore size.
- Colloidal particles must be dispersed.
- Base fluid viscosity can be increased.
 - For OBM the particle distribution is mainly taken care of by emulsified water droplets, with a wide droplet distribution.
 - Follow up by making a filter press test every 30 min. In case filter loss increases, every bullet point above must be evaluated through more tests, viscosity especially and specific countermeasures are set in motion.
 - Filter test is important mainly to obtain a thin and tight filter cake to avoid stuck. Secondly, while drilling in the reservoir, to minimize fm-damage.
- Filter loss is increasing because we are drilling through contaminants like salt, chalk, etc., which are causing flocculation; resulting in thick filter cake and perhaps in stuck pipe. Solution/explanation: Add thinners/-dispersants/deflocculators.

If massive attack; dump the returning mud.

5.3 CUTTINGS CONCENTRATION I – SOLUTION

- a) At the end of the horizontal section the cuttings concentration would also be close to 0.02. A bed has been established which is in equilibrium between erosional and depositional forces. The bed height is a result of the steady state process; settling and lifting of cuttings is a function of flow rate, ROP, etc. The bed height can be estimated theoretically. We select not to do that, but rather assume that a certain % of the generated cuttings are left behind in the wellbore. E.g. 10 % of the wellbore cross sectional area is in average filled by cuttings. This means 10 % of what is drilled out is left in the newly drilled well. The initial concentration is accordingly reduced by 10 %;

$$c_2 = c_1 \cdot (1 - 0.1) = 0.2 \cdot 0.9 = 0.018$$

- b) In the vertical section the concentration will increase due to the vertical slipping of cuttings, expressed through the transport ratio R_t . This could have been estimated through Stokes Law. We select here just to assume a typical value of R_t , like 0.75. We then have:

$$c_3 = c_2 / R_t = 0.018 / 0.75 = 0.024$$

- c) The cuttings removal forces are opposed by gravity and cohesive forces. Gravitational forces are given by Stokes law. Removal forces are given by drag and lift forces. The drag force is a function of particle Reynolds number and sphericity. The drag and lift forces can be developed into the critical lift velocity or rolling velocity. String-RPM will induce a drag force onto the cuttings, referred to as the viscous coupling. At a given cuttings feed-rate, a stationary bed height will form as a function of the equilibrium state between all involved input variables, some eroding, some building.
- d) Here the bed height will be higher due to higher cross sectional area and thus lower fluid velocity, assuming the entrance effects (into and out of the enlargement) do not ruin this assumption. Settling rate will increase, but first after the entrance effects are passed. When the BHA, during tripping, is shoveling much cuttings into a narrower wellbore it is easy to imagine that the BHA may become jammed.
- e) At least five issues are related to poor solids control:
- Building of solids bed → Mechanical stuck pipe
 - Building of viscosity / high gel → high pressure losses → high ECD → fracture
 - High cuttings concentration in annulus → higher mud density in annulus → high ECD → lower ROP
 - Higher mechanical friction → loss of WOB → reduced ROP
 - Loss of filter control → thicker mud cake → differential pipe sticking

5.4 CUTTINGS CONCENTRATION II – SOLUTION

- a) Friction, drag, lifts cohesive, gravity. Make drawing. Rolling when $\sum M \geq 0$, lifting when $\sum F_z \geq 0$
- b) Stoke's law is valid only for infinitesimal dilution (one sphere), for small spheres ($r < 0.1\text{mm}$) and for laminar flow around the particle
- c) High ROP, high inclination, highly viscous mud, rolling, lifting etc.
- d) Two drawings are needed: One for these four forces; drag, lift, cohesion, gravity, and one for a rotating string with viscous coupling. The viscous coupling radius relative to R_0 , increase with RPM and climb the TJ at around 120.

5.5 DENSITY CONTROL – SOLUTION

- a) When weight material has to be added to the mud it is called weighted mud. To clean it, normally a 60 + 250 Mesh shakers + a centrifuge would be applied. Barite is preliminary taken out by the centrifuge and later re-injected.
- b) By combining this information:

$$\rho_2 = \frac{\sum m}{\sum V} \quad \text{and} \quad m_1 = V_1 / \rho_1, \quad \text{we obtain} \quad \Rightarrow \Delta V_B = \frac{(\rho_2 - \rho_1)}{\rho_B - \rho_2} V_1$$

Using it for the specified task:

$$\Delta V_B = \frac{60\,000(1.4 - 1.3)}{4.3 - 1.4} = 2\,092 \text{ l}$$

However, Barite is controlled by its mass, not volume:

$$\Delta m_B = \Delta V_B \cdot \rho_B = 2.092 \text{ m}^3 \cdot 4.3 \text{ ton} / \text{m}^3 = 9.1 \text{ ton}$$

c) In the next two tasks we simply take the weighted average of all densities:

$$\bar{\rho} = \frac{\sum \rho V}{\sum V} = \frac{\rho_1 V_1 + \rho_2 V_2 + \rho_3 V_3 + \rho_w \cdot V_w}{V_1 + V_2 + V_3 + V_w} = \frac{1\,500 \cdot 1 + 1\,800 \cdot 0.1 + 40 + m_B \cdot (m_B / 4300)}{1 + 0.1 + 40 / 2300 + m_B / 4300} \quad m_B = 143.2 \text{ kg}$$

$$\begin{aligned} \text{d) } \bar{\rho} &= 1.55 = \frac{\rho_1 V_1 + \rho_2 V_2 + \rho_3 V_3 + \rho_w \cdot V_w}{V_1 + V_2 + V_3 + V_w} \\ &= \frac{1\,500 \cdot 10 + 1\,600 \cdot 20 + 1\,900 \cdot 3 + V_w \cdot 1\,000}{10 + 20 + 3 + V_w} = 1\,550 \rightarrow V_w = 2.8 \text{ m}^3 \end{aligned}$$

5.6 DENSITY CONTROL – SOLUTION

a) Remaining volume $V_r = \frac{3}{5} V = 60 \text{ m}^3 \rightarrow$ Remove 40 m^3 and then add $V_{\text{add}} = V_w + V_b = 40 \text{ m}^3$
Density of added volume must also be 1.8 kg/l

$$\rho_{\text{add}} = \frac{m_1 + m_w + m_b}{V_1 + V_w + V_b}$$



Maastricht University *Leading in Learning!*

**Join the best at
the Maastricht University
School of Business and
Economics!**

Top master's programmes

- 33rd place Financial Times worldwide ranking: MSc International Business
- 1st place: MSc International Business
- 1st place: MSc Financial Economics
- 2nd place: MSc Management of Learning
- 2nd place: MSc Economics
- 2nd place: MSc Econometrics and Operations Research
- 2nd place: MSc Global Supply Chain Management and Change

Sources: Keuzegids Master ranking 2013; Elsevier 'Beste Studies' ranking 2012; Financial Times Global Masters in Management ranking 2012

**Maastricht
University is
the best specialist
university in the
Netherlands
(Elsevier)**

Visit us and find out why we are the best!
Master's Open Day: 22 February 2014

www.mastersopenday.nl



$$m_1 = \rho_1 \cdot V_1 = 1800 \cdot 60 = 108\,000 \text{ kg}$$

$$V_w + V_b = 40 \text{ m}^3$$

$$1800 = \frac{108\,000 + m_w + m_b}{100} \text{ kg/m}^3$$

$$m_w + m_b = 72\,000 \text{ kg}$$

$$m_w = V_w \cdot 1\,000$$

$$m_b = V_b \cdot 4\,300 = (40 - V_w) \cdot 4\,300$$

$$V_w \cdot 1\,000 + (40 - V_w) \cdot 4\,300 = 72\,000 \text{ kg}$$

$$V_w = 30.3 \text{ m}^3$$

$$V_b = 40 - 30.3 = 9.7 \text{ m}^3$$

$$m_b = 72\,000 - m_w = 72\,000 - 30.3 \cdot 1\,000 = 41\,700 \text{ kg}$$

Conclusion: Remove 40 m³ mud, add 30.3 m³ of water and 41 700 kg Barite to obtain 100 m³ mud of $\rho = 1800 \text{ kg/m}^3$ and LSGS of 3%.

b) Dump first $V_2 = 90 \cdot (0.055 - 0.035) / 0.055 = 40.9 \text{ m}^3$

Remaining volume $V_1 = 49.1$, $\rho_1 = 1\,600$, $m_1 = 78\,560 \text{ kg}$

$$\rho_w = 1\,000, \rho_b = 4\,300 \text{ kg}$$

Step 1: Add 40 900 kg of water and find new density:

$$\rho_{\text{new}} = (78\,560 + 40\,900) / 90 = 1\,327 \text{ kg/m}^3 = \rho_{\text{old}} \text{ in step 2.}$$

Step 2: Find out how much Barite must be added to reach the desired density of 1.7 kg/l

$$V_{\text{add}} = V_1 \frac{\rho_{\text{new}} - \rho_{\text{old}}}{\rho_{\text{add}} - \rho_{\text{new}}} = 90 \cdot (1.6 - 1.327) / (4.3 - 1.6) = 9.1 \text{ m}^3$$

The new volume content of Low Gravity Solids, becomes:

$$\text{LSGC}_2 = 0.03 \cdot (90 + 9.1) / 90 = 0.033 \rightarrow 3.3 \%$$

c) Necessary ρ_2 : $\rho_2 g h = 410 \cdot 10^5 \rightarrow \rho_2 = \frac{410 \cdot 10^5}{9.81 \cdot 3000} = 1393 \text{ kg/m}^3$

Fill a tank consisting of 10 m³ with new mud of ρ_2 :

From data: $V_1 = \text{volume old mud}$ $V_2 = 10 \text{ m}^3$

$$\rho_1 = 1\,200 \text{ kg/m}^3 \quad V_b = \text{volume barite} \quad \rho_b = 4\,300 \text{ kg/m}^3$$

Increase from r_1 to r_2 :

$$\rho_2 = \frac{m_1 + m_b}{V_1 + V_b}, \quad V_b = \frac{m_b}{\rho_b}, \quad \rho_1 = \frac{m_1}{V_1}$$

$$V_1 + V_b = 10 \text{ m}^3 \rightarrow V_1 = (10 - V_b)$$

$$\rho_2 = \frac{(10 - V_b) \cdot \rho_1 + V_b \rho_b}{(10 - V_b) + V_b} \Rightarrow V_b = 0.6226 \text{ m}^3 \Rightarrow V_1 = 9.3774 \text{ m}^3$$

It is shown that 0.6226 m³ of Barite requires 9.3774 m³ of water to produce 10 m³ mud of density 1.393 kg/l.

5.7 ECD. BARITE – SOLUTION

Start by converting to SI units. When $\rho_{mud} > \sim 1.5 \text{ kg/l}$, the barite concentration is high. At stillstand, most mud types quickly develop a yield point, and barite is suspended in the gelled mud. During pumping of mud in laminar mode, any existing gel is broken, and barite will not be held in suspension as during stillstand with gelled mud. However, the mud will under these conditions exhibit a high effective viscosity. Barite will, nevertheless, slip slowly downwards due to gravity. Agglomeration may also affect the settling rate. Barite has a specific density of 4.3, and an average particle size of approximately $20 \mu\text{m}$. In accordance with Stokes's law of settling, Barite particles will settle, but as indicated above, very slowly. However, wellbore inclination will shorten the settling distance to only a few centimetres, and a stratified bed of Barite and cuttings will form. The stratified layers of solids will, when the angle of repose is surpassed, slide downwards. The critical angle of repose is found mainly in the build-up section of the well, and here sliding takes place. After the first "landslide", the Barite concentration in the mud has become slightly lower and accordingly, also the viscosity. Barite settling will now be a fraction faster, and the process continues at accelerated speed. The self-preserving dynamics may lead to separation of almost all the barite in the fluid in the build-up section, especially during still stand after tripping-out of the hole. The pile of Barite at the bottom of the build-up section may cause pipe sticking. Worse is the reduction of mud weight. It may disrupt the safety.

The following summary of guidelines to obtain efficient hole-cleaning is based on field experiences and on many laboratory investigations:

- a) Apply micro-Barite or equivalent. Such material systems have an average particle size of $2 \mu\text{m}$
- b) Use top-drive to allow for pipe rotation and redistribution of the settling Barite and cuttings while tripping and drilling
- c) Maximize fluid velocity during drilling and reaming by increasing pumping output and/or use large diameter drill string. This improves the hydraulics and agitation of cuttings. Use in addition downhole flow enhancers
- d) Design mud rheology so that it enhances turbulence in the annulus (if ECD allows). Turbulent flow will bring the cuttings and Barite back into the flow stream if point c) above "failed"
- e) Perform frequent wiper trips

5.8 ECD. FLOW RATE & FLUID CONSISTENCY – SOLUTION

- a) In order to determine the ECD we need to estimate the pressure loss in the annulus. The mud has some gel, so we assume the Bingham model will suit well.

$$\mu_{pl} = \frac{\tau_{600} - \tau_{300}}{\gamma_{600} - \gamma_{300}} = \frac{51.7 - 30.6}{1022 - 511} = 0.0413 \text{ Pas}$$

$$\tau_0 = 51.7 \text{ Pa} - 1022 \cdot 0.0413 \text{ Pas} = 9.5 \text{ Pa}$$

Although the flow rate is rather high, we assume laminar flow in the annulus. However, if the purpose were to find the exact Dp we would need to check the Reynolds number to confirm this. Annular pressure loss:

$$\Delta p_a = 48 \cdot \mu_{pl} \cdot \left[\frac{L_{DC/OH} \cdot v_{DC/OH}}{(d_o - d_i)_{DC/OH}^2} + \frac{L_{DP/OH} \cdot v_{DP/OH}}{(d_o - d_i)_{DP/OH}^2} + \frac{L_{DP/C} \cdot v_{DP/C}}{(d_o - d_i)_{DP/C}^2} \right] +$$

$$6 \cdot \tau_0 \cdot \left[\frac{L_{DC/OH}}{(d_o - d_i)_{DC/OH}} + \frac{L_{DP/OH}}{(d_o - d_i)_{DP/OH}} + \frac{L_{DP/C}}{(d_o - d_i)_{DP/C}} \right] = \Delta p_a = 385179 \text{ Pa} = 3.85 \text{ bar}$$

Now the ECD:

$$ECD = \frac{P_{hydr} + \Delta p_{ann}}{g \cdot h} = \frac{p \cdot g \cdot h + \Delta p_{ann}}{g \cdot h}$$

$$ECD = 1250 + \frac{3.85 \cdot 10^5}{0.0981 \cdot 2100} = 1270 \text{ kg/m}^3$$



Empowering People. Improving Business.

BI Norwegian Business School is one of Europe's largest business schools welcoming more than 20,000 students. Our programmes provide a stimulating and multi-cultural learning environment with an international outlook ultimately providing students with professional skills to meet the increasing needs of businesses.

BI offers four different two-year, full-time Master of Science (MSc) programmes that are taught entirely in English and have been designed to provide professional skills to meet the increasing need of businesses. The MSc programmes provide a stimulating and multi-cultural learning environment to give you the best platform to launch into your career.

- MSc in Business
- MSc in Financial Economics
- MSc in Strategic Marketing Management
- MSc in Leadership and Organisational Psychology

www.bi.edu/master



**NORWEGIAN
BUSINESS SCHOOL**



b) What is the ECD during drilling? Production of mud and cuttings:

$$q_{\text{mud}} = 3\,500 / (1000 \cdot 60) = 0.058 \text{ m}^3/\text{s}$$

$$q_{\text{cuttings}} = \text{ROP} \cdot A_{\text{bit}} = 3\,500 / (1000 \cdot 60) \cdot 3.14/4 \cdot (17.5 \cdot 0.0254)^2 = 0.0022 \text{ m}^3/\text{s}$$

$$\text{Total flow rate in annulus: } q_{\text{ann}} = q_{\text{mud}} + q_{\text{cuttings}} \cong q_{\text{mud}}$$

Volumetric concentration of cuttings:

$$c_{\text{cuttings}} = q_{\text{cuttings}} / (q_{\text{mud}}) = 0.0022 / 0.058 = 0.038$$

We assume the cuttings will slip; $R_t = 0.75$

$$c_{\text{cuttings}} = 0.038 / 0.75 = 0.051$$

ECD contribution will be enhanced by the higher density of cuttings:

$$ECD = \rho_{\text{mud}} \cdot c_{\text{mud}} + \rho_{\text{cuttings}} \cdot c_{\text{cuttings}} = 1.25(1 - 0.051) + 2.4 \cdot 0.051 = 1.31 \text{ kg/l}$$

The effect of slightly increasing well length is neglected.

$$\begin{aligned} \text{The casing shoe's equivalent fracture density: } \rho_{\text{fr}} &= p / gh = 228 \cdot 10^5 / (1\,800 \cdot 9.81) \\ &= 1\,291 \text{ kg/m}^3 \end{aligned}$$

c) Suggested procedure to determine pressure profile, which is a $f(T)$:

- 1) Find the stable temperature profile in the well in accordance with Chapter 7 of the Text book. Default temperature gradient in sedimentary rocks = $(10 + 0.03)^\circ\text{C/m}$.
- 2) Look up the thermal coefficients of materials, α , in a handbook;

$$\alpha_{\text{steel}} =$$

$$\alpha_{\text{water}} =$$

- 3) Mud density: $\rho_i = \rho_o - \rho_o \cdot \alpha_{(T_i - T_{i-1})}$ at each depth interval Δh

- 4) Estimate $\rho_i = f(D(f(T)))$

- 5) Find p_{bottom} as $\sum \rho_i g \Delta h$

- 6) $\rho_{\text{equiv}} = \frac{p_{\text{bottom}}}{g \sum \Delta h}$

5.9 WATER ACTIVITY – SOLUTION

- a) One definition of water activity is the vapor pressure of its salt water solution and compares it to the water vapor pressure above distilled water.

$$A_w = \frac{P_{\text{saline water}}}{P_{\text{distilled water}}}$$

Water solution: Distilled water thus has a water activity of 1.00. All water molecules are freely moving around, not electrostatically bound to salt ions. A_w will diminish at increasing salt content.

Pore water: Find the A_w of clay through its in-situ weight and then by comparing with clays with known A_w . Thus A_w of water phase is determined.

- b) Salt ions attract polar water and make it in-active. Distilled water has a water activity 1.0 whereas for saline water it is less than 1.0.

- c) Clay swelling leads to increased pore water pressure according to this equation:

$$p_{\text{swelling}} = -\frac{RT}{V_w} \ln \left(\frac{p_{w,\text{clay}}}{p_{w,\text{mud}}} \right)$$

V_w = Molar volume of water vapor;

Most shale formations contain water since shale is water wet. Water sensitive clay materials, such as smectite, illite and mixed – layer clays, will adsorb water and swell. This leads to an elevated localized pressure around the wellbore. The pressure may surpass the material strength; the material will disintegrate and collapse. Water is transported into the shale through different mechanisms (hydraulic pressure, osmosis, diffusion etc.).

- d) Adding K-salt to WBM: Dissolved salt will bind water and hinder it to evaporate; the water vapor pressure will decline and so also the measured A_w . The A_w is inversely proportional to salinity.
- e) If $A_{w, \text{OBM}} \geq A_{w, \text{pore}}$, water will be drawn from the droplets in the OBM on the wellbore wall and into the formation, making the shale swell.
If $A_{w, \text{OBM}} \leq A_{w, \text{pore}}$, the shale will be dried out and become brittle.
Yes, it can be reduced by creating a filter in the shale. This can be done by adding particles to the water phase where the average particle size distribution 1/3 of the average pore throat (indeed small).

5.10 SHALE STABILITY – SOLUTION

- a) Using Figure 5-6 in the task section a calcium chloride concentration of 28.2 % by weight is needed to give an activity of 0.69.
- b) Take an "in-situ" cut of the core, crush it and place it in a desiccator (completely air tight), expose it to different humidities (vapour pressure) through designed brines. The weight of the exposed sample will gradually convert to typical weight of this type of shale. Through this comparison the water activity in the core can be determined. Since this is the water activity of the shale's pore water, the water activity of the mud should be identical, to avoid swelling or shrinking of the shale.
- c) Oil does not penetrate clay because the capillary forces opposing the flow are too large;

$$p_c = \frac{2 \cdot \sigma_f \cdot \cos \theta}{r}$$

This depends on the wettability (which governs the θ). For oil to be the wetting phase against the formation/cuttings/steel a wetting agent must be added to the base oil. If water is emulsified into the oil, the water activity of the water phase must be controlled properly.

Emulsifier is used to reduce the surface tension between oil and water, enabling smaller droplets, enhancing emulsion stability. Wetting agents make sure that oil is wetting the shale.

5.12 WELLBORE PROBLEMS – SOLUTION

- a) Lots of material in the mud (cuttings, cavings, sloughing shale), combined with small and large washouts, material tends to accumulate here. During tripping, material is scraped and squeezed.

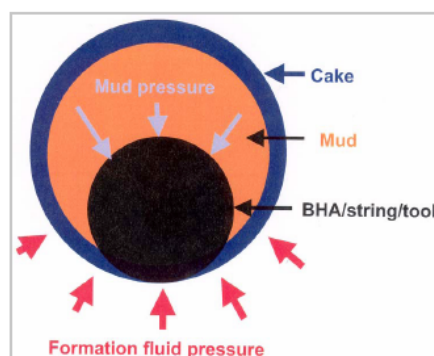


Figure 5-12. Differential sticking mechanism.

Differential sticking: Once the drill string touches the wellbore wall, the mud pressure, which is higher than the formation fluid pressure, holds the string in place. The cake forms a seal, and sticking occurs, as shown in Figure 5-12.

Need help with your dissertation?

Get in-depth feedback & advice from experts in your topic area. Find out what you can do to improve the quality of your dissertation!

Get Help Now



Go to www.helpmyassignment.co.uk for more info



Helpmyassignment



b) The consequences of a stuck pipe are very costly. They include:

- Lost drilling time spent on freeing the pipe, and on fishing, if jarring did not free the string
- Abandon tools in the hole because fishing was given up.

Rules of Thumb

1. Begin working the string immediately. Jar in the opposite direction to the pipe movement prior to becoming more stuck.
2. Work the pipe to their strength limits.
3. If obtaining movement down, concentrate on expanding downward - and vice versa.
4. In cases of hole bridging/packing off, concentrate on downward working. Increase the applied working force in gradual increments up to the maximum.

c) Salt tends to "flow" at high temperature and pressure. Use high mud weight and a mud that tend to dissolve salt (to keep the wellbore diameter as large as possible). WBM can be used with some additives. Halite is stable and exhibit neglectable creep tendency.

d) Dominating mechanisms causing lost circulation are:

- low pressure window
- high ECD (promote filter cake)

Counter measures are:

- improved hole cleaning
- improved ECD - control

Wellbore breathing (ballooning) (any two sentences of the suggested ones below are enough for obtaining full score).

- The onset of wellbore breathing, often referred to as wellbore ballooning, is typically an indicator of imminent lost circulation.
- Wellbore breathing is associated with fractures that open when annular pressure is applied to the wellbore. They close when the pressure is reduced.
- These fractures will fill with drilling fluid when open and subsequently return the fluid when the pumps are off.
- One of the more severe consequences of wellbore breathing is the misinterpretation of the observed flow as a kick when the pumps are shut down.
- Implementing well control procedures including increasing the mud weight is often enough to propagate the existing fractures leading to severe loss of circulation, a situation that is very difficult to manage.

5.11 SHALE STABILITY - SOLUTION

- a) By adding salt to the mud's water phase corresponding to A_w of pore water. No osmotic force between mud and clay, and thus no water driven swelling. OBM consists of minimum 5 ingredients:
1. Base oil
 2. Water
 3. Emulsifier (surface active additive I)
 4. Surface wetting (surface active additive II)
 5. Salt
- b) K^+ is geometrically fitting in between the Montmorillonite platelets and leads to high inter-platelet attraction (low swelling).
- c) The higher concentration, the more K^+ is exchanged.
- d) Yes, it can be reduced by creating a filter in the shale. This can be done by adding particles to the water phase where the average particle size distribution 1/3 of the average pore throat size distribution.
- e) Just like for WBM.
- f) Water flow, ion-flux, pressure flux, leading to instable wellbore wall.
- g) Osmotic, non-invading drilling fluid.
- h) Cyclic spalling, but also fractures and kick.